

Topological Persistence in Computer Vision: Applications to Segmentation and Classification

Qian Ge

Outline

- **Introduction**
- **Image Segmentation Framework**
- **Persistence Homology**
- **Consensus-based Image Segmentation**
- **Obstacle Detection of Outdoor Scene**
- **Conclusion and Future Work**

Image Segmentation

- Image segmentation clusters the image pixels into a set of groups visually distinct and uniform with respect to some properties.
- Region of interest depends on applications.



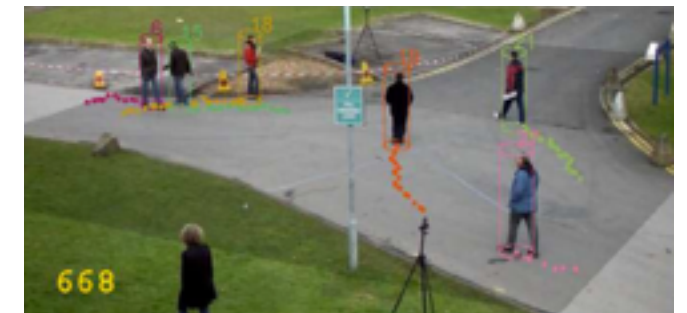
Image Segmentation

- Applications

Object Recognition



Object Tracking



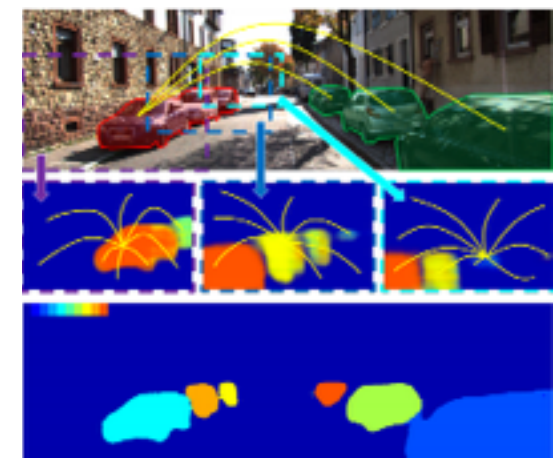
Video Surveillance



Image Segmentation



Autonomous Driving



Medical Imaging

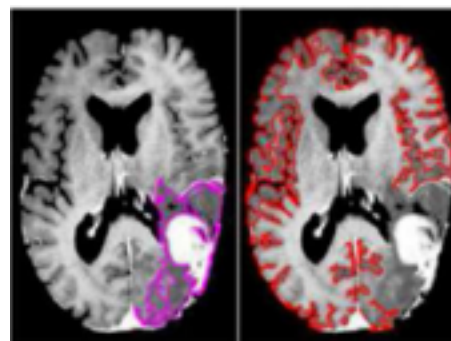
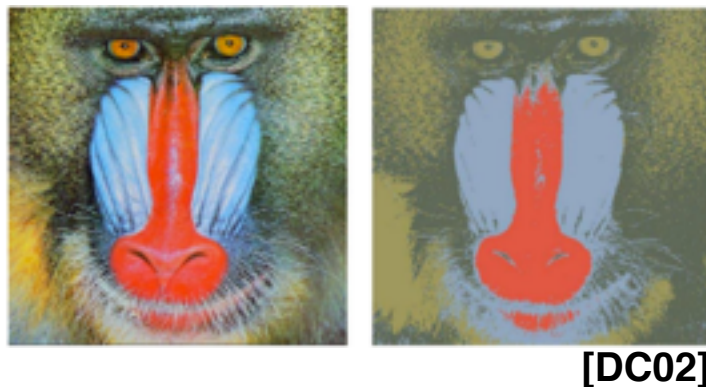


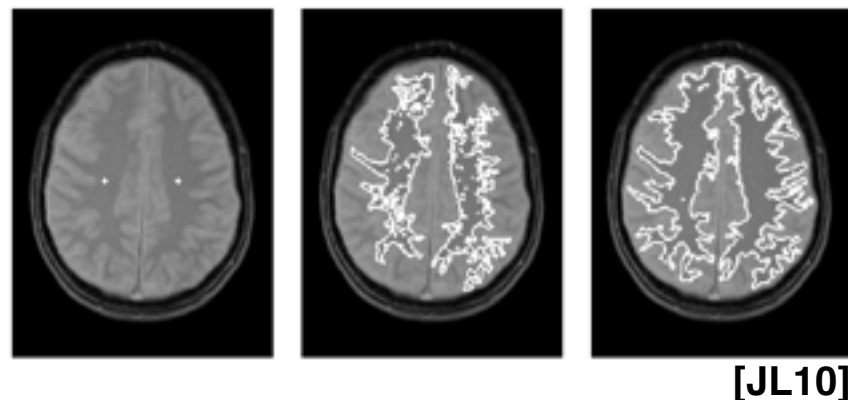
Image Segmentation

- Grouped by methodology:

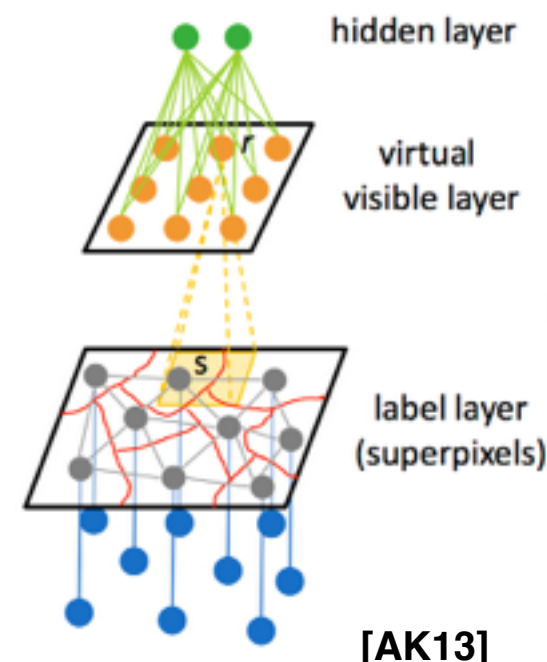
Clustering-based



Region Growing



Graph-based



Supapixel-based



Edge-based



<http://www.roborealm.com/help/Canny.php>

[DC02] Dorin Comaniciu and Peter Meer. 2002. Mean Shift: A Robust Approach Toward Feature Space Analysis. IEEE Trans. Pattern Anal. Mach. Intell. 24, 5 (May 2002), 603-619.

[AK13] A. Kae, K. Sohn, H. Lee and E. Learned-Miller, "Augmenting CRFs with Boltzmann Machine Shape Priors for Image Labeling," 2013 IEEE Conference on Computer Vision and Pattern Recognition, Portland, OR, 2013, pp. 2019-2026.

[JL10] J. L. Rose, T. Grenier, C. Revol-Muller and C. Odet, "Unifying variational approach and region growing segmentation," 2010 18th European Signal Processing Conference, Aalborg, 2010, pp. 1781-1785.

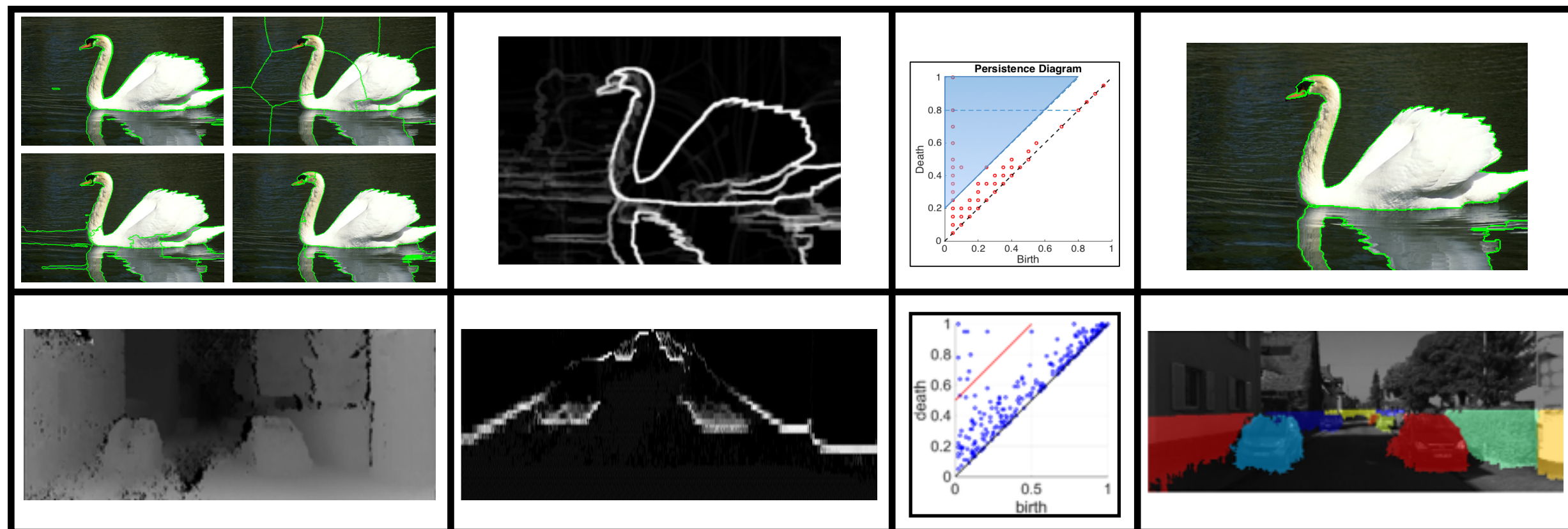
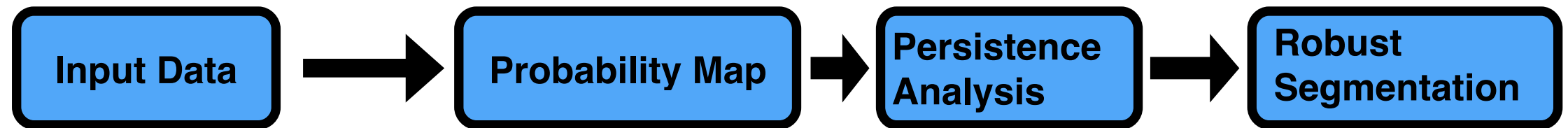
[RA12] Radhakrishna Achanta, Appu Shaji, Kevin Smith, Aurelien Lucchi, Pascal Fua, and Sabine Susstrunk. 2012. SLIC Superpixels Compared to State-of-the-Art Superpixel Methods. IEEE Trans. Pattern Anal. Mach. Intell. 34, 11 (November 2012), 2274-2282.

Why Robust?

- **Robust to noise, parameter selection, image quality and resolution**
 - Medical images are often polluted noisy.
 - User inputs cannot be the same every time.
 - Outdoor scene images quality varies over time.

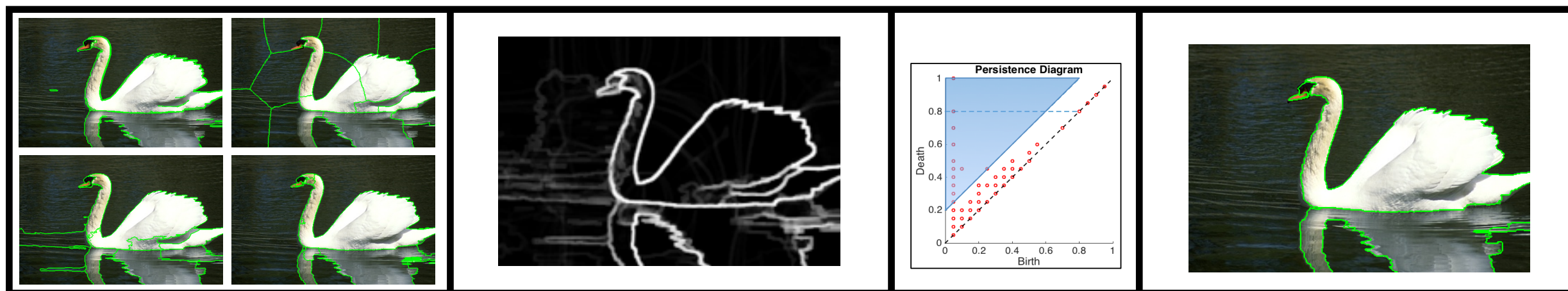
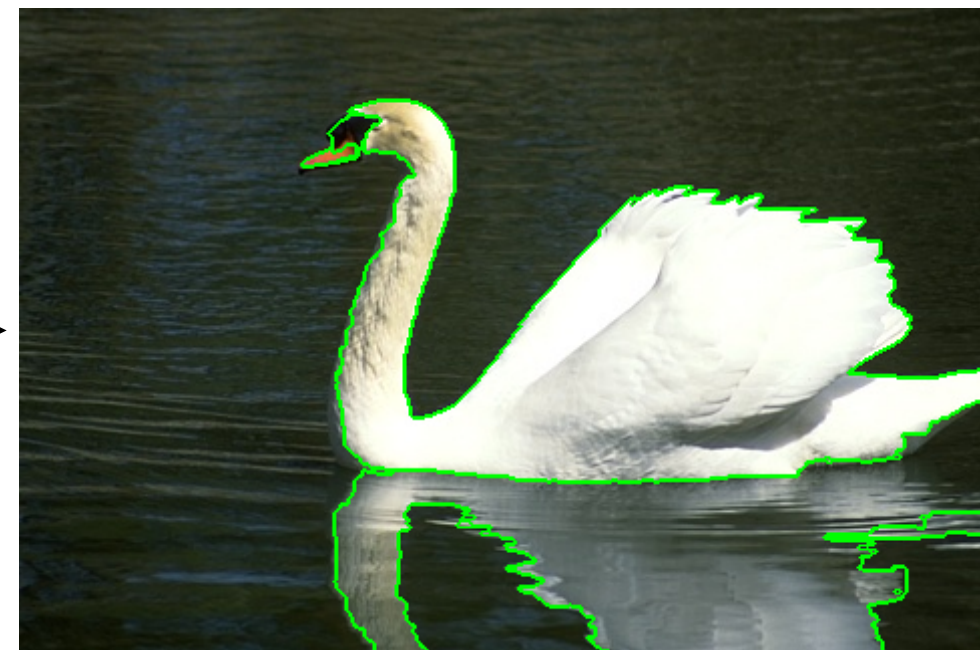
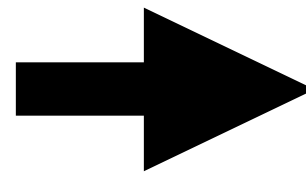
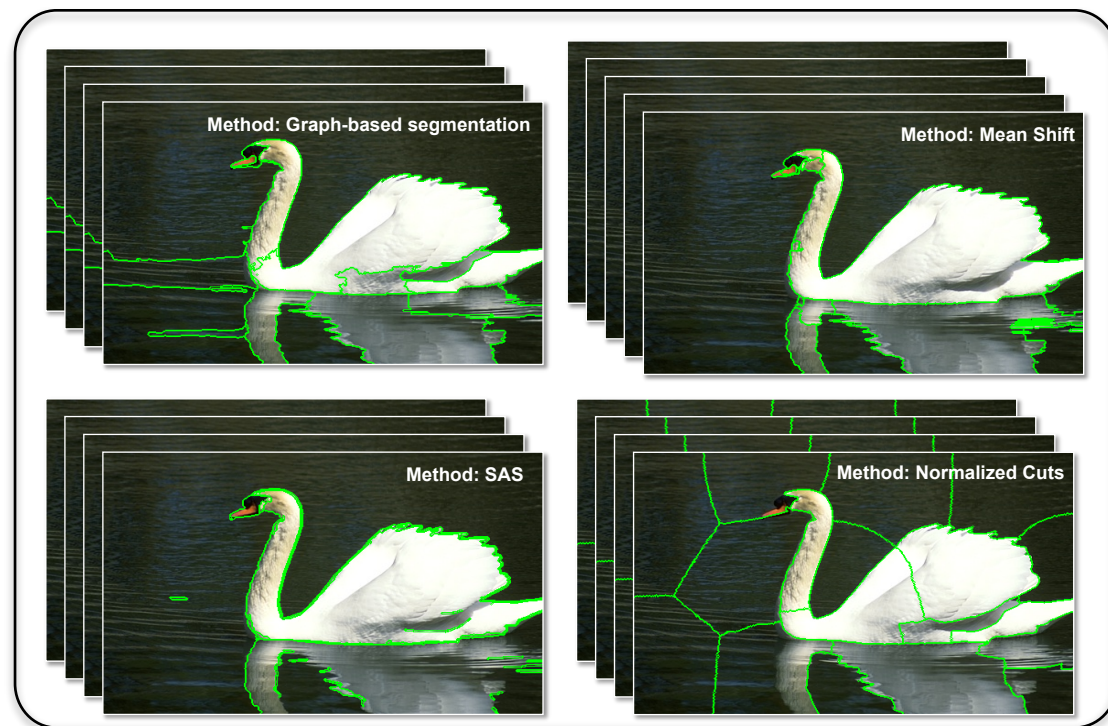


Framework of Robust Segmentation



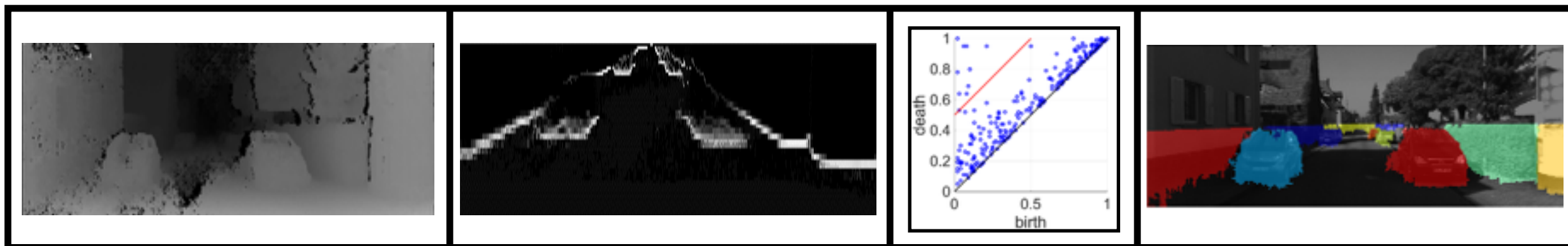
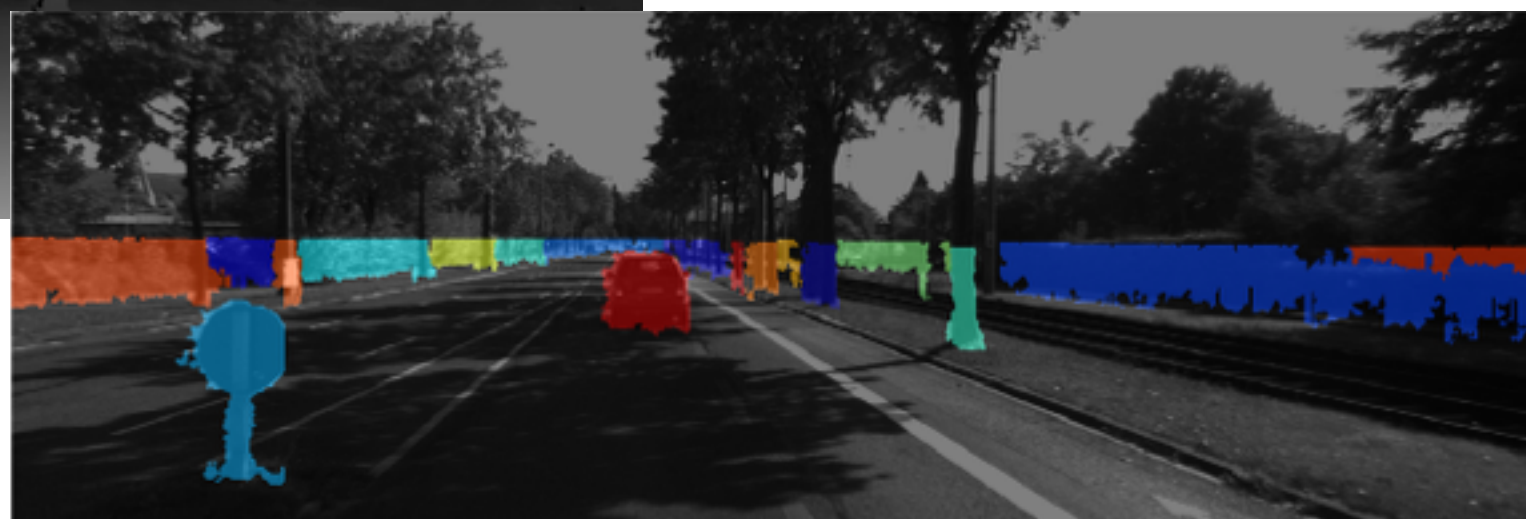
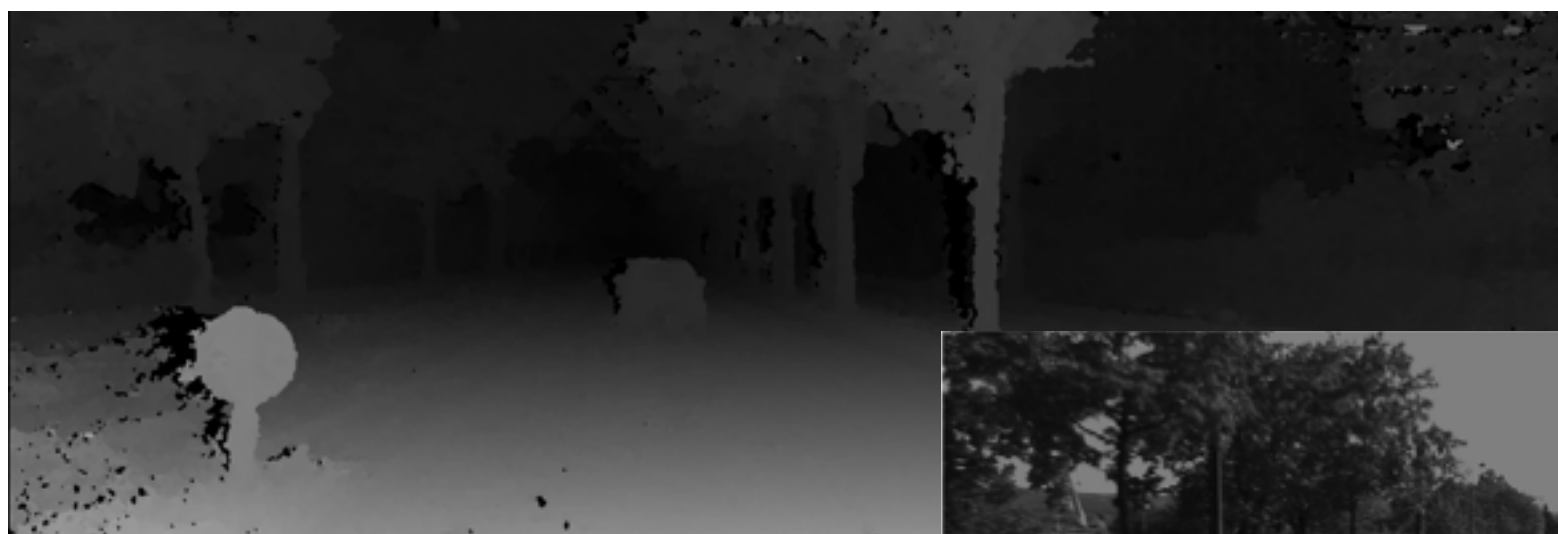
Framework of Robust Segmentation

- Consensus-based image segmentation



Framework of Robust Segmentation

- Obstacle segmentation of outdoor scene

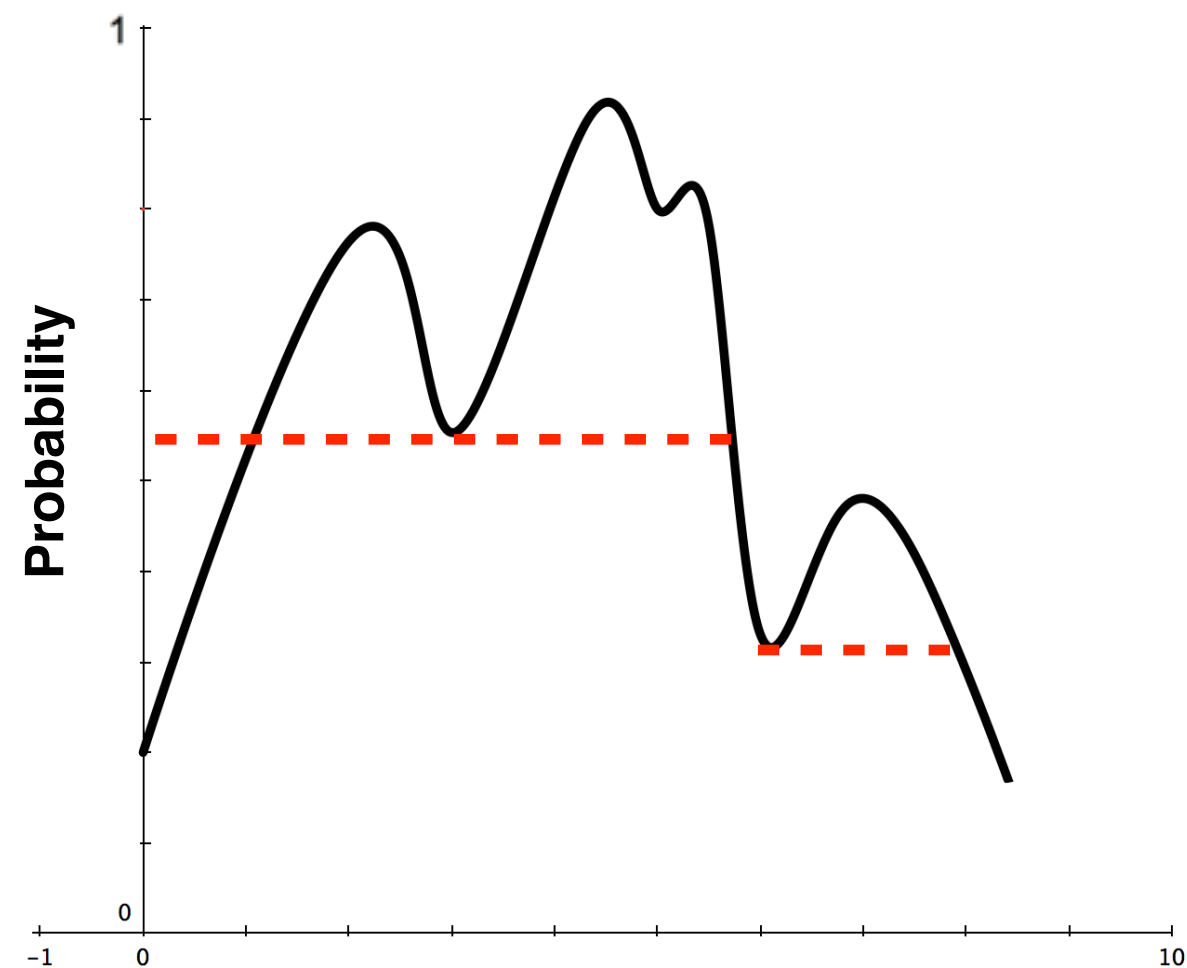
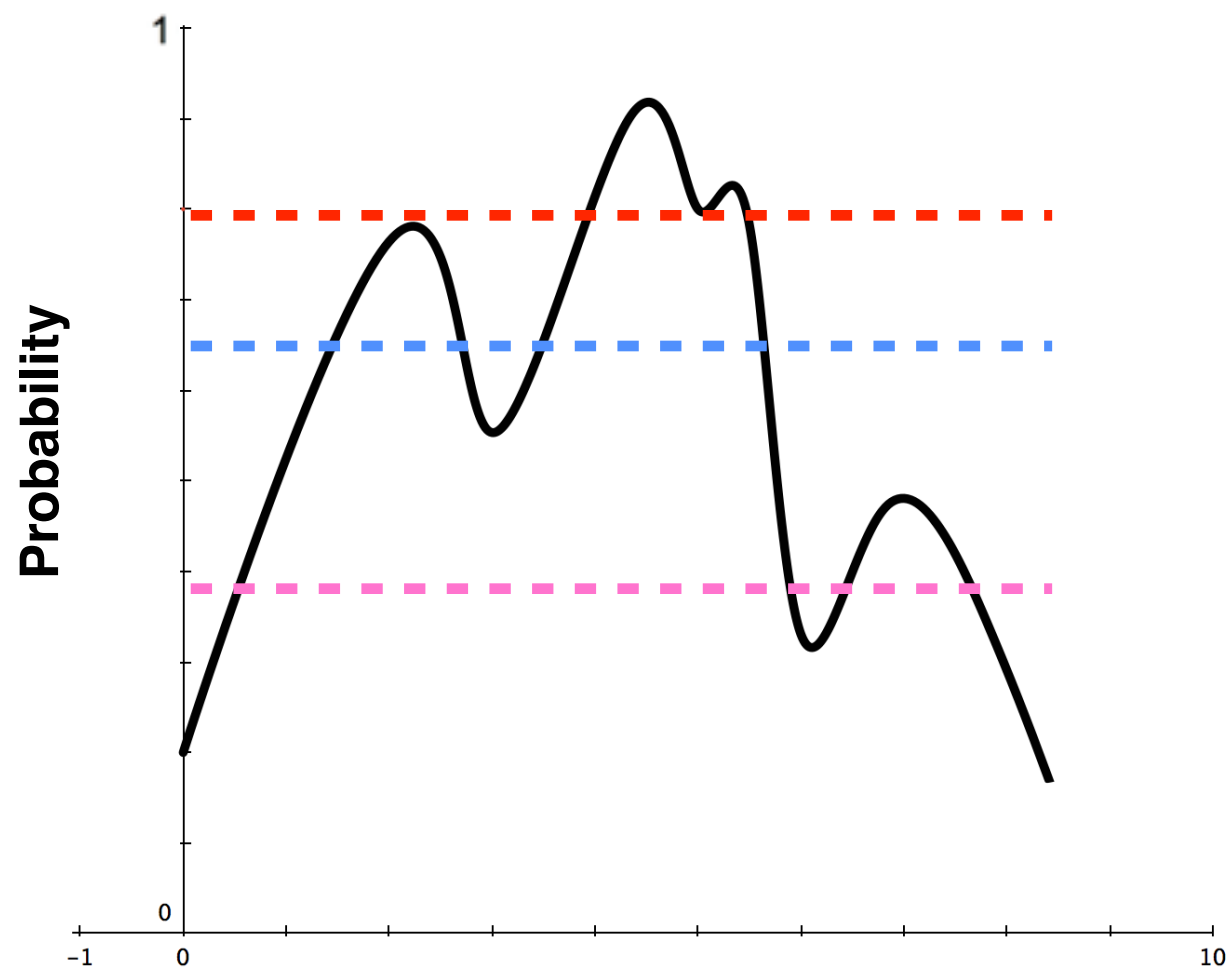


Contribution

- ▶ Present an innovative framework for image segmentation based on topological persistence which is robust to image conditions and parameter selection.
- ▶ Applied to consensus-based image segmentation which is able to get better segmentation results.
- ▶ Applied to obstacle detection in outdoor scene for autonomous driving which is robust to parameter selection.

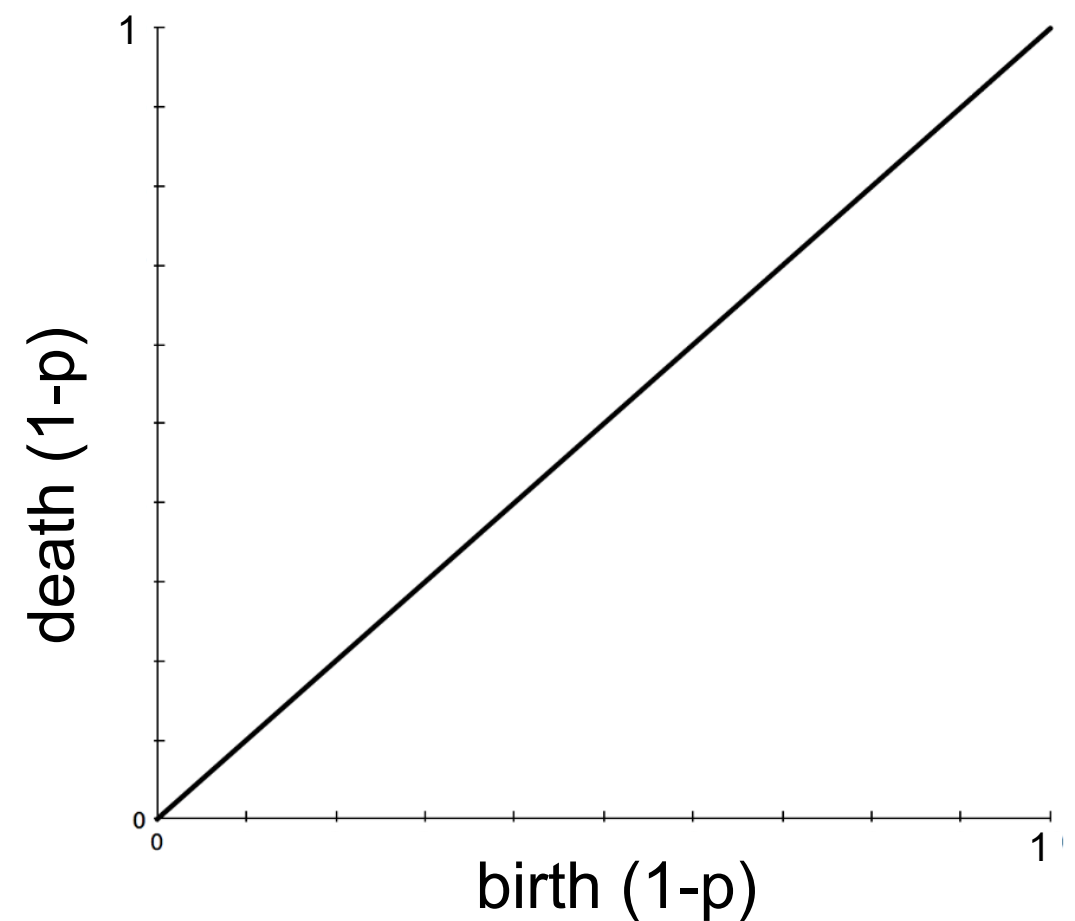
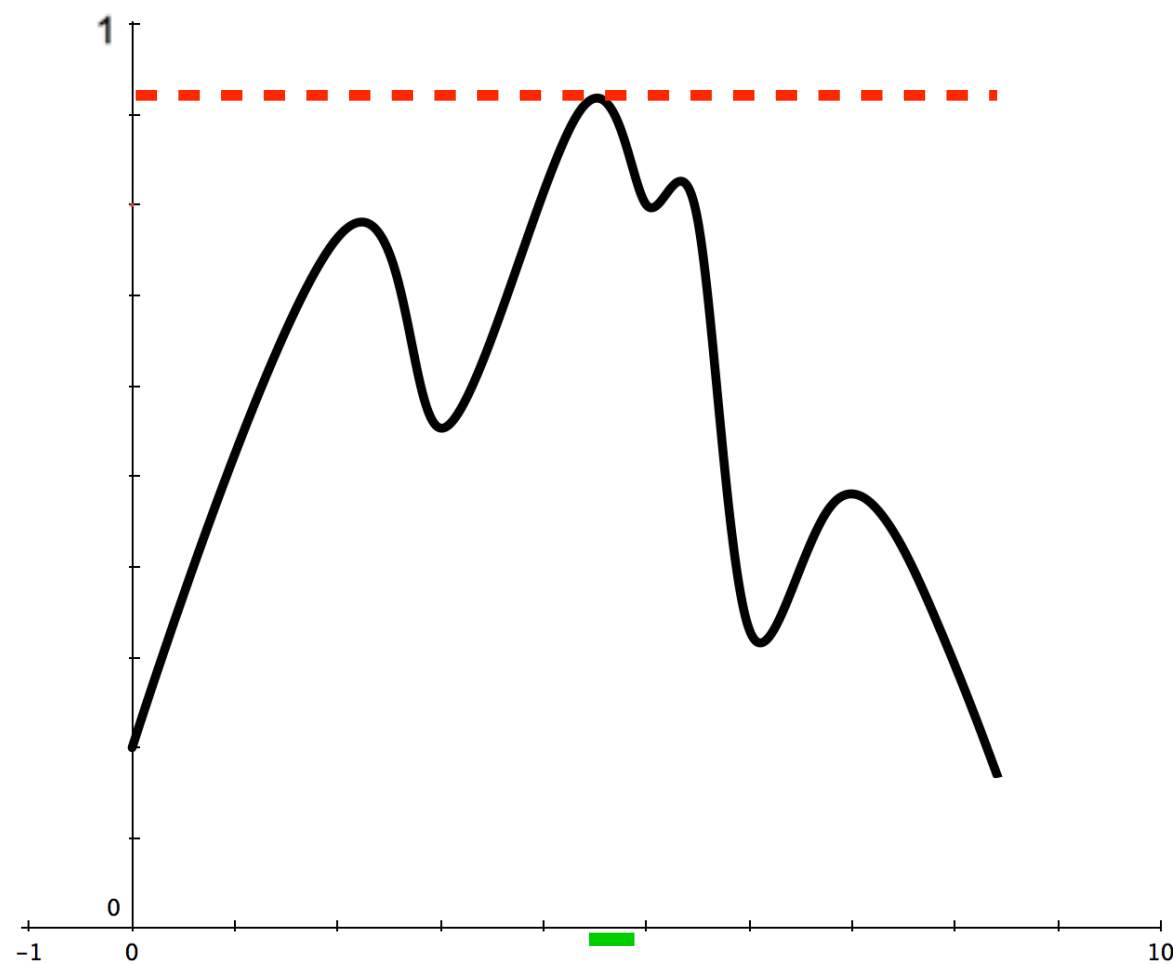
Persistent Homology

- For image segmentation, we borrow the concept of persistent homology to extract persistence regions and avoid noise.



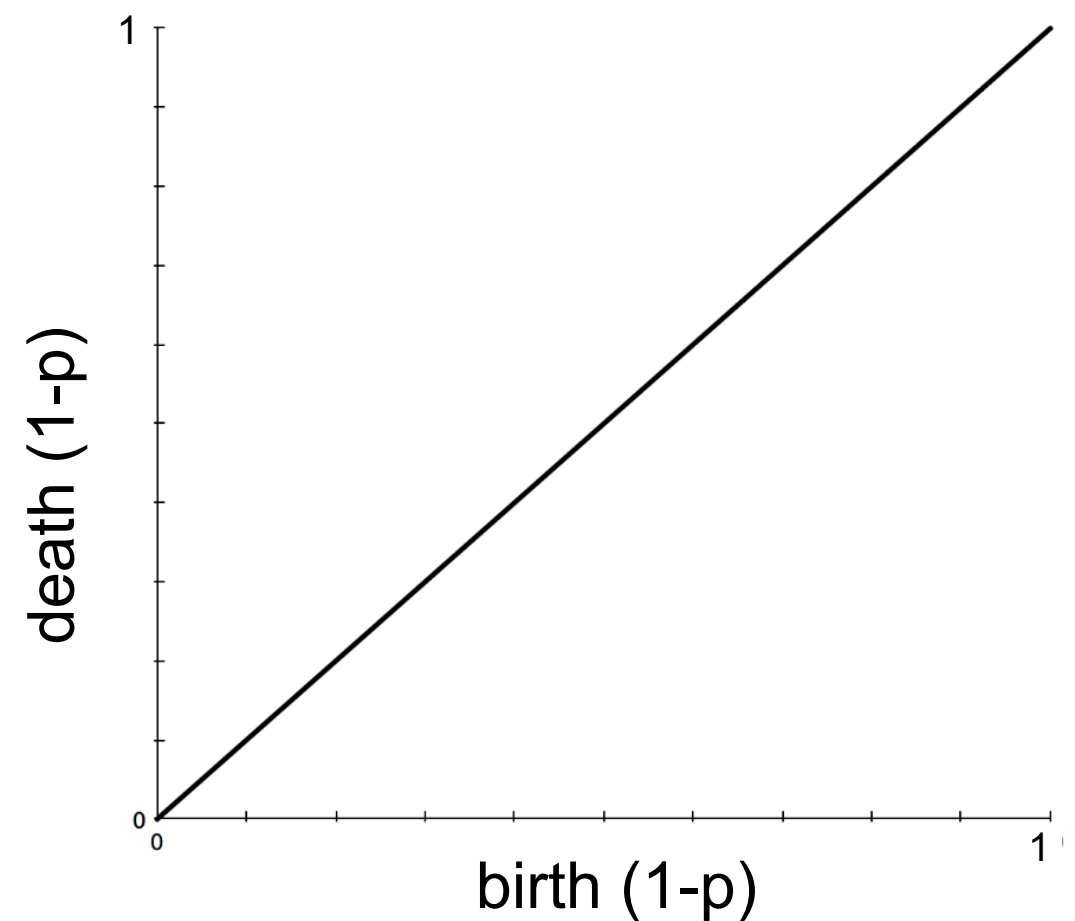
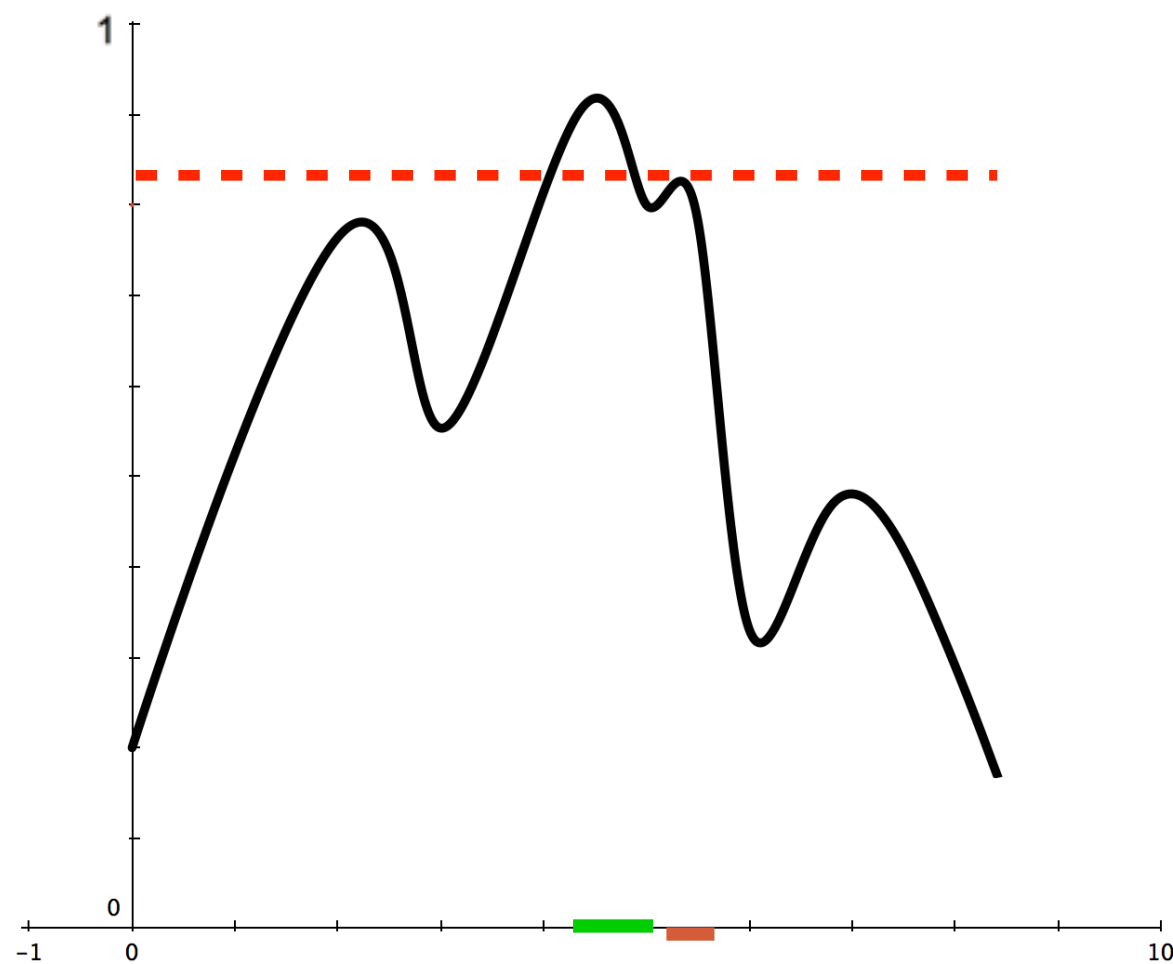
Persistent Homology

- Topological persistence



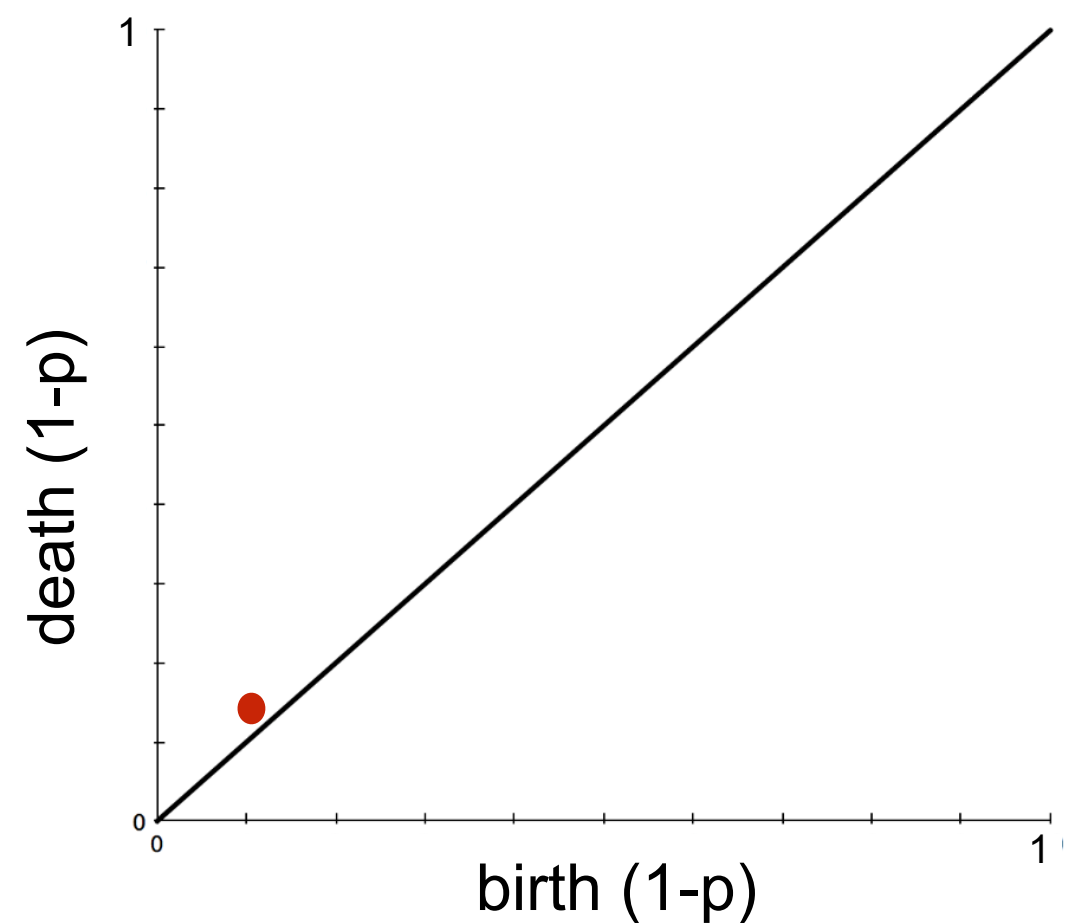
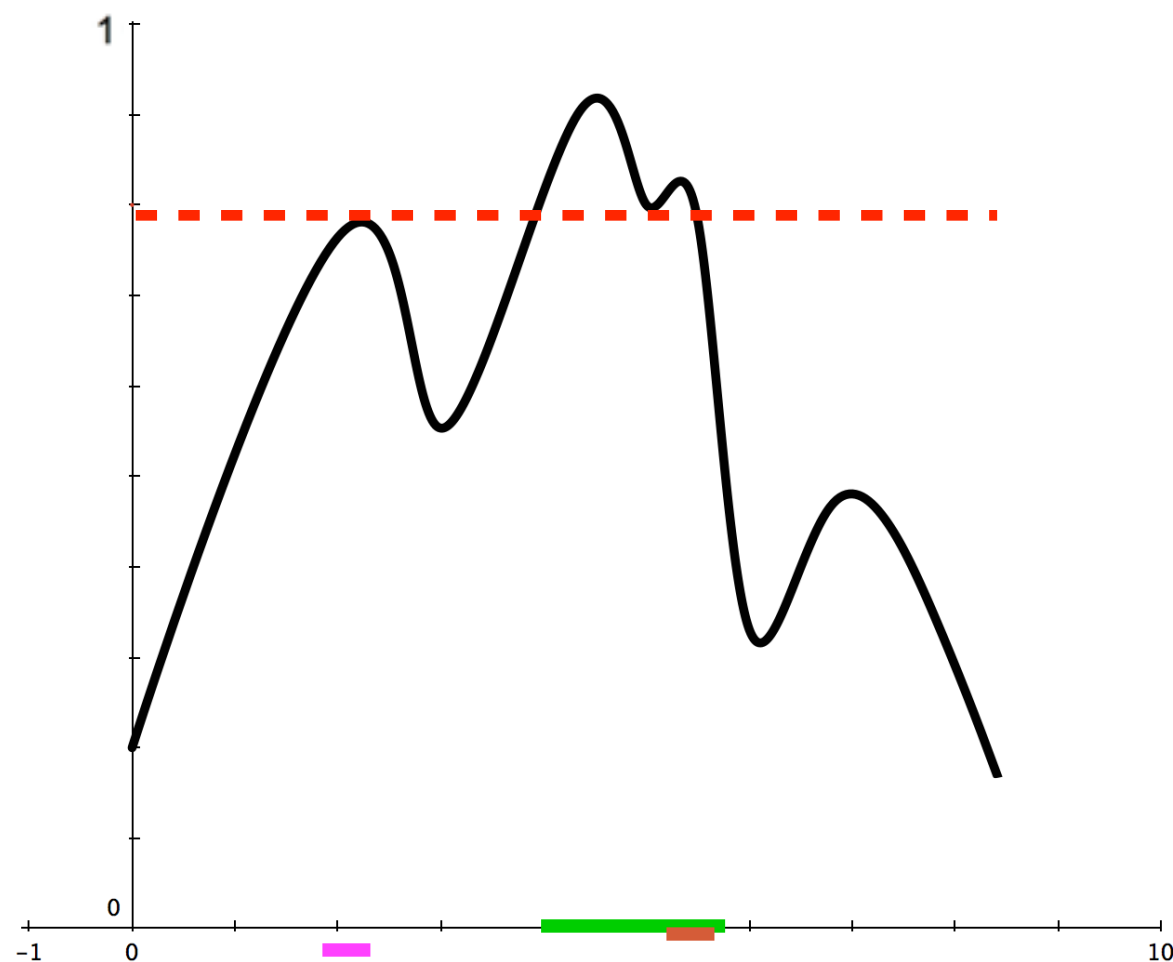
Persistent Homology

- Topological persistence



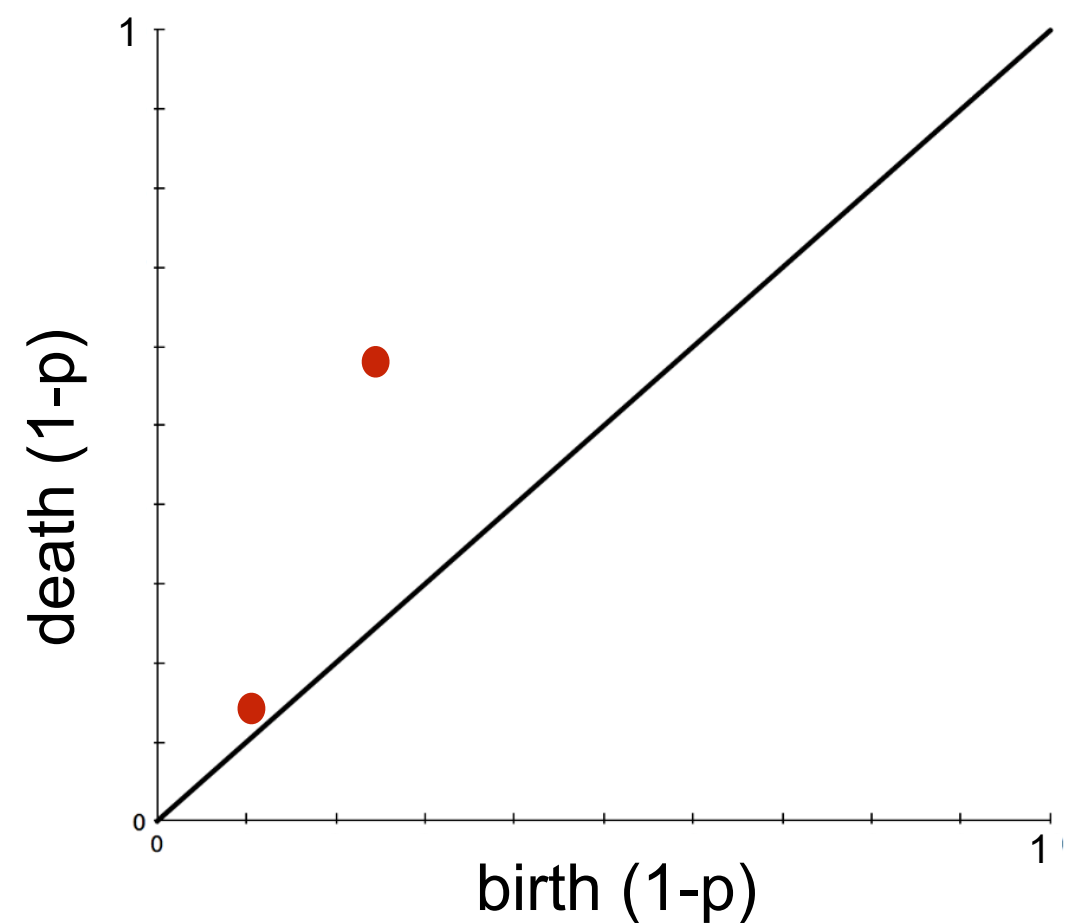
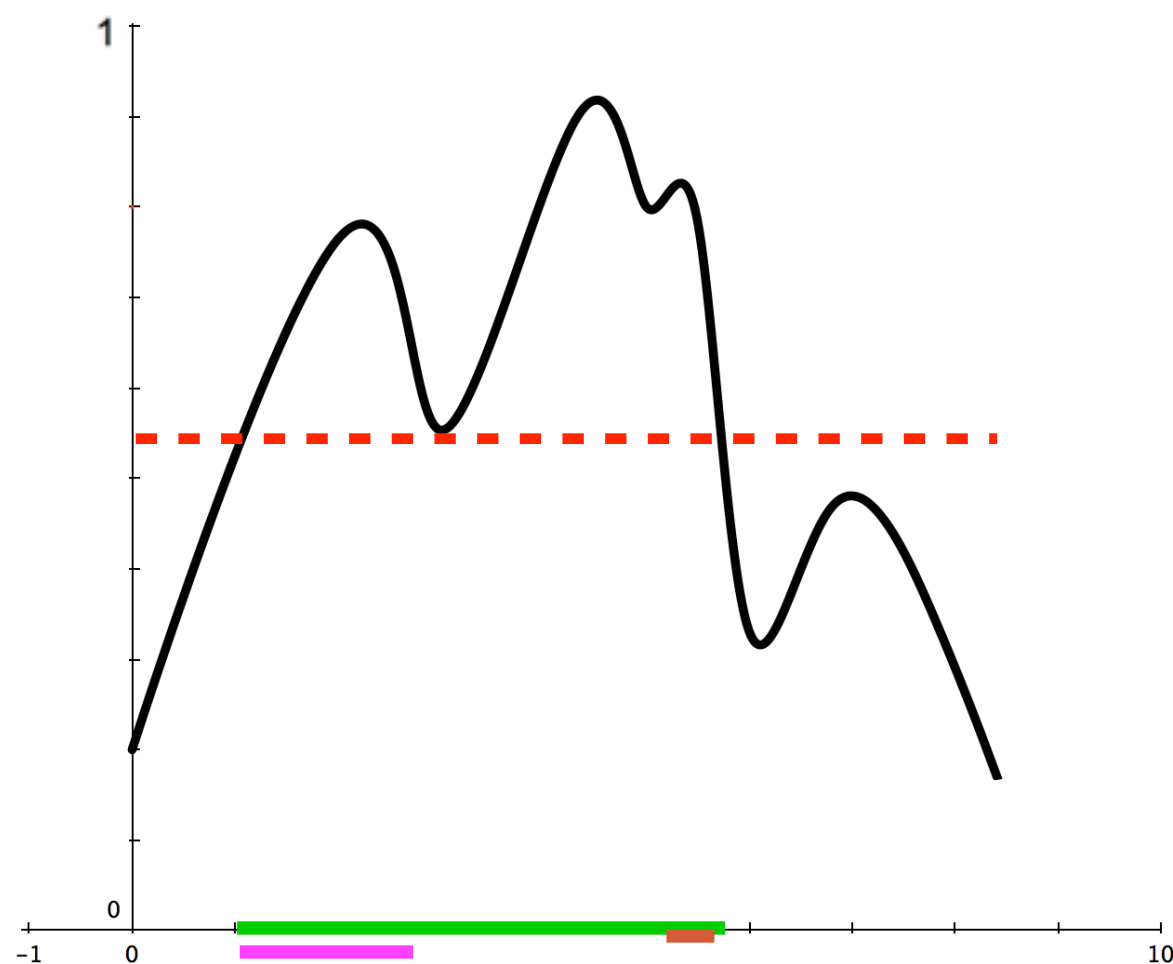
Persistent Homology

- Topological persistence



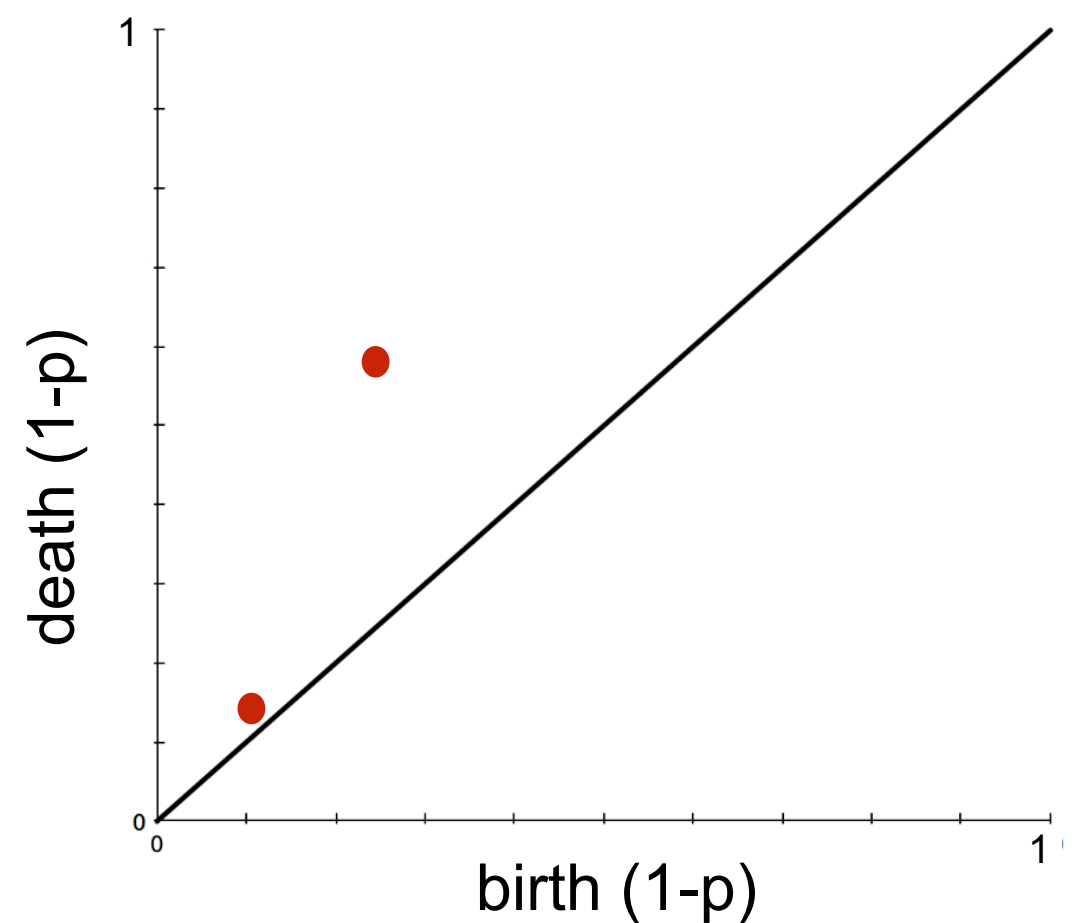
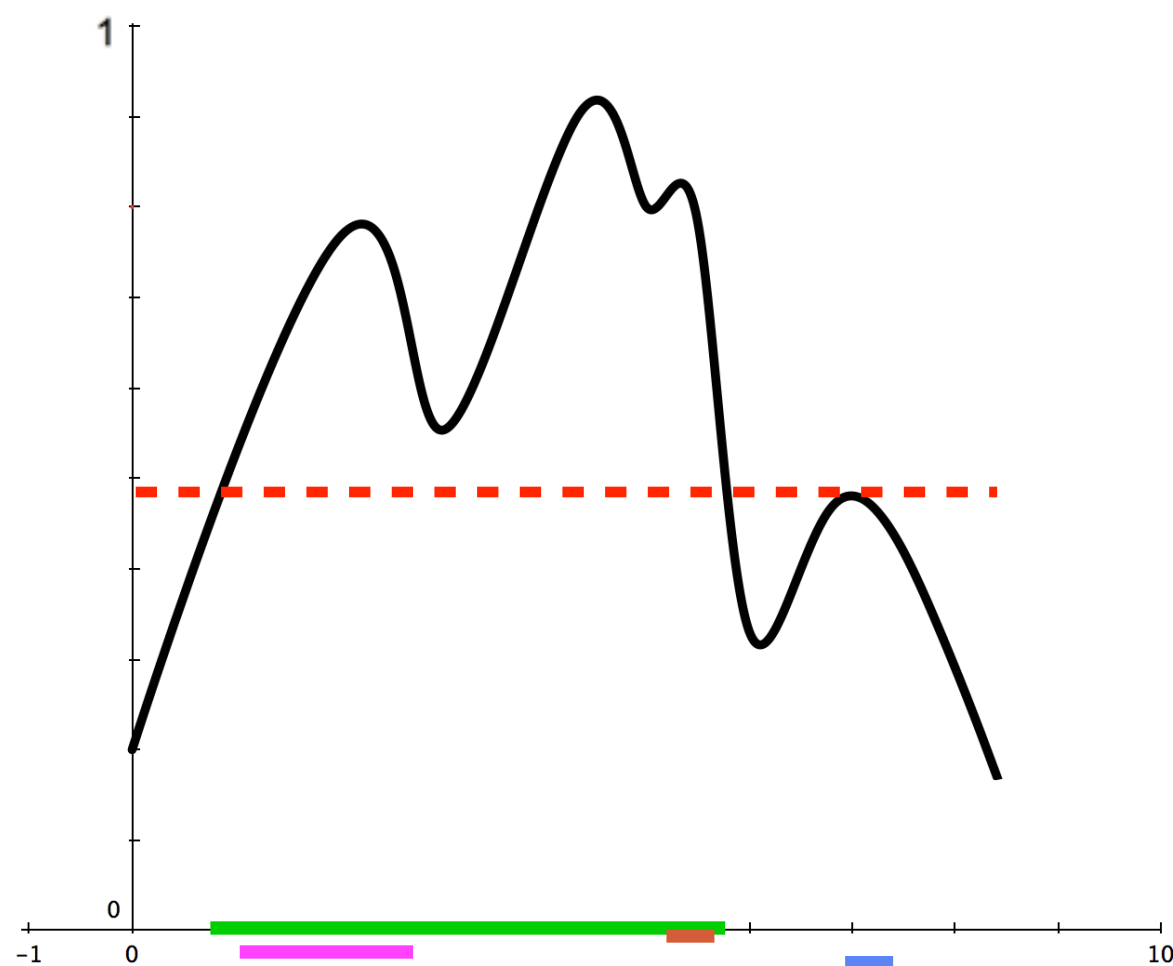
Persistent Homology

- Topological persistence



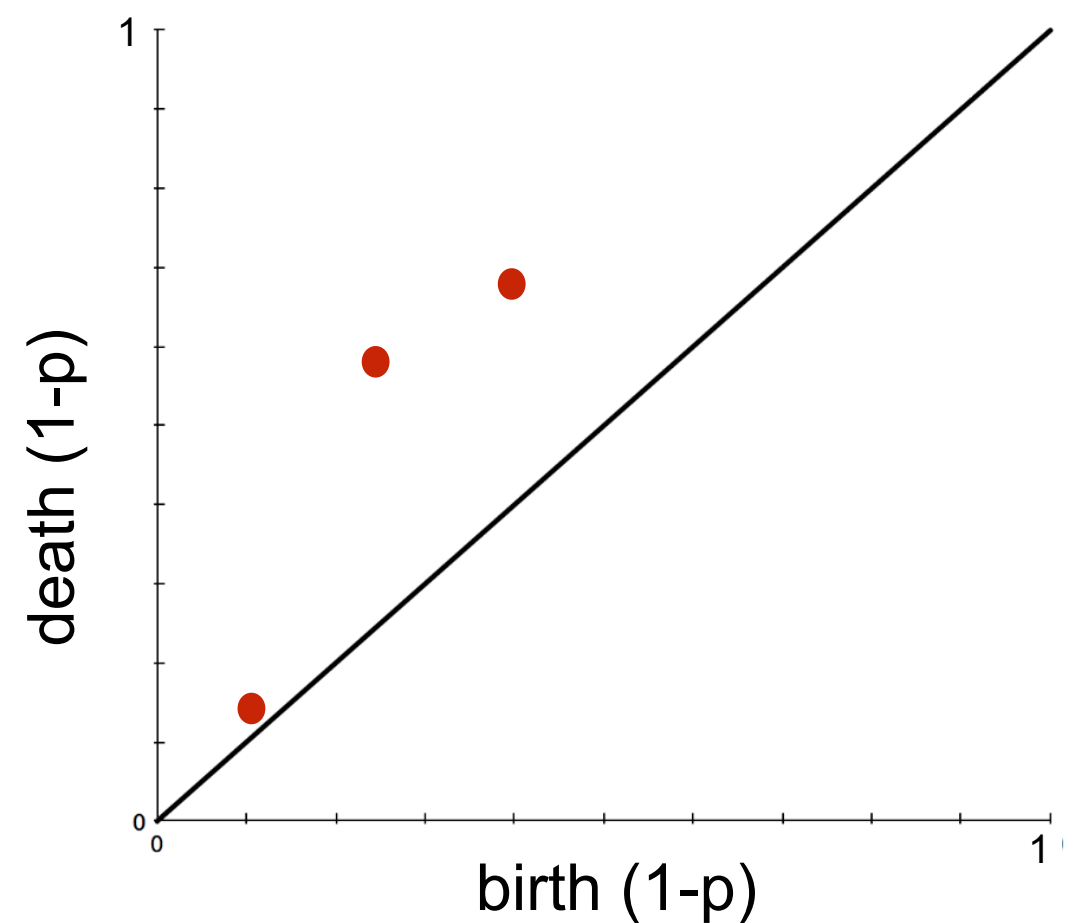
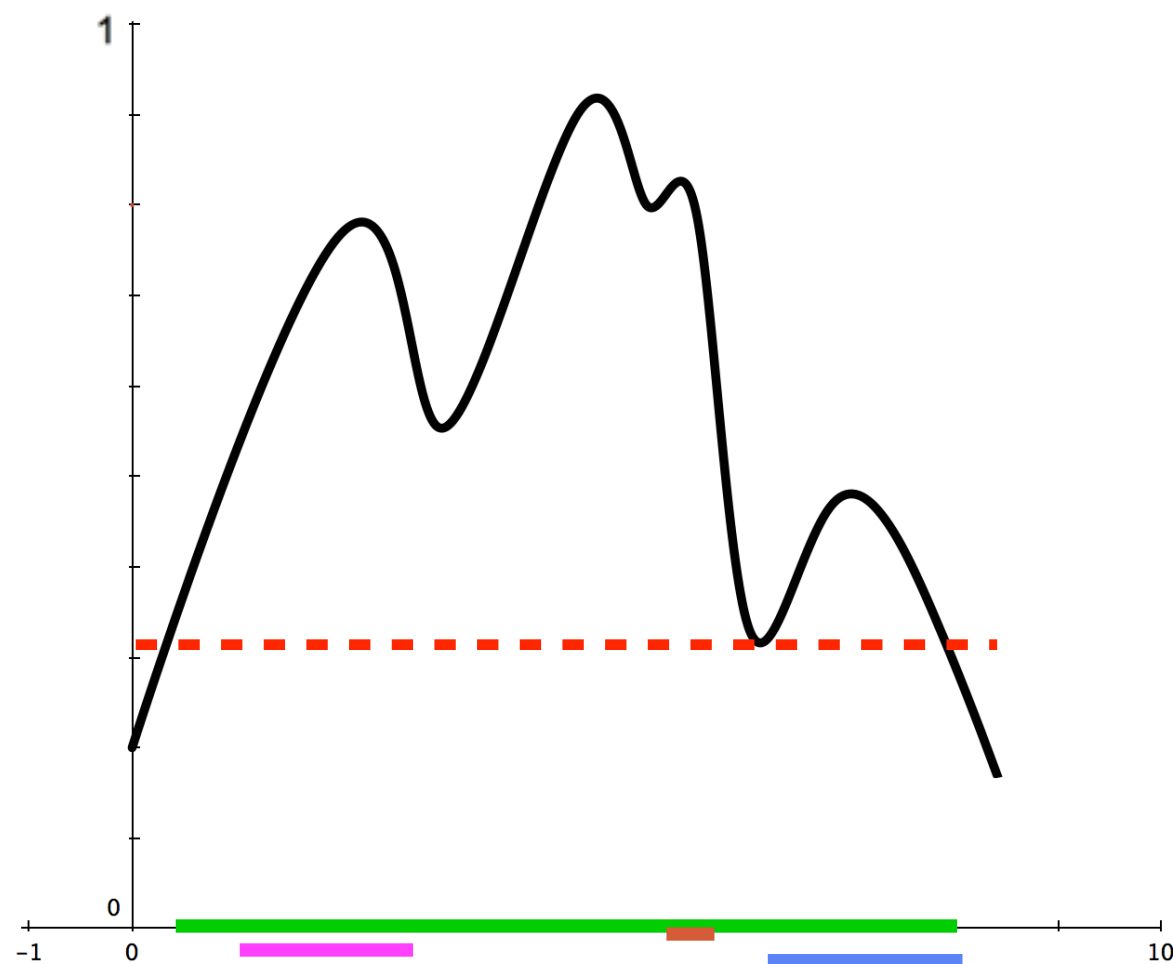
Persistent Homology

- Topological persistence



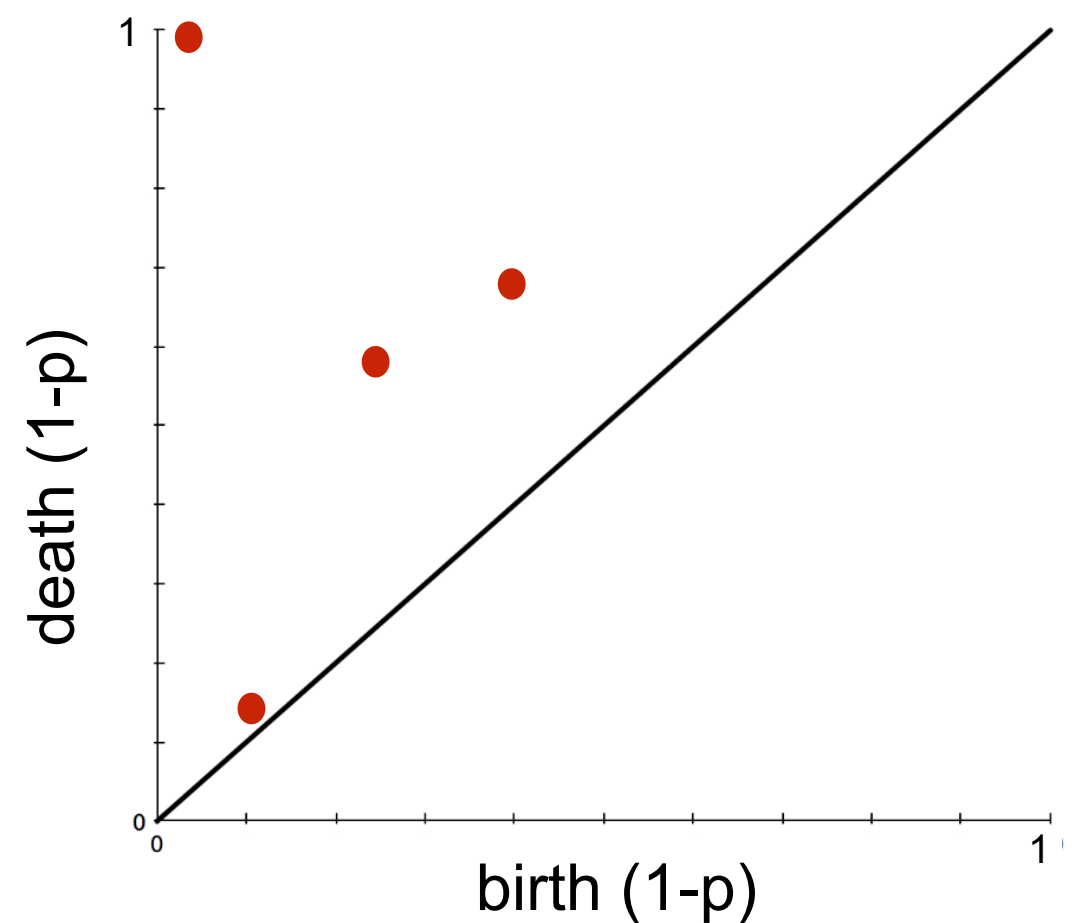
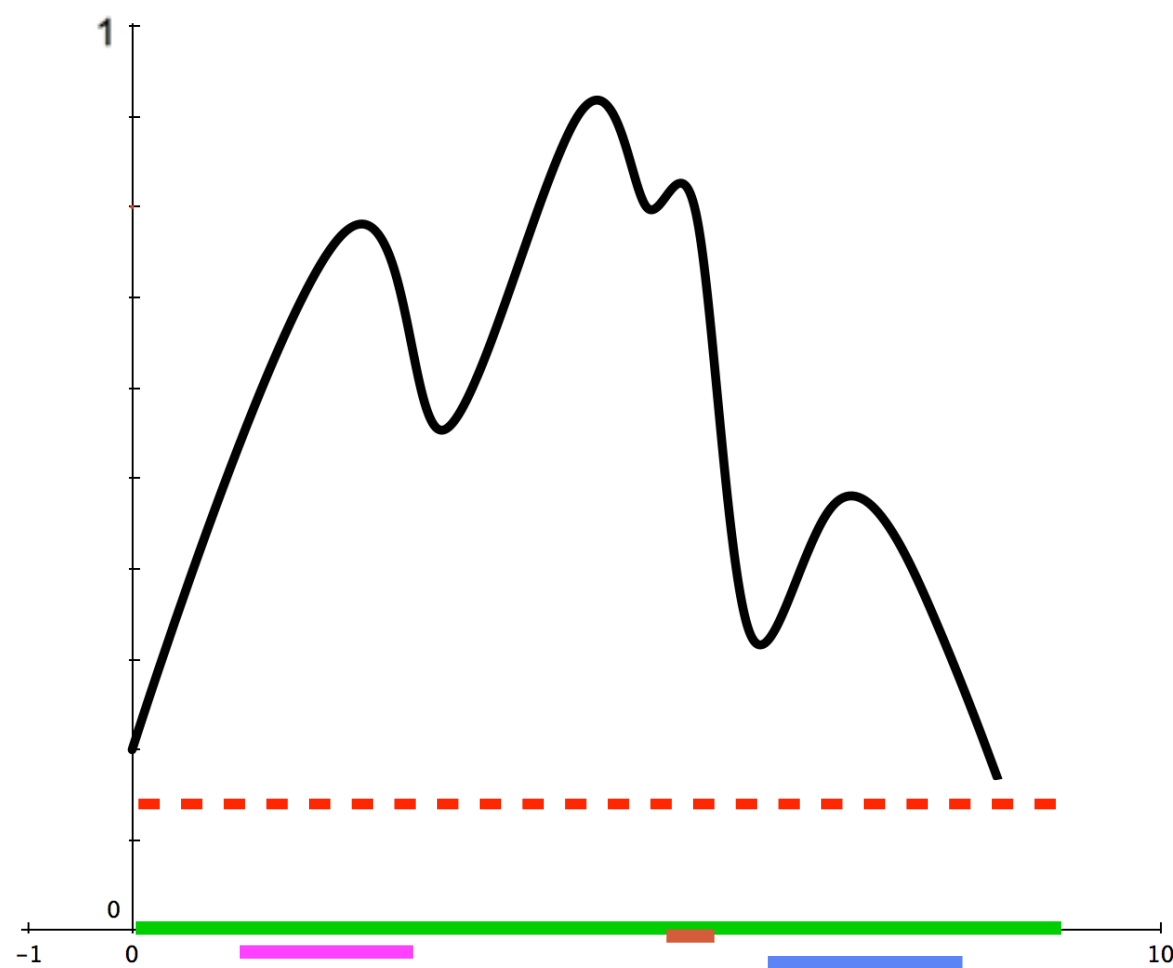
Persistent Homology

- Topological persistence



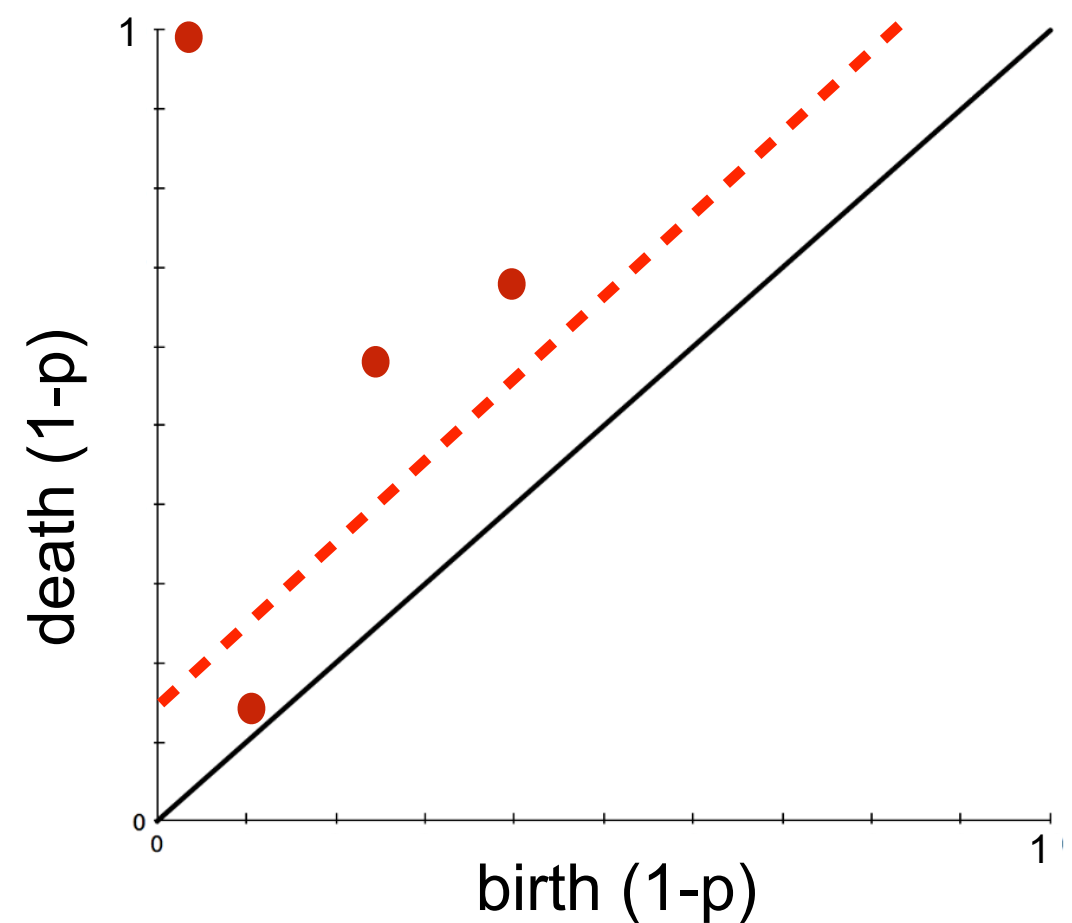
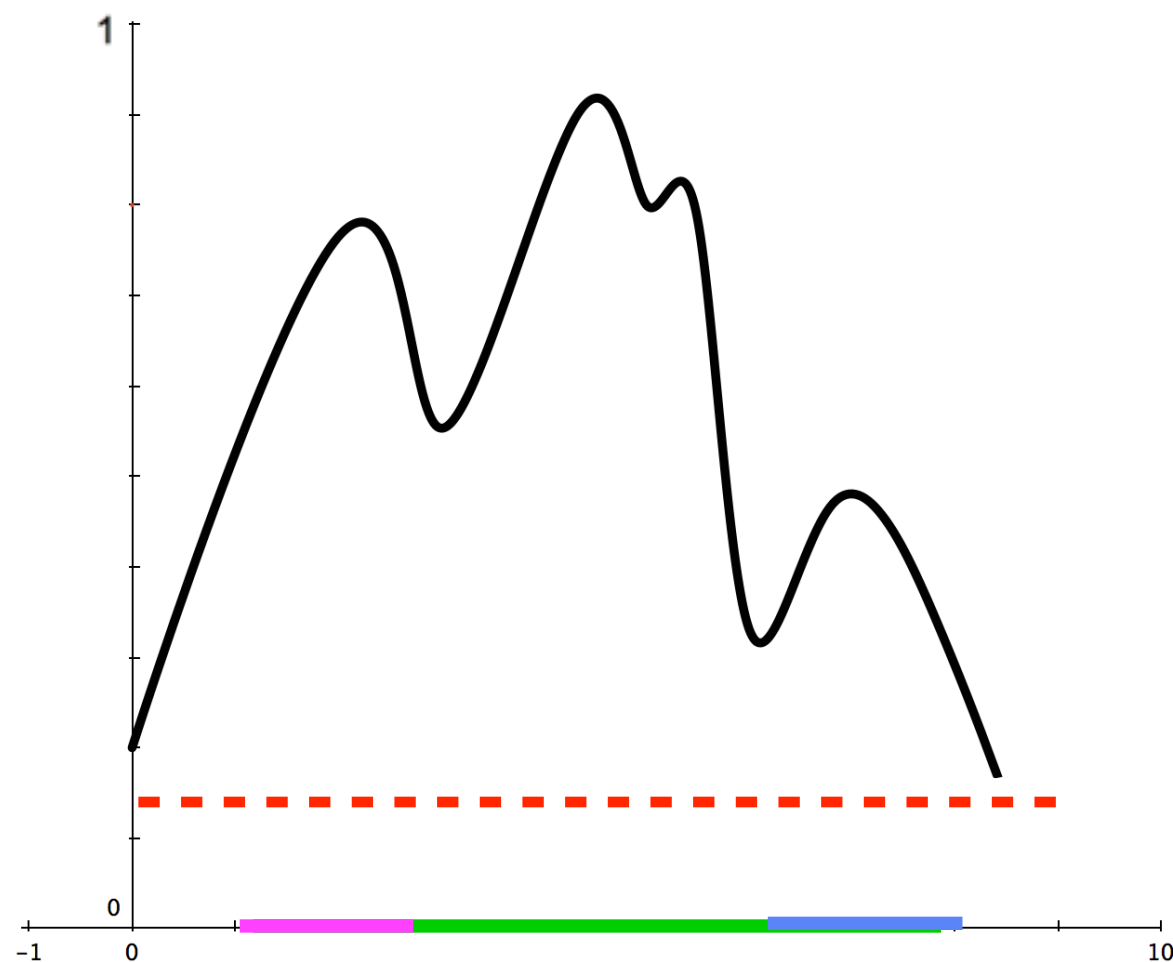
Persistent Homology

- Topological persistence



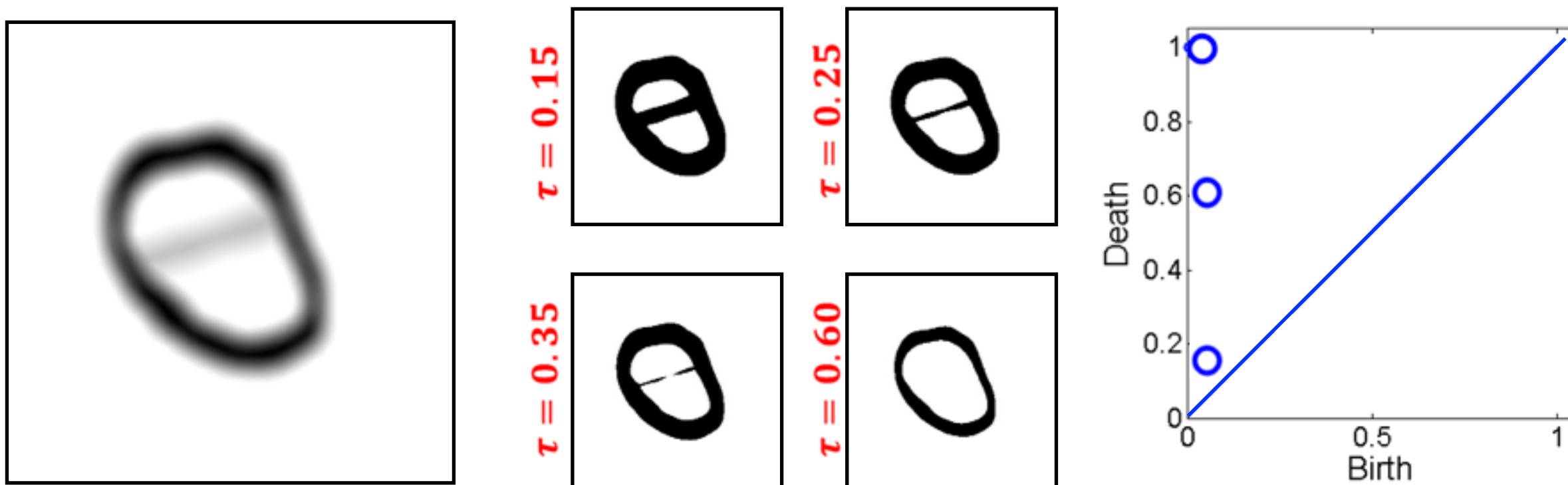
Persistent Homology

- Topological persistence

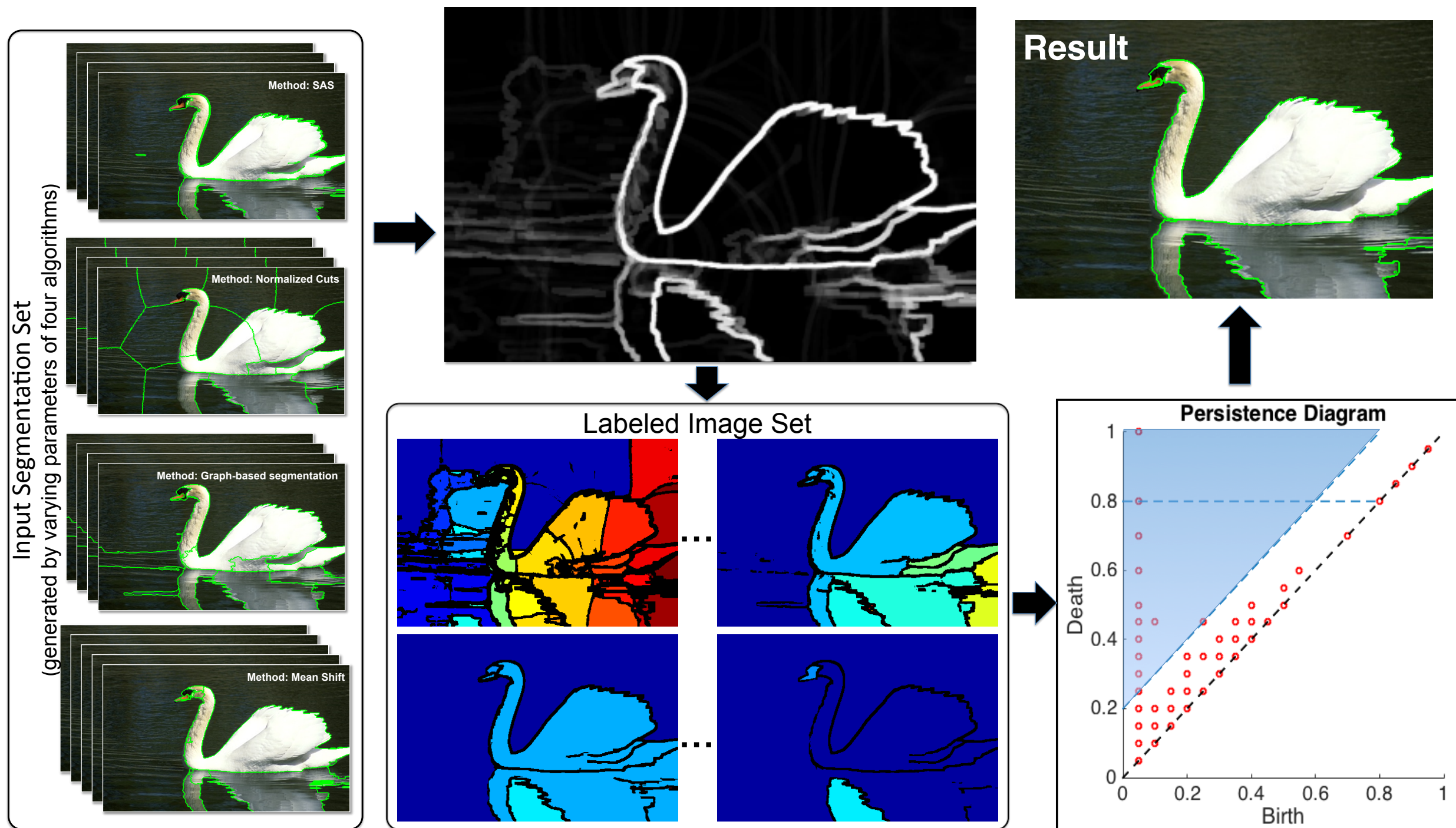


Persistent Homology

- Topological persistence

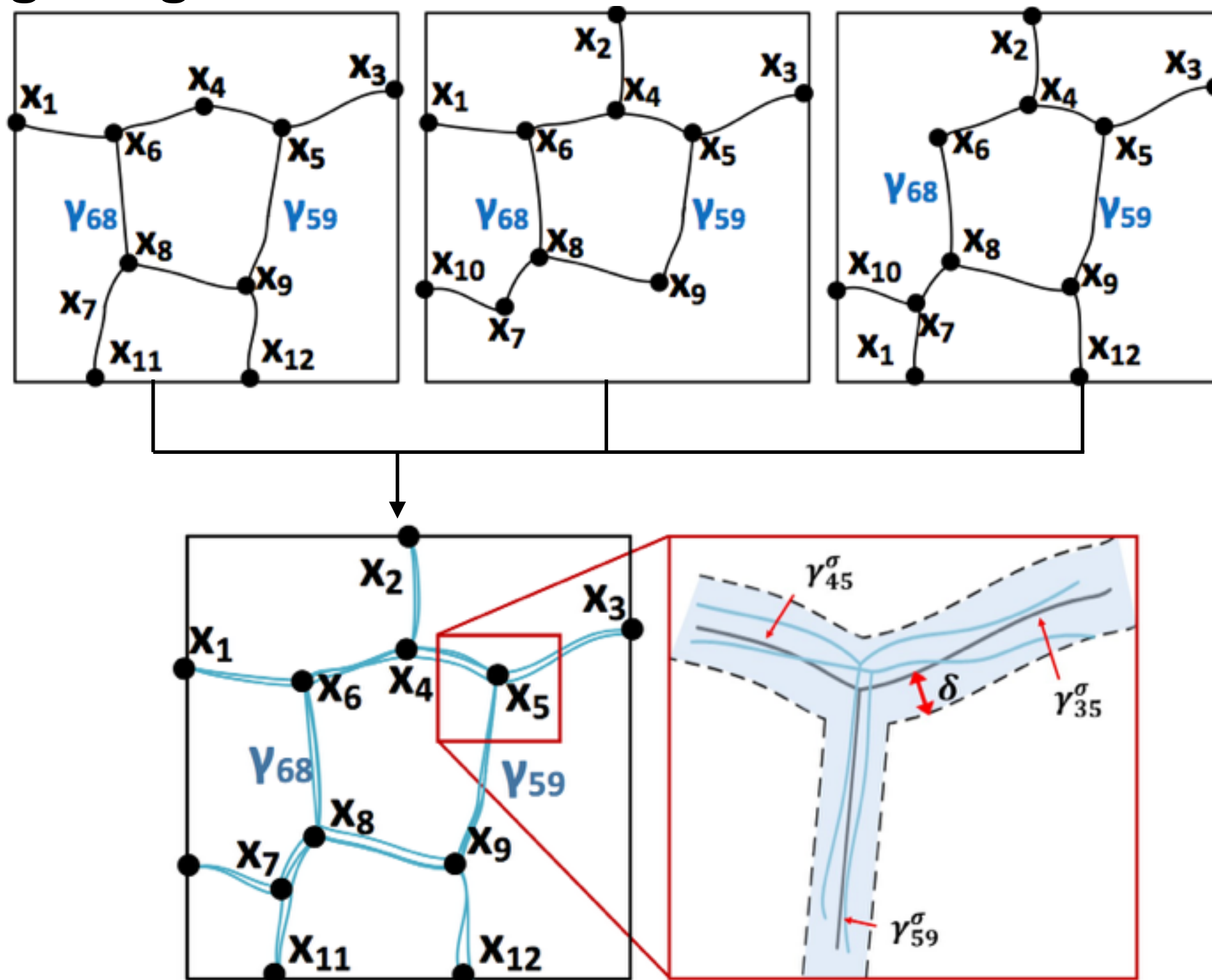


Consensus-based Image Segmentation



Consensus-based Image Segmentation

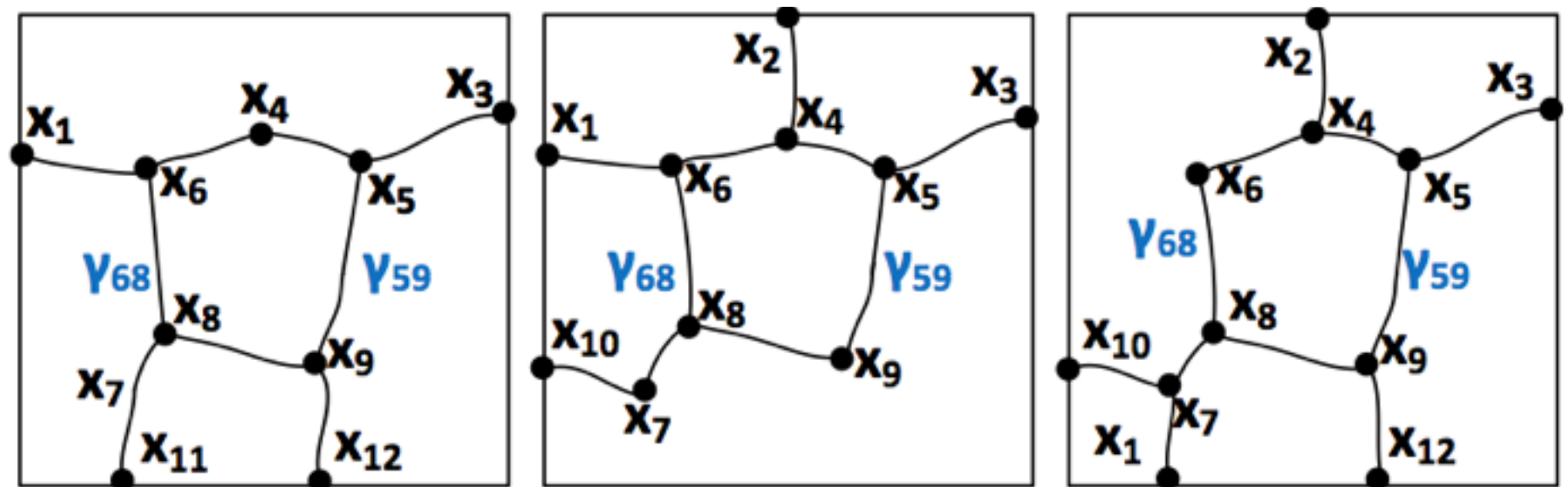
- Image segmentation model



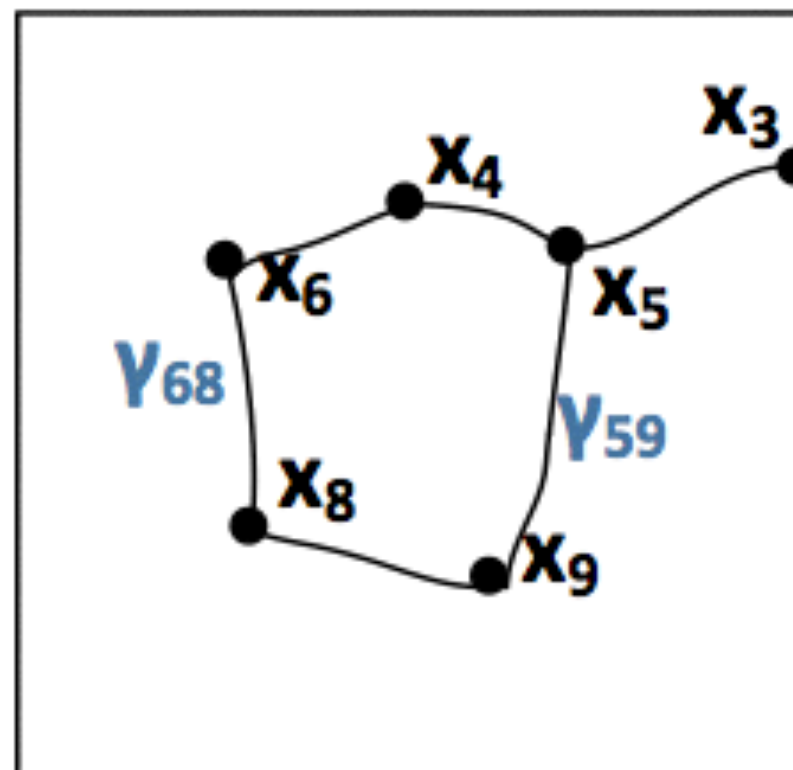
Consensus-based Image Segmentation

- Image segmentation model

Input

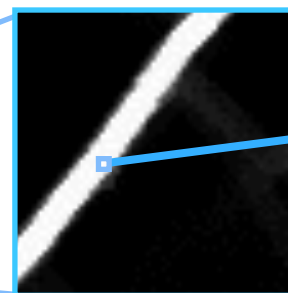


Segmentation
Result



Consensus-based Image Segmentation

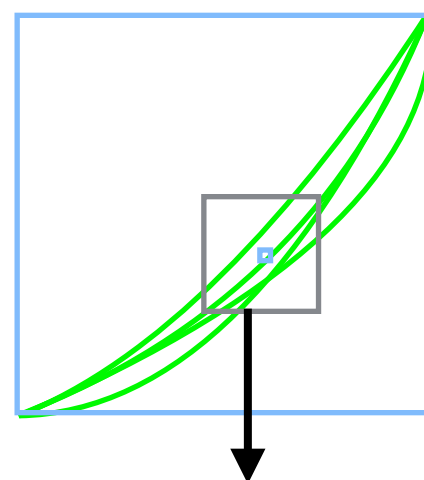
- Probability map construction



Probability of edge
at this pixel



Overlay



$$D^*(X) = \frac{\# \text{ edge}}{\# \text{ segmentations}}$$

A small patch around pixel X

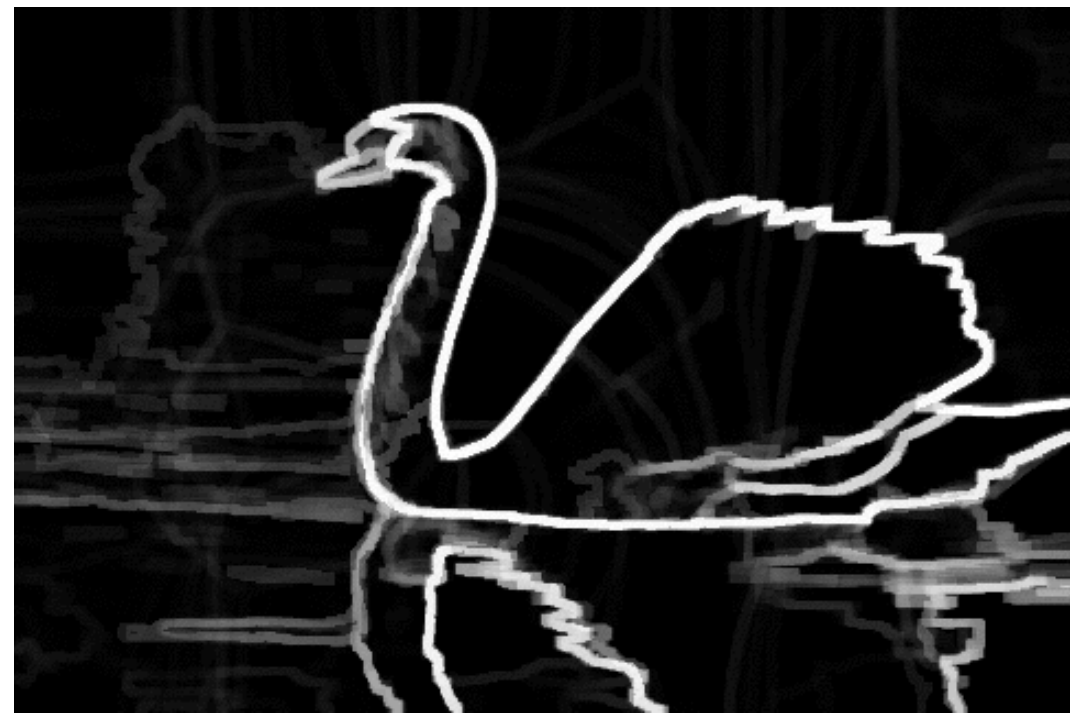
Consensus-based Image Segmentation

- Probability map construction



Connection probability map

$$1 - D_n^*(x)$$

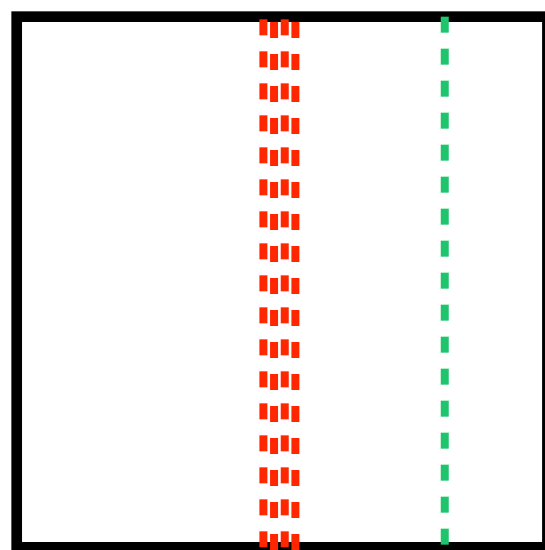
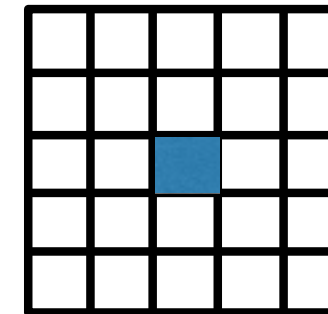
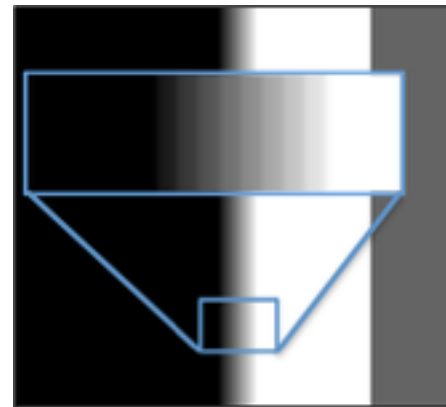


Edge probability map

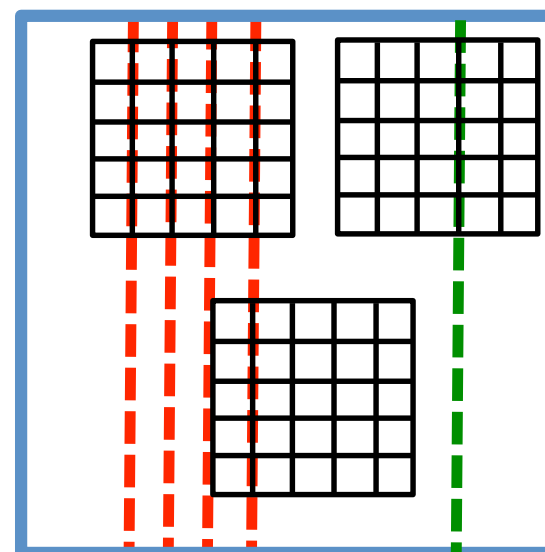
$$D_n^*(x)$$

Consensus-based Image Segmentation

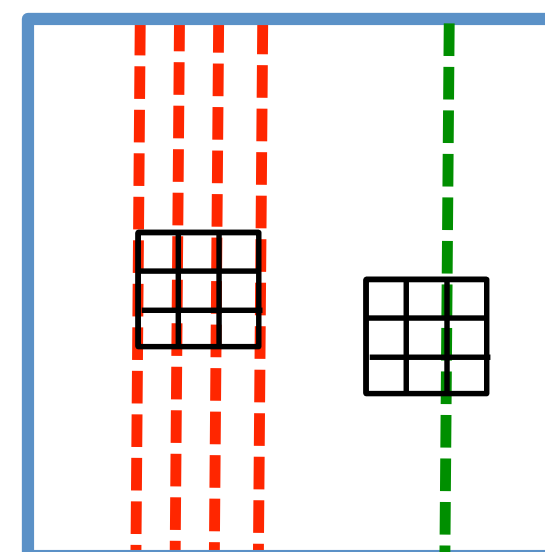
- Effect of patch size n



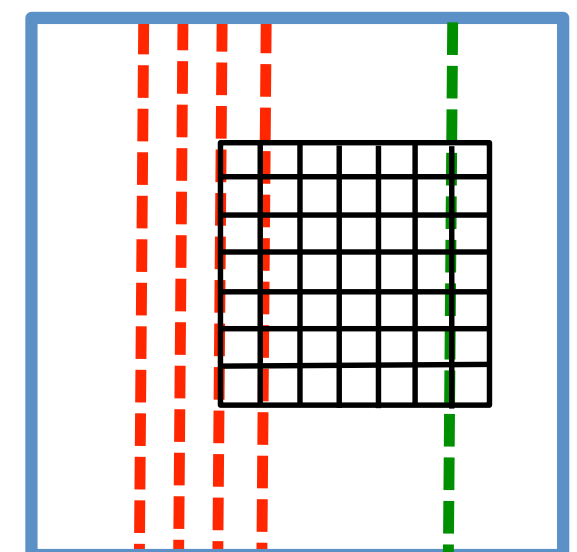
True Probability



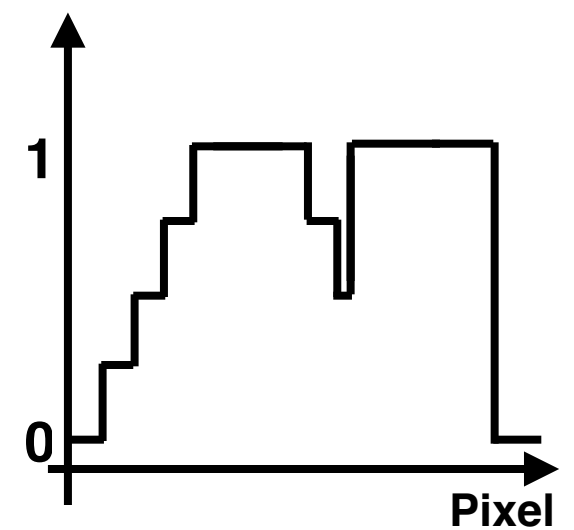
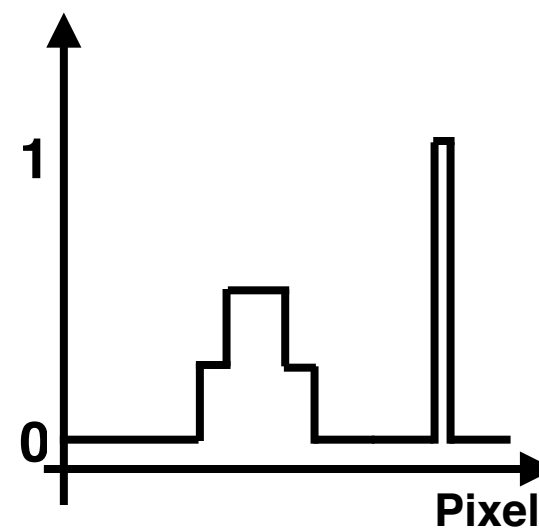
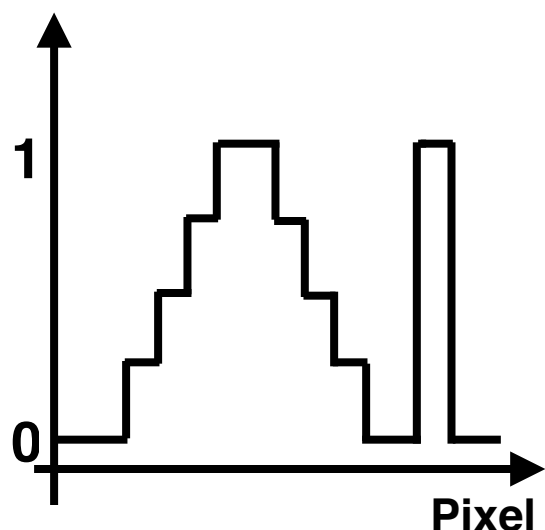
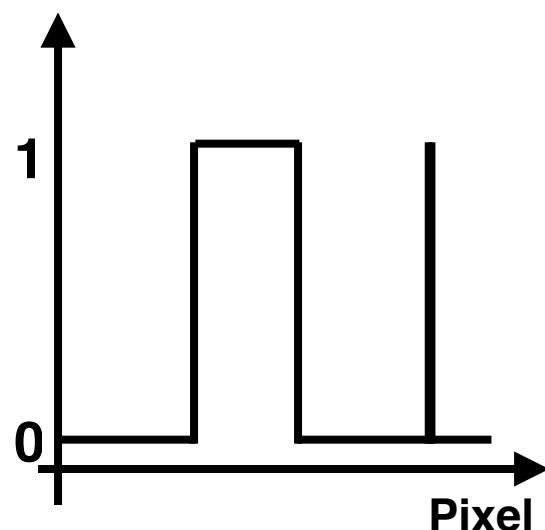
Proper Patch



Small Patch

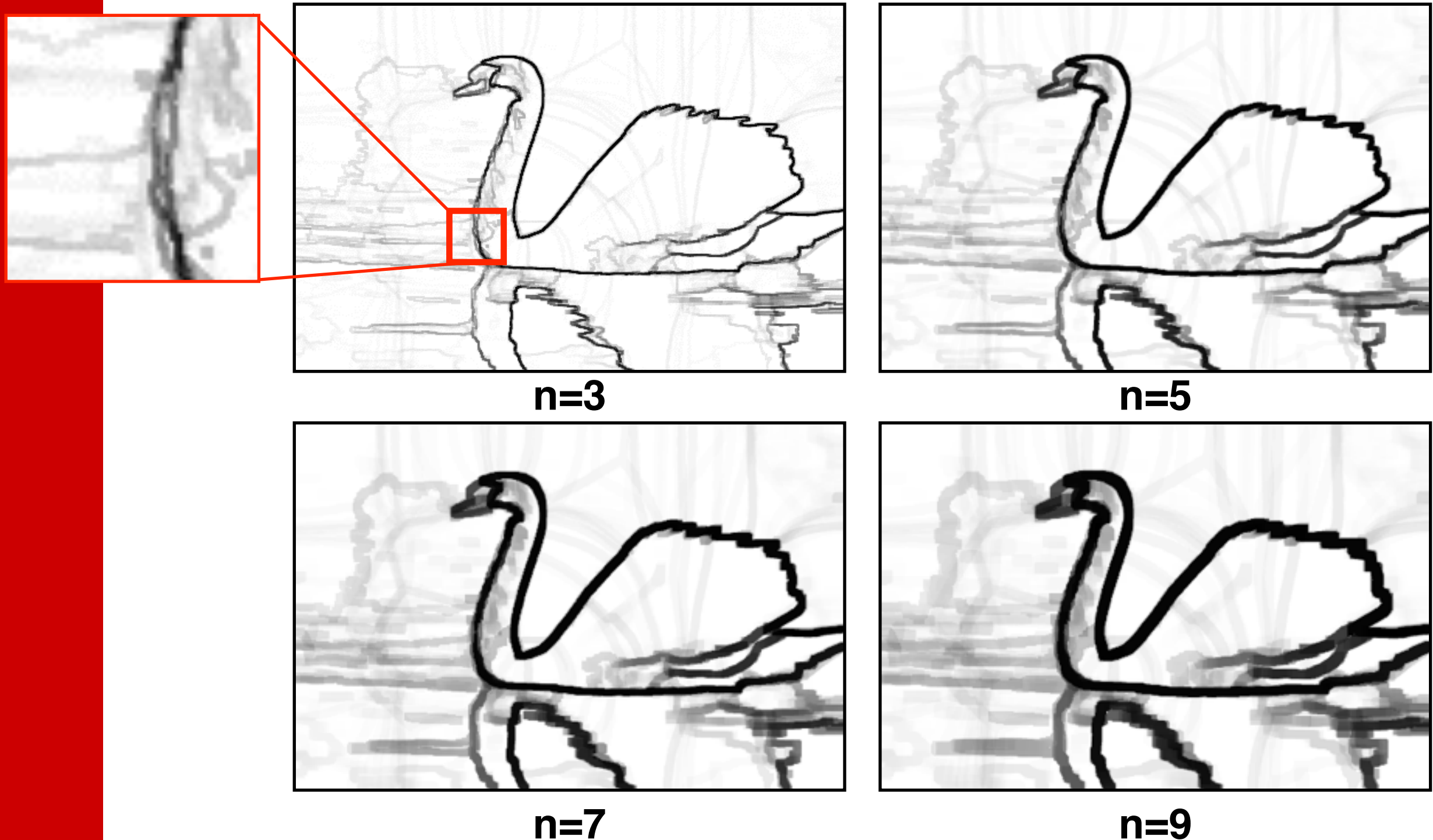


Large Patch



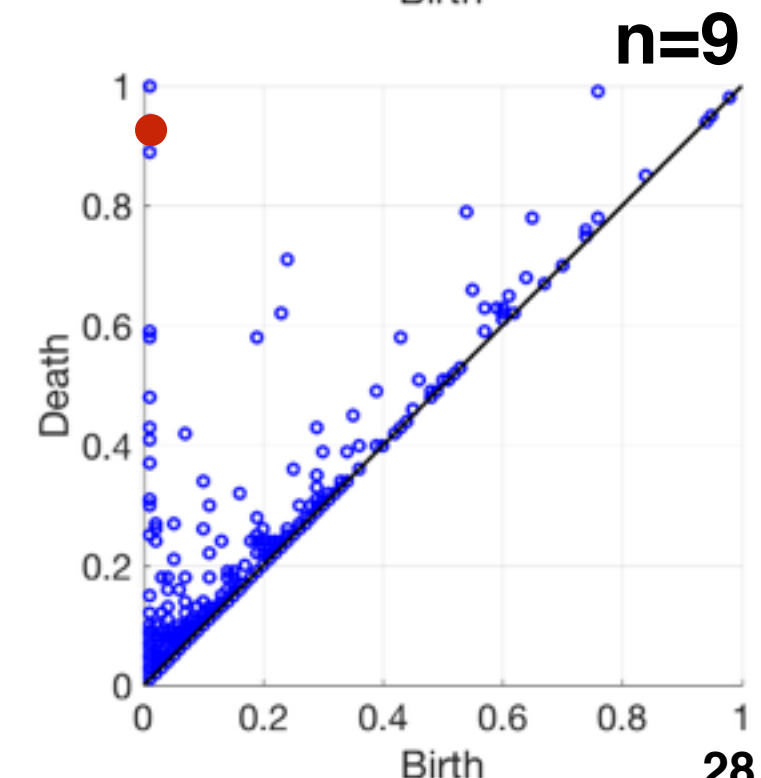
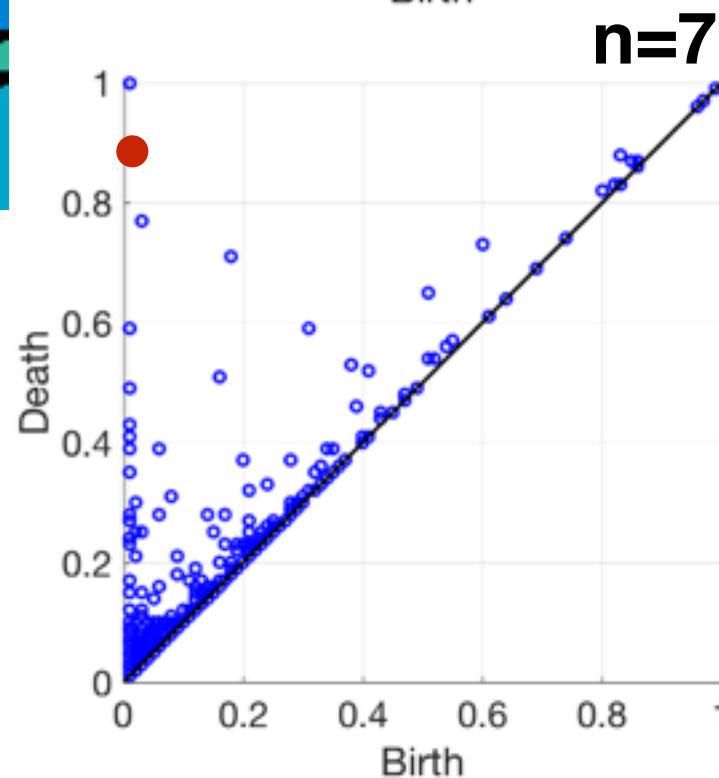
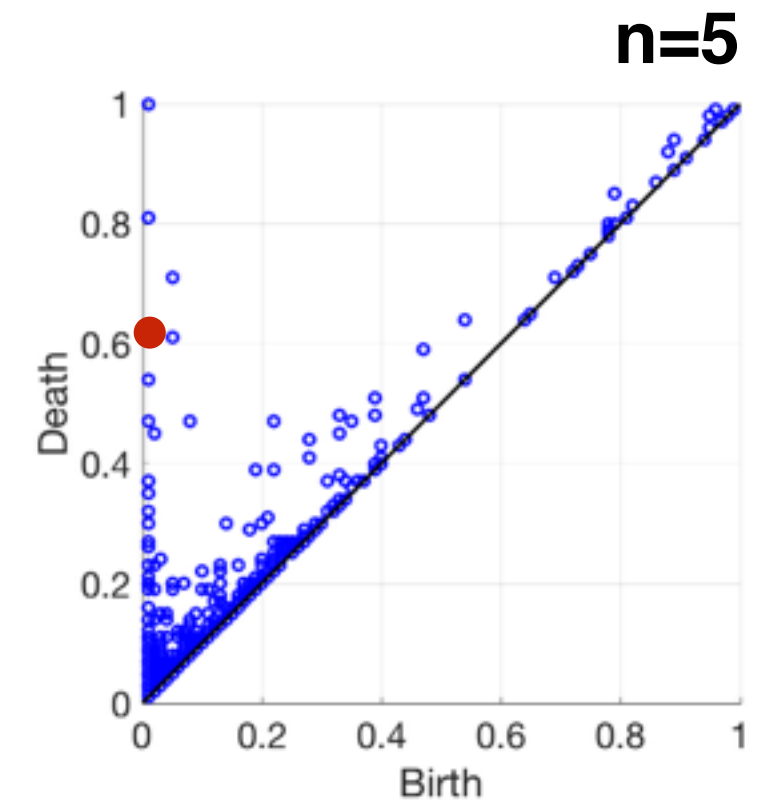
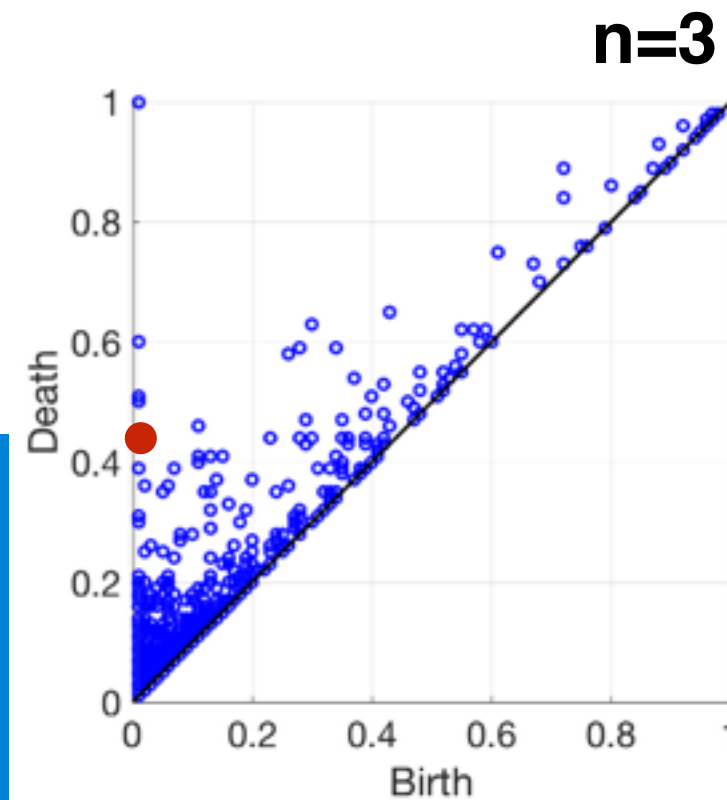
Consensus-based Image Segmentation

- Effect of patch size n



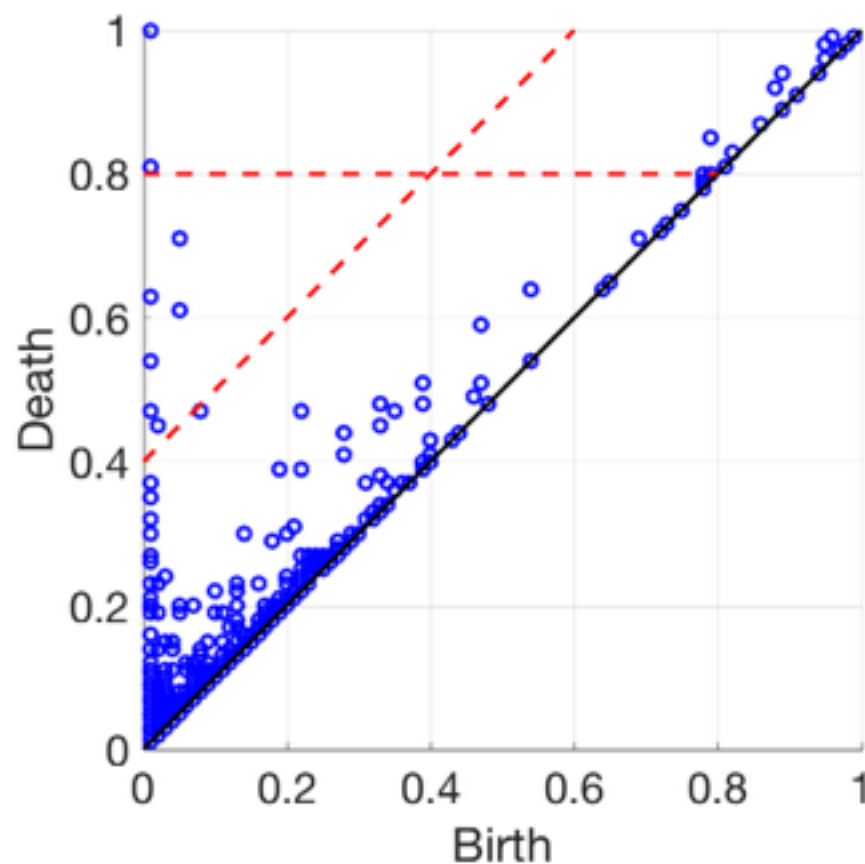
Consensus-based Image Segmentation

- Persistence diagram



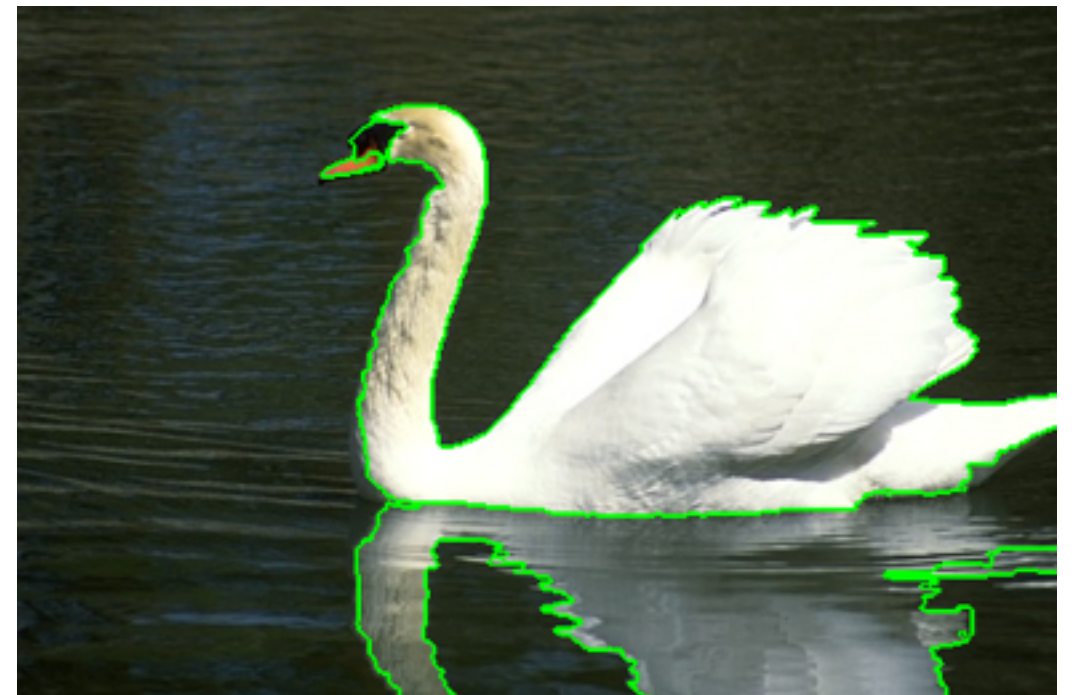
Consensus-based Image Segmentation

- **Thresholding persistence diagram**
 - Persistence threshold - extract persistent region and remove noise.
 - Probability threshold - make sure capture edges being present in high probability.



Consensus-based Image Segmentation

- Segmentation obtained by color-based region growing

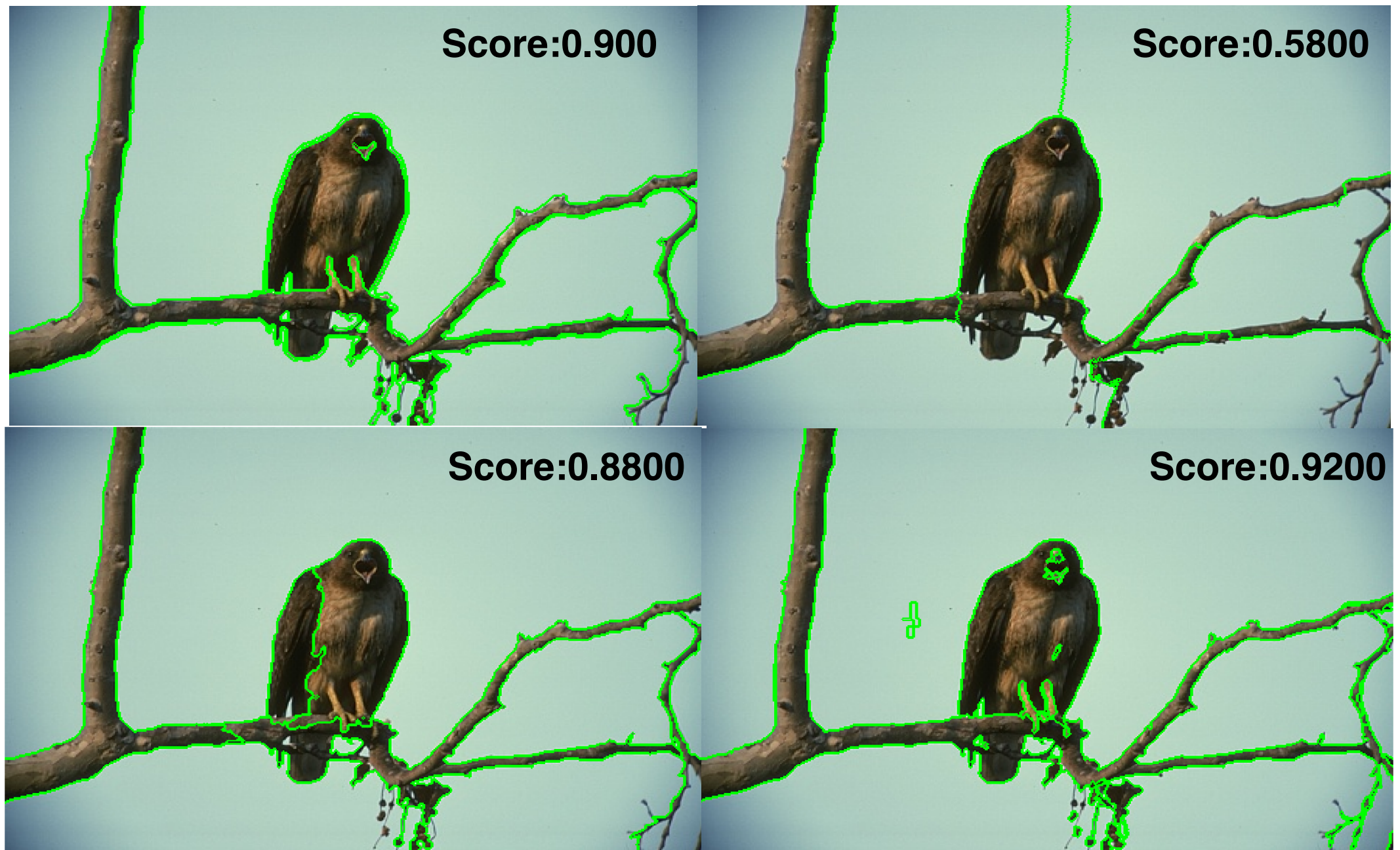


Consensus-based Image Segmentation

- **Experiment - Input set generation**
 - **Dataset - Berkeley Segmentation Database**
 - **Four input algorithms: SAS, Normalized Cuts, Graph-based and Mean Shift**
 - **SAS: number of region varying from 5 to 30**
 - **Normalized Cuts: number of region varying from 5 to 30**
 - **Graph-based: σ varying from 0.4 to 0.8, k varying from 500 to 5000**
 - **Mean Shift: k1 varying from 2 to 15, k2 varying from 7 to 15**
 - **238 input segmentations in total**
 - **Probability are weighted by number of input from each algorithm**

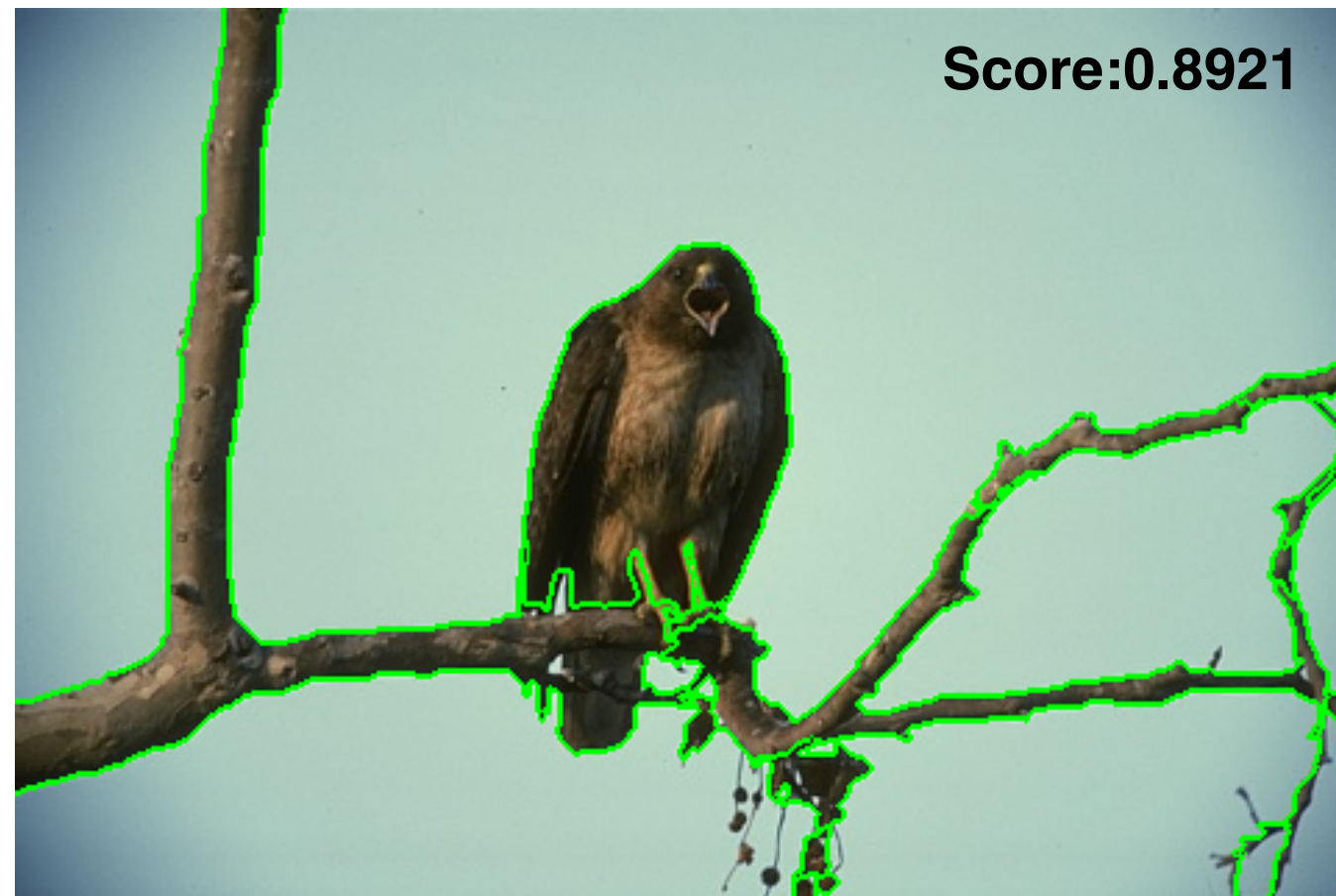
Consensus-based Image Segmentation

- Experiment - Result



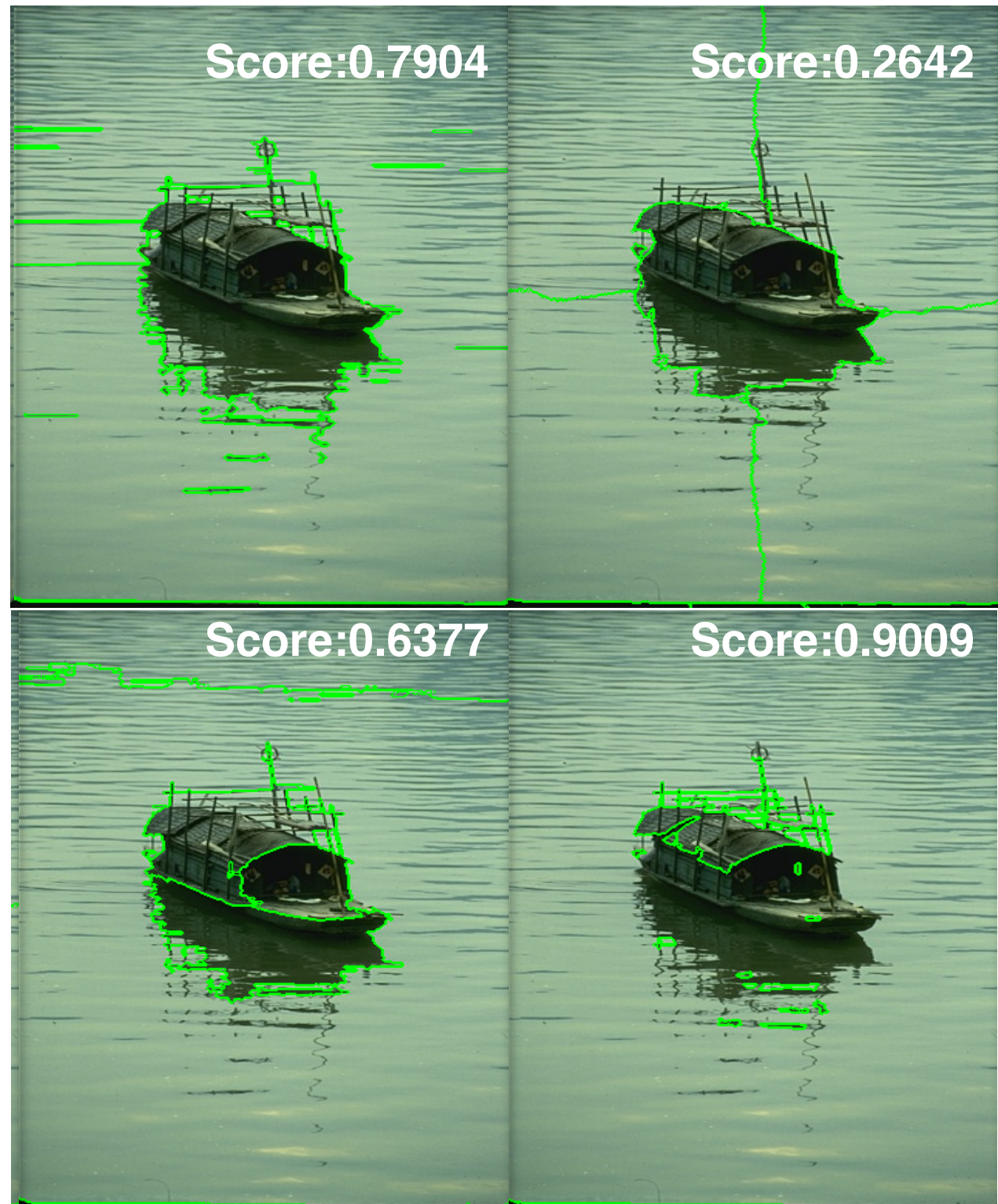
Consensus-based Image Segmentation

- Experiment - Result



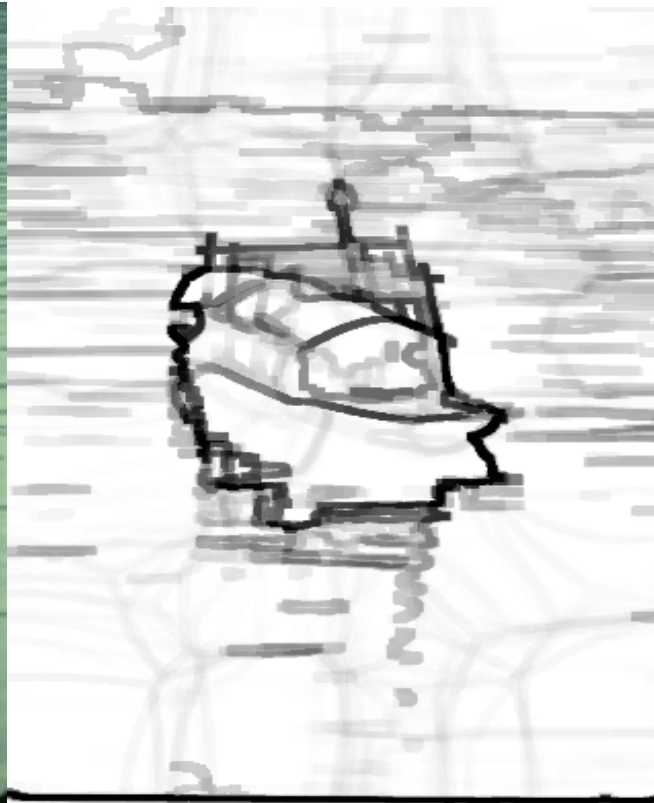
Consensus-based Image Segmentation

- Experiment - Result



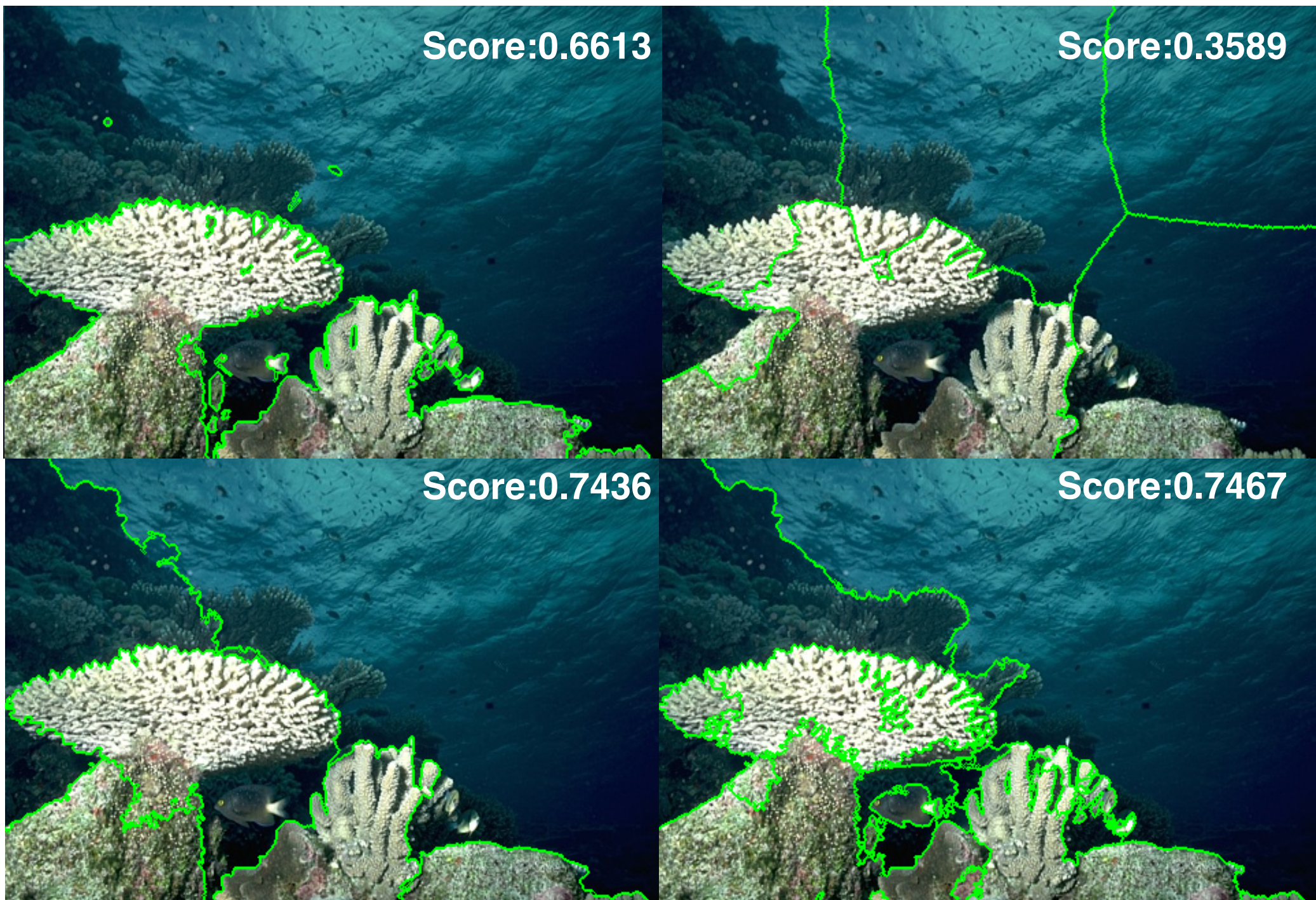
Consensus-based Image Segmentation

- Experiment - Result



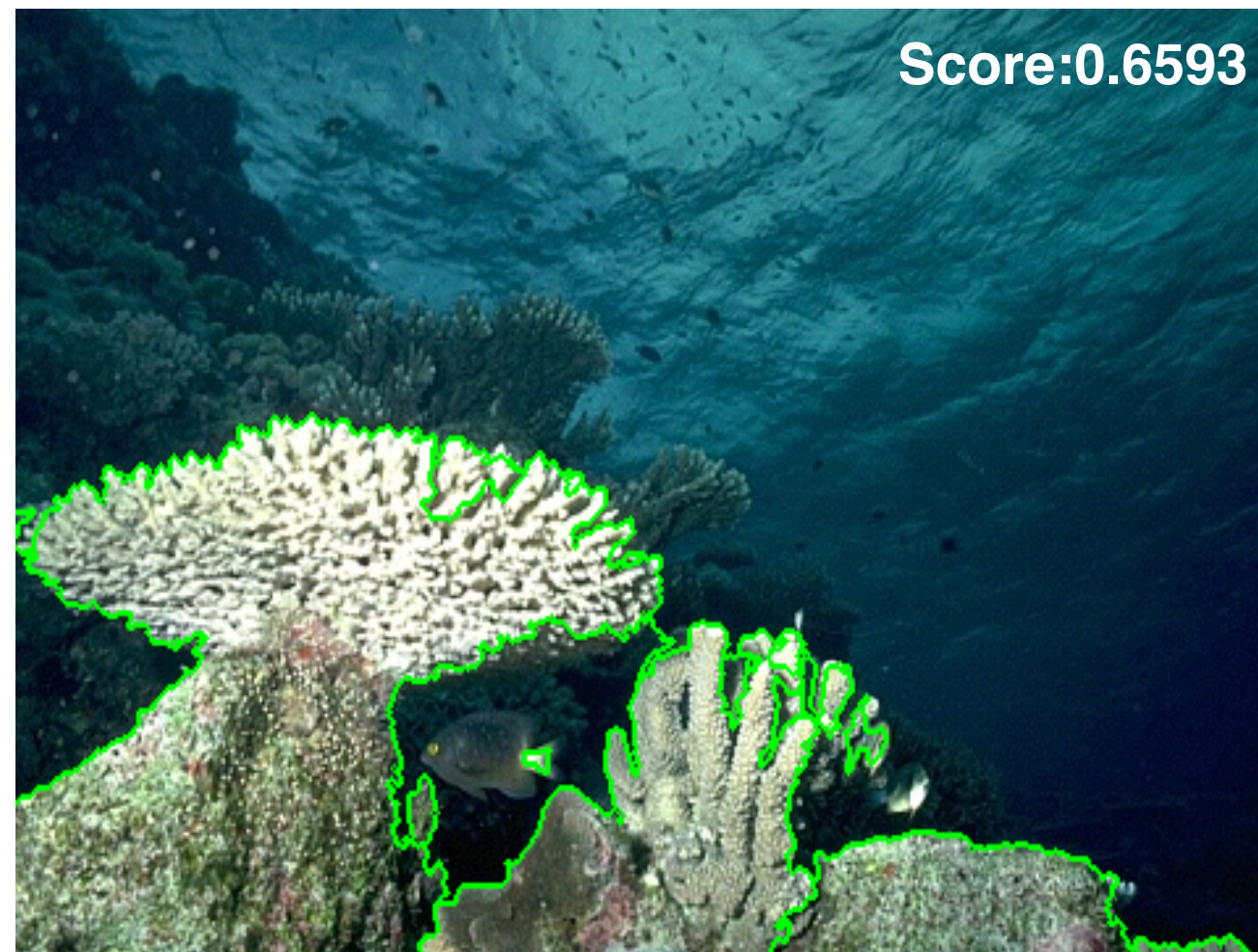
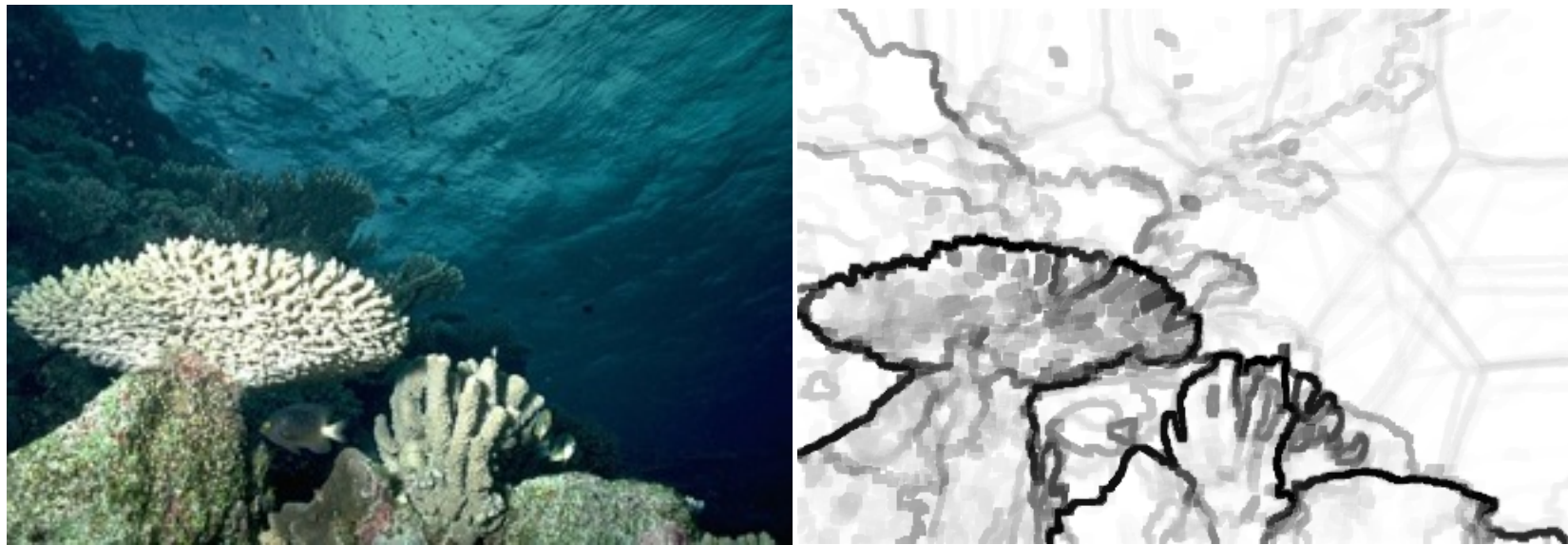
Consensus-based Image Segmentation

- Experiment - Result



Consensus-based Image Segmentation

- Experiment - Result



Consensus-based Image Segmentation

- **Experiment - Result**

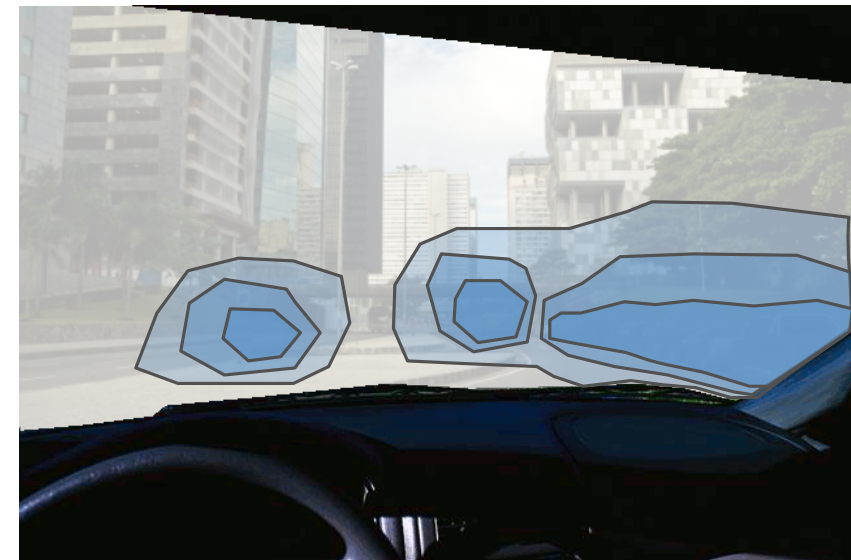
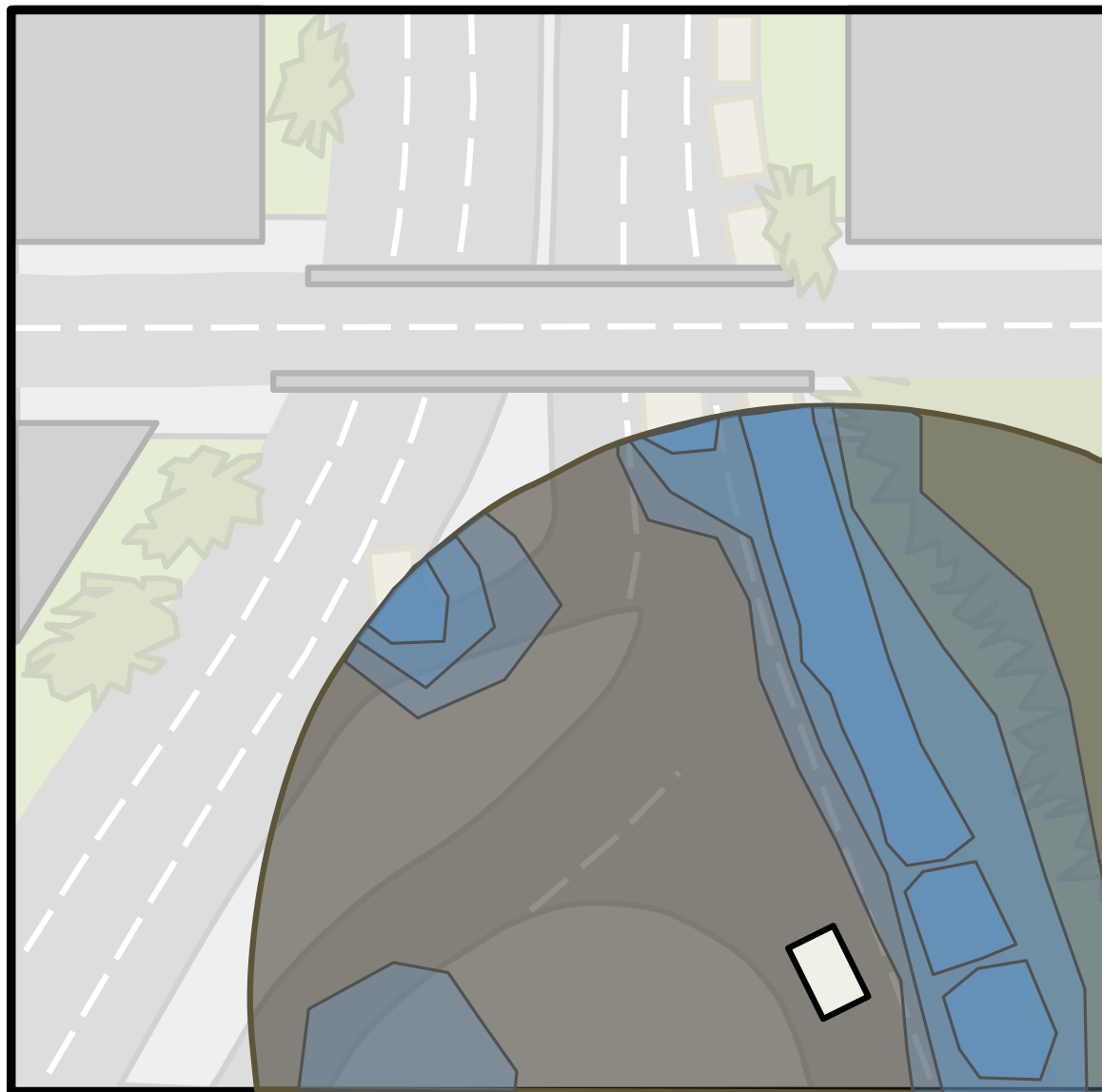
- RSC - Coverage score
- VoI - Variation of information

Methods	Graph	NCuts	SAS	Mean Shift
RSC	0.5359	0.3970	0.5325	0.5540
VoI	2.1128	2.3515	1.8251	1.8946

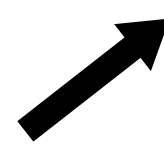
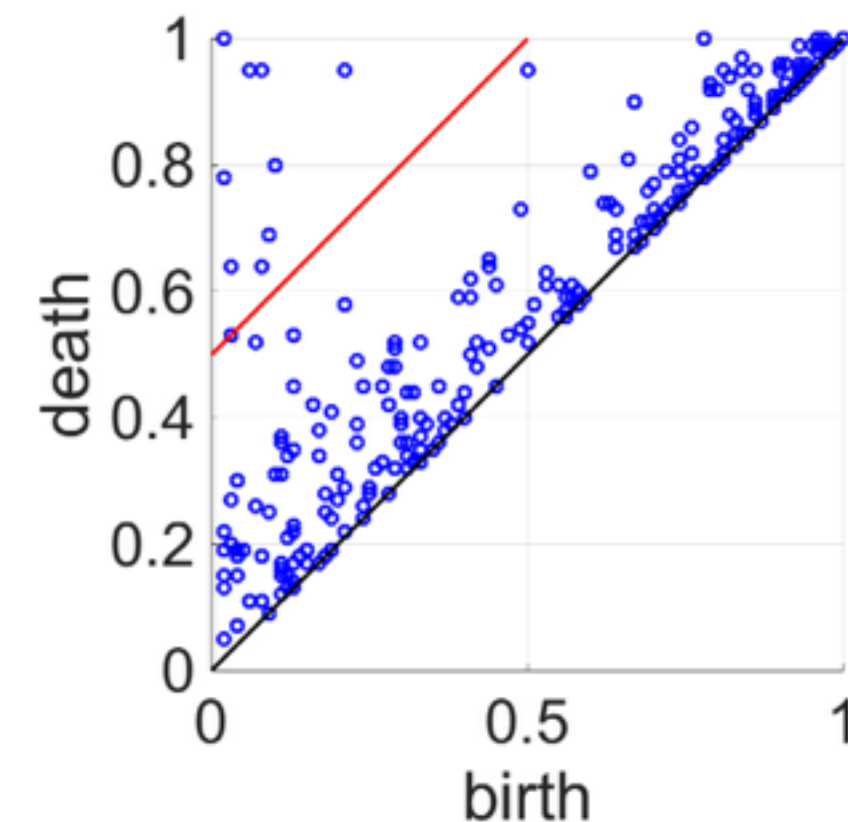
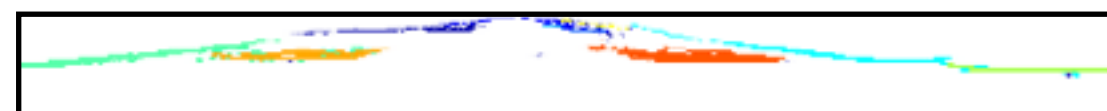
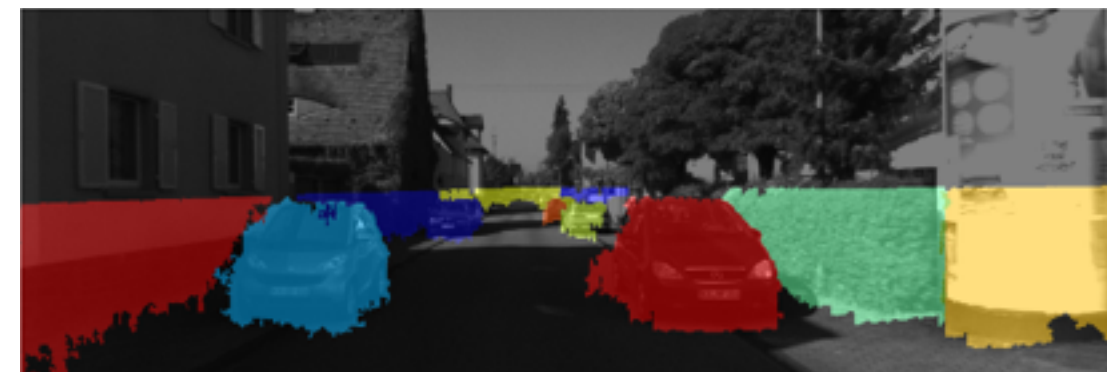
Methods	Consensus-base			
	$\tau = 0.30$	$\tau = 0.35$	$\tau = 0.40$	$\tau = 0.45$
RSC	0.5982	0.6085	0.5725	0.5731
VoI	1.7070	1.6700	1.7600	1.7930

Obstacle Segmentation of Outdoor Scene

- Vision system for autonomous driving

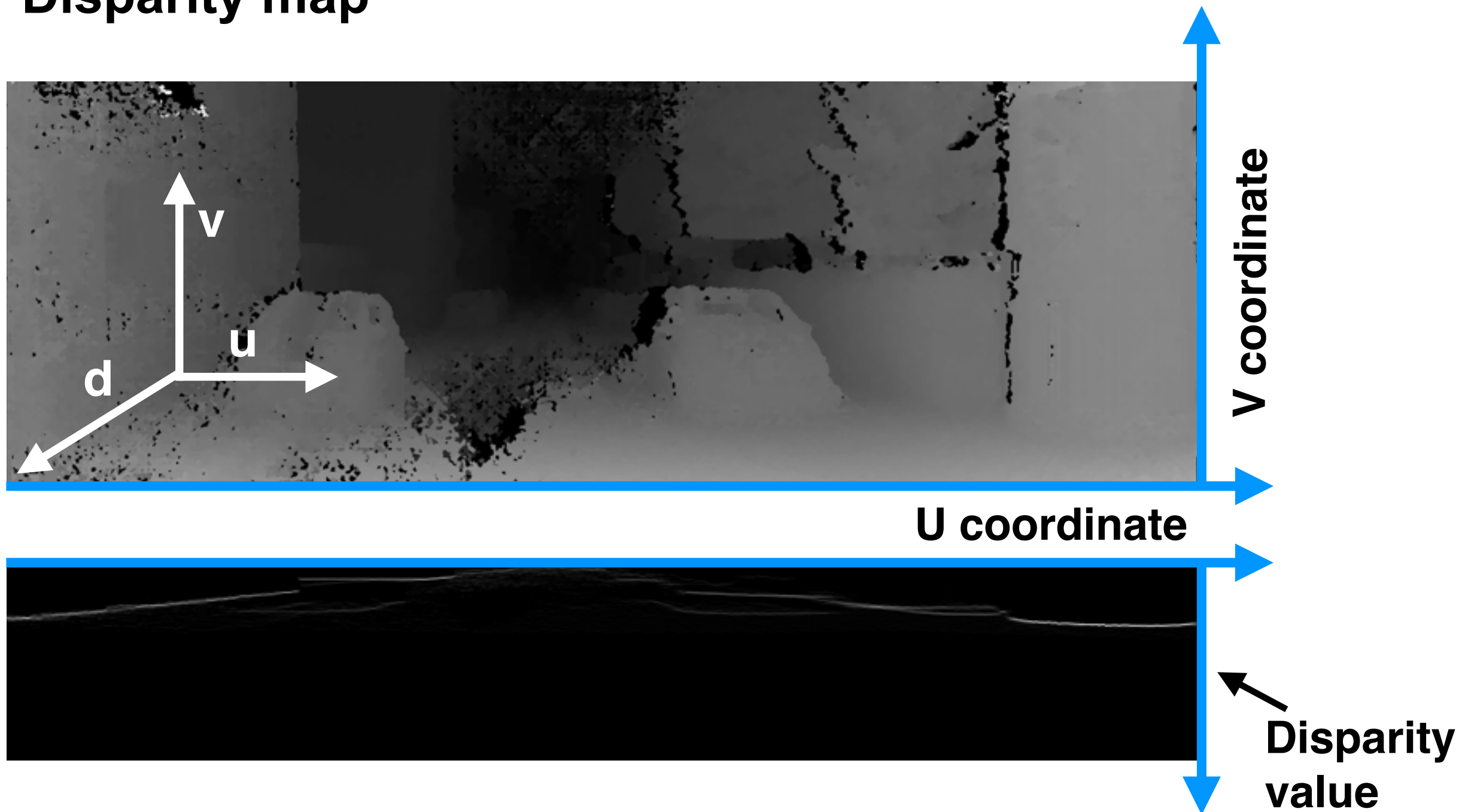


Obstacle Segmentation of Outdoor Scene



Obstacle Segmentation of Outdoor Scene

- Disparity map



Obstacle Segmentation of Outdoor Scene

- Ground Segmentation



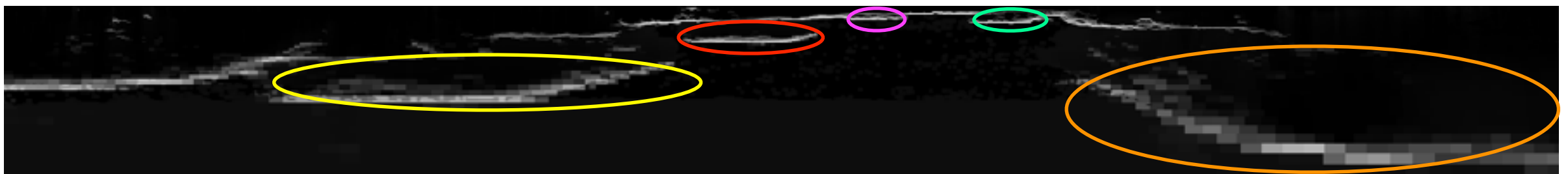
Obstacle Segmentation of Outdoor Scene

- Occupancy computation



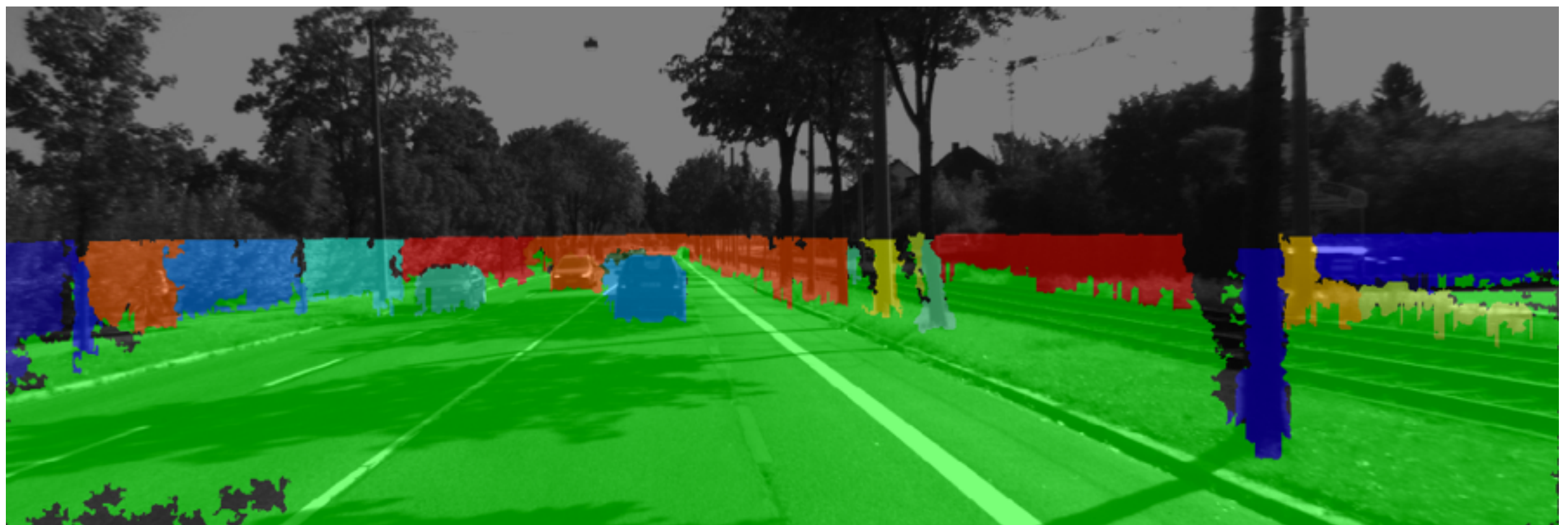
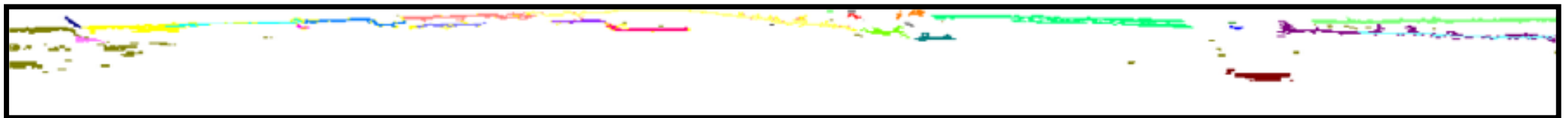
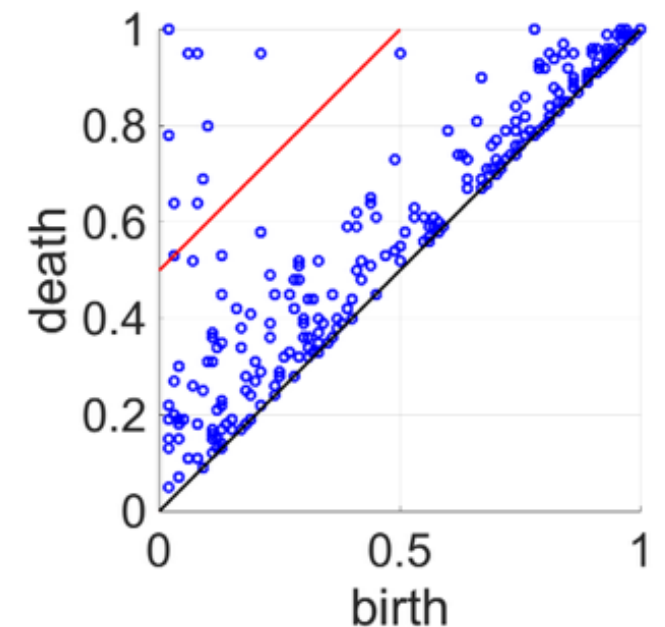
Obstacle Segmentation of Outdoor Scene

- Occupancy computation



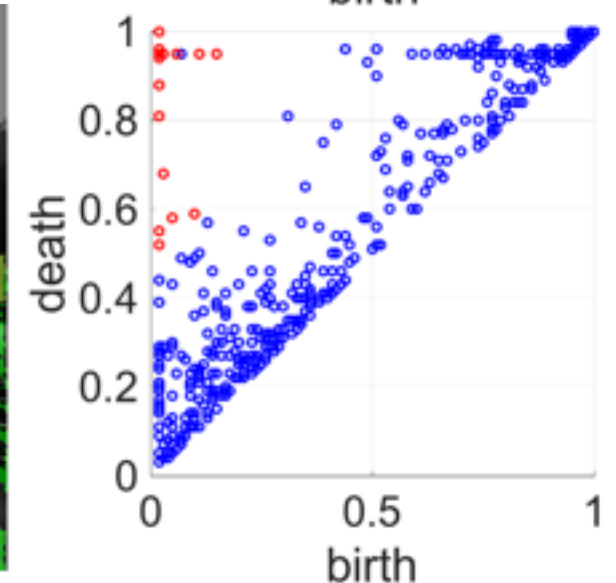
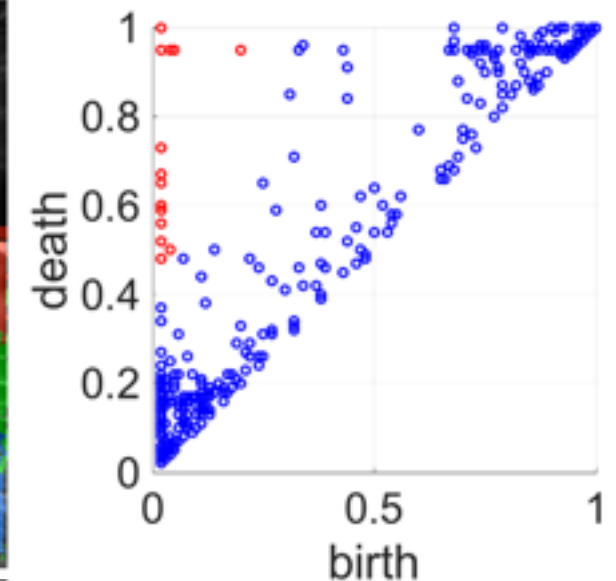
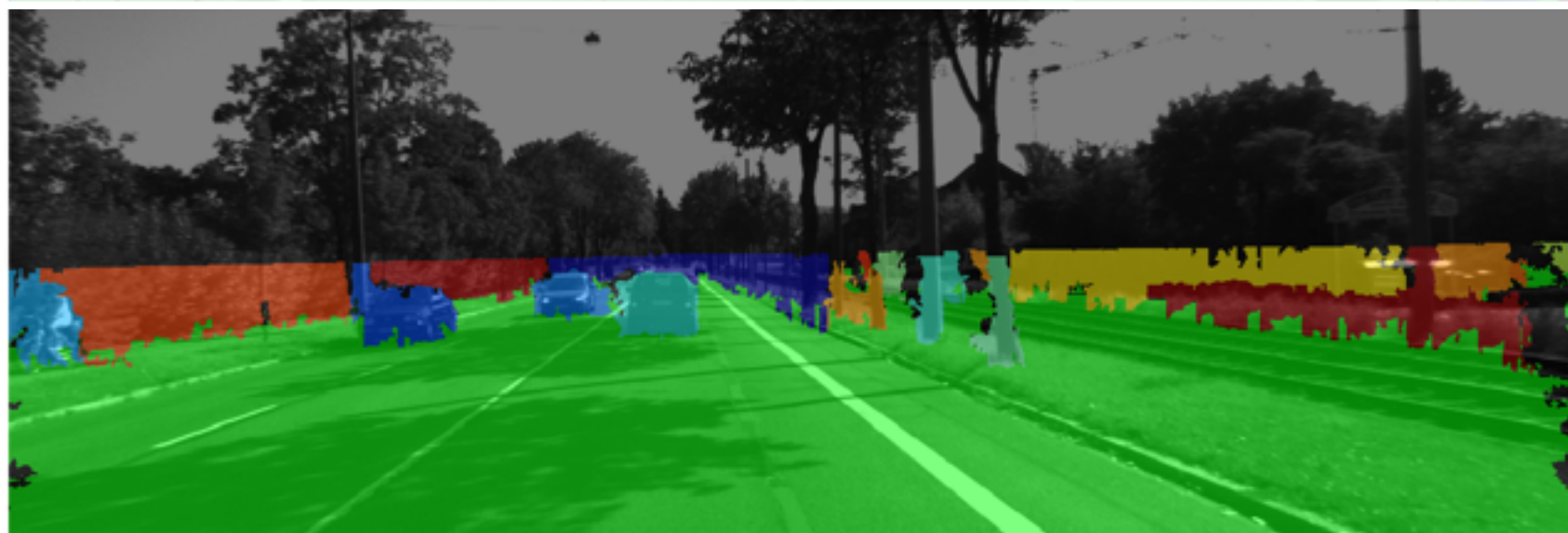
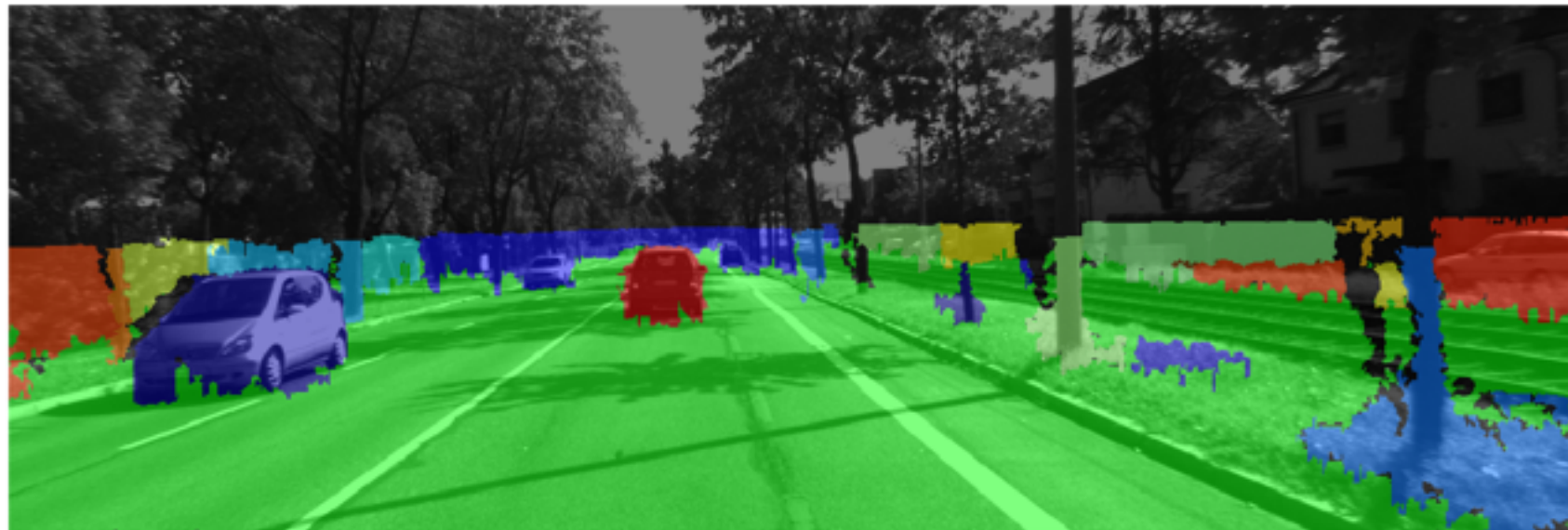
Obstacle Segmentation of Outdoor Scene

- Persistence region extraction



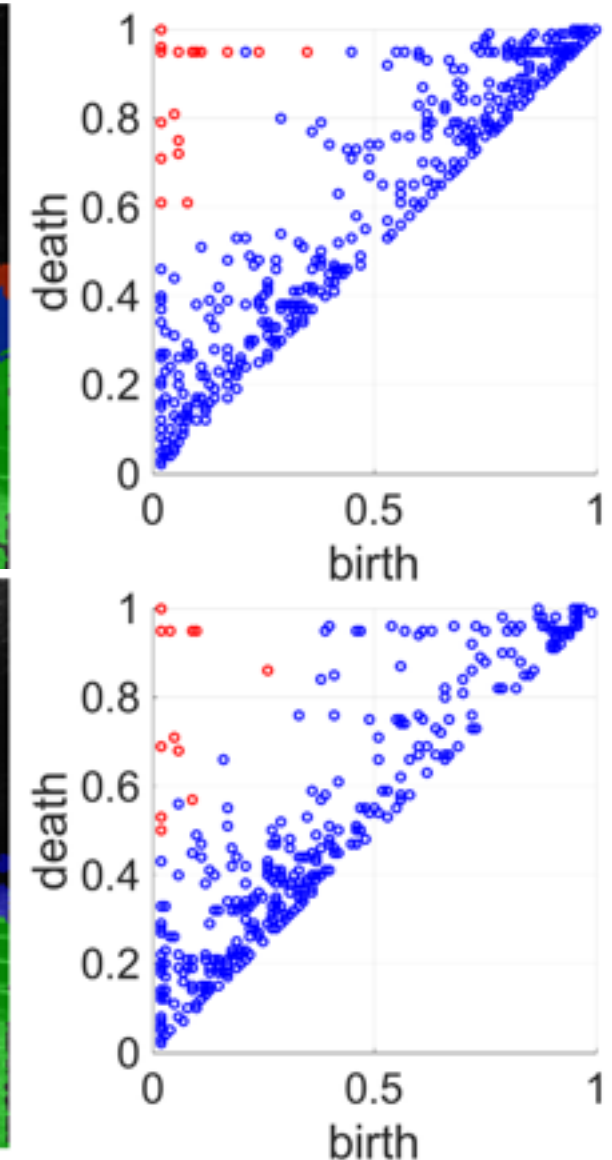
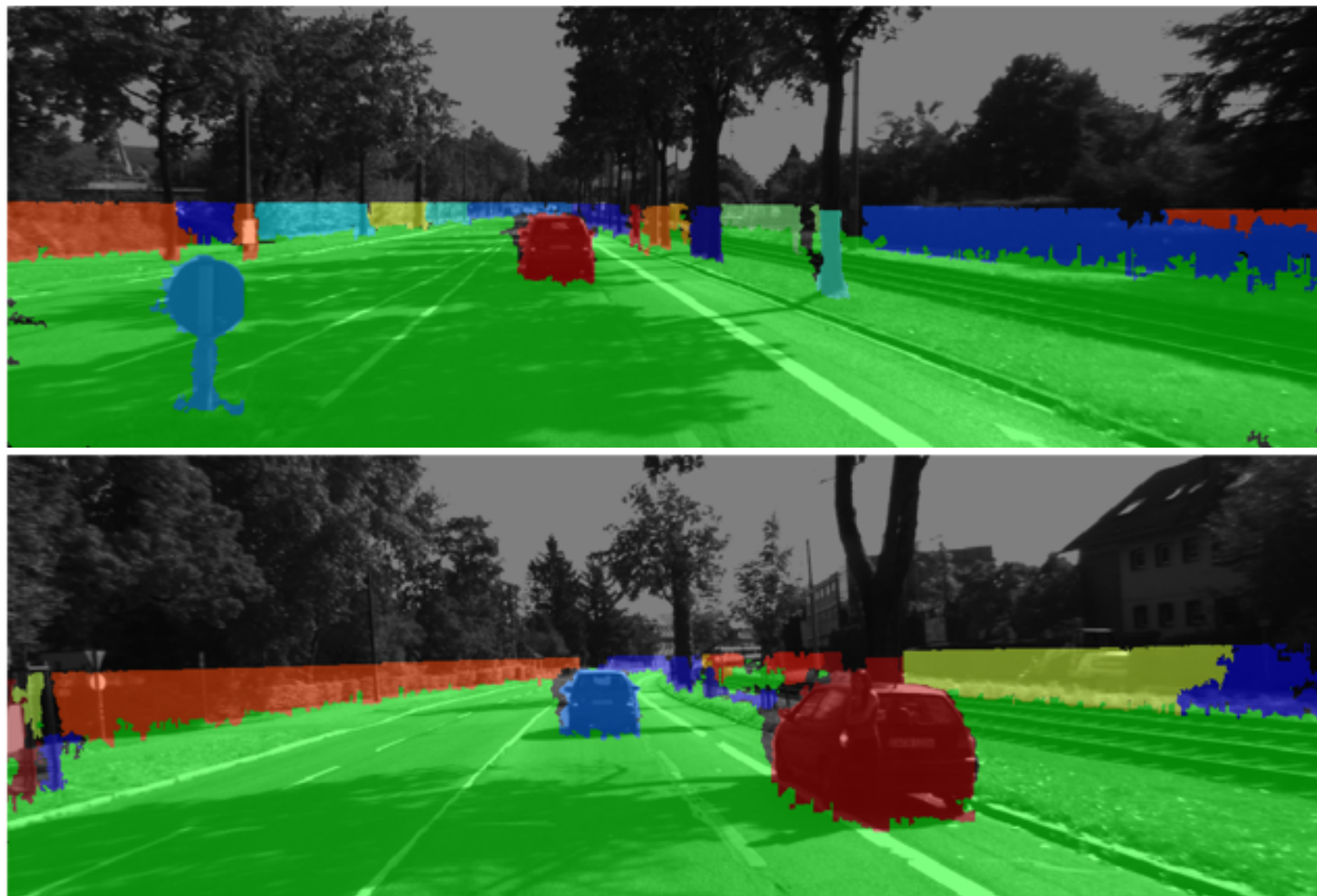
Obstacle Segmentation of Outdoor Scene

- **Experiment**
 - Dataset - KITTI Vision Benchmark Suite
 - Persistence threshold = 0.45



Obstacle Segmentation of Outdoor Scene

- **Experiment**
 - Dataset - KITTI Vision Benchmark Suite
 - Persistence threshold = 0.45



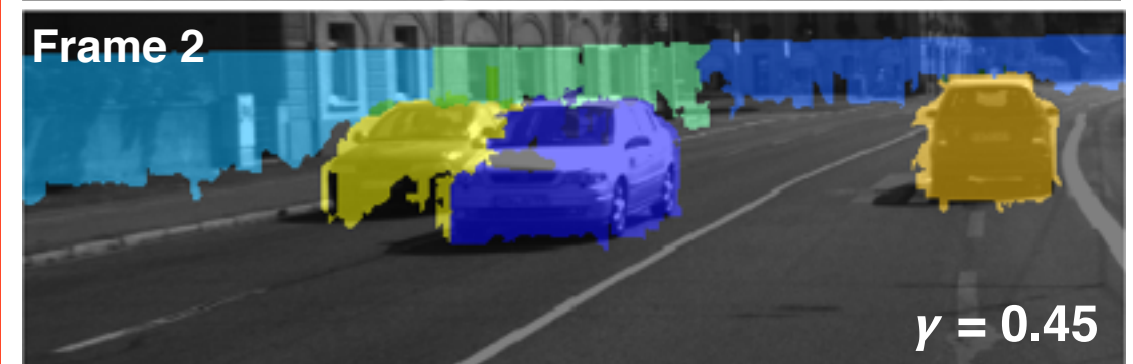
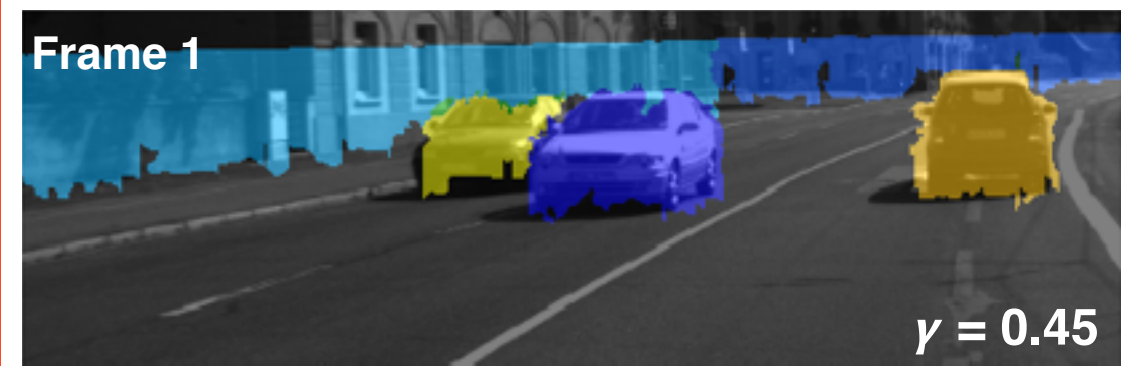
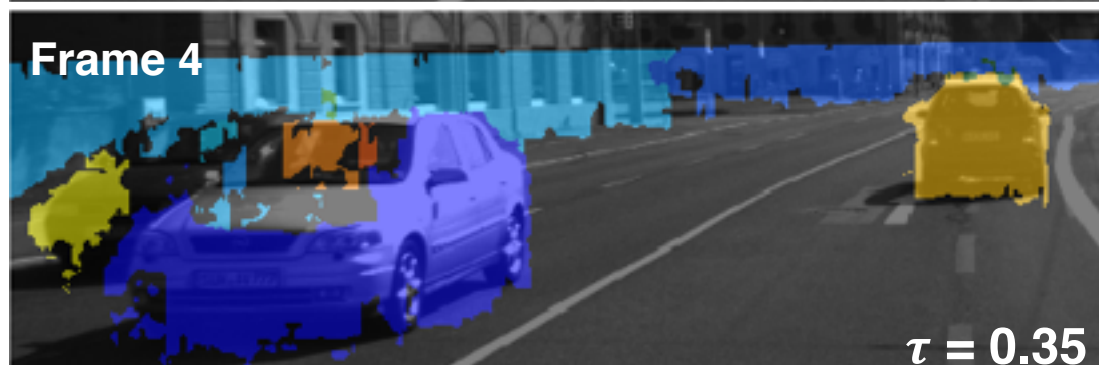
Obstacle Segmentation of Outdoor Scene

- Experiment - Compare with simple thresholding
 - Changing thresholding parameters



Obstacle Segmentation of Outdoor Scene

- Experiment - Compare with simple thresholding
 - Changing images with the same threshold



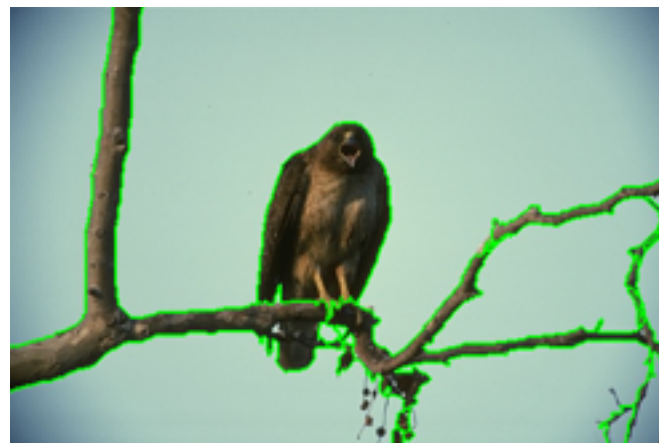
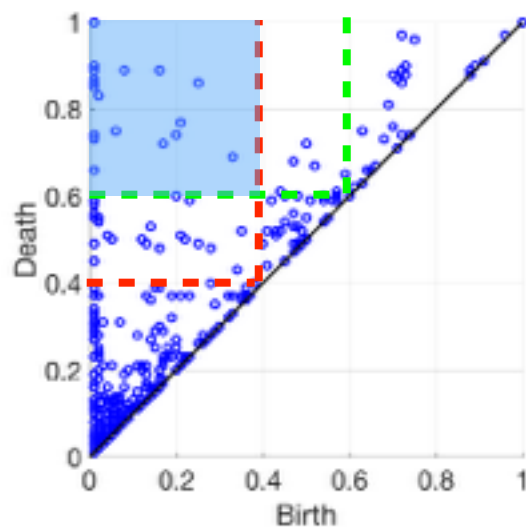
Conclusion

- ▶ Present an innovative framework for image segmentation based on topological persistence which is robust to image conditions and parameter selection.
- ▶ Applied to consensus-based image segmentation which is able to get better segmentation results.
- ▶ Applied to obstacle detection in outdoor scene for autonomous driving which is robust to parameter selection.

Future work

- **Extension**

- ▶ Find a better parameter selection strategy for consensus-based image segmentation.



- ▶ Refine the obstacle segmentation using Markov Random Field.



Thanks!

Obstacle Segmentation of Outdoor Scene

- Disparity map



Persistent Homology

- Homology is motivated by the observation that two shapes can be distinguished by their holes



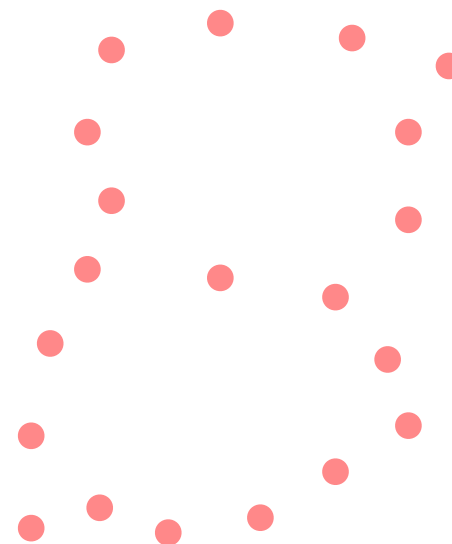
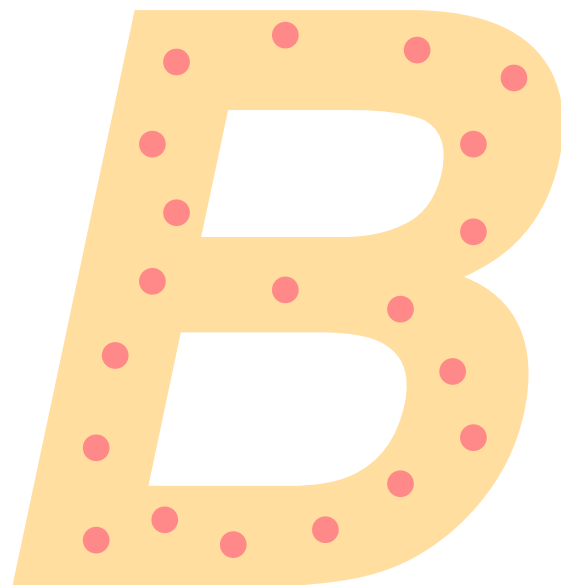
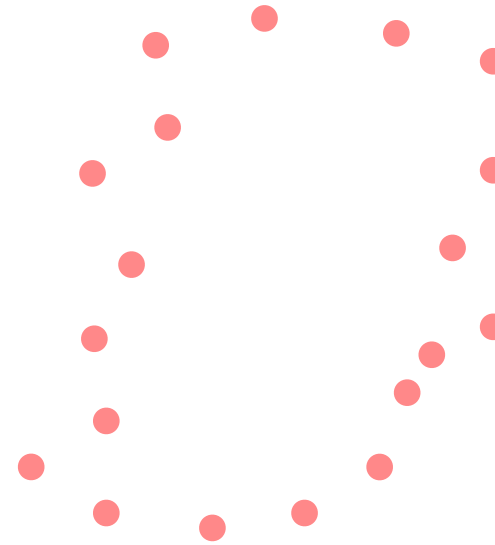
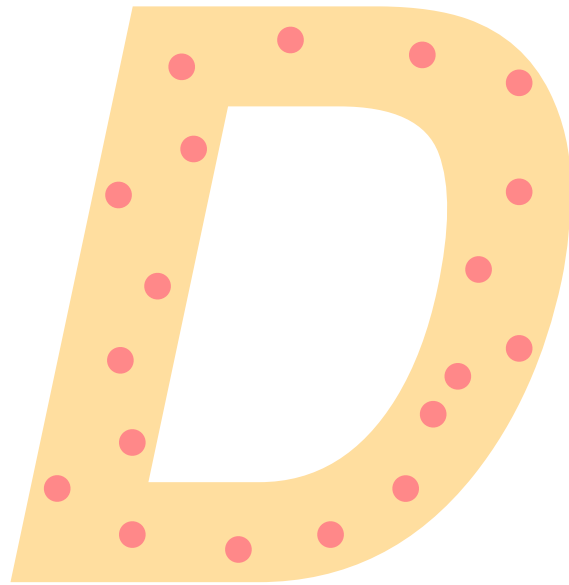
- One connected component
- One hole



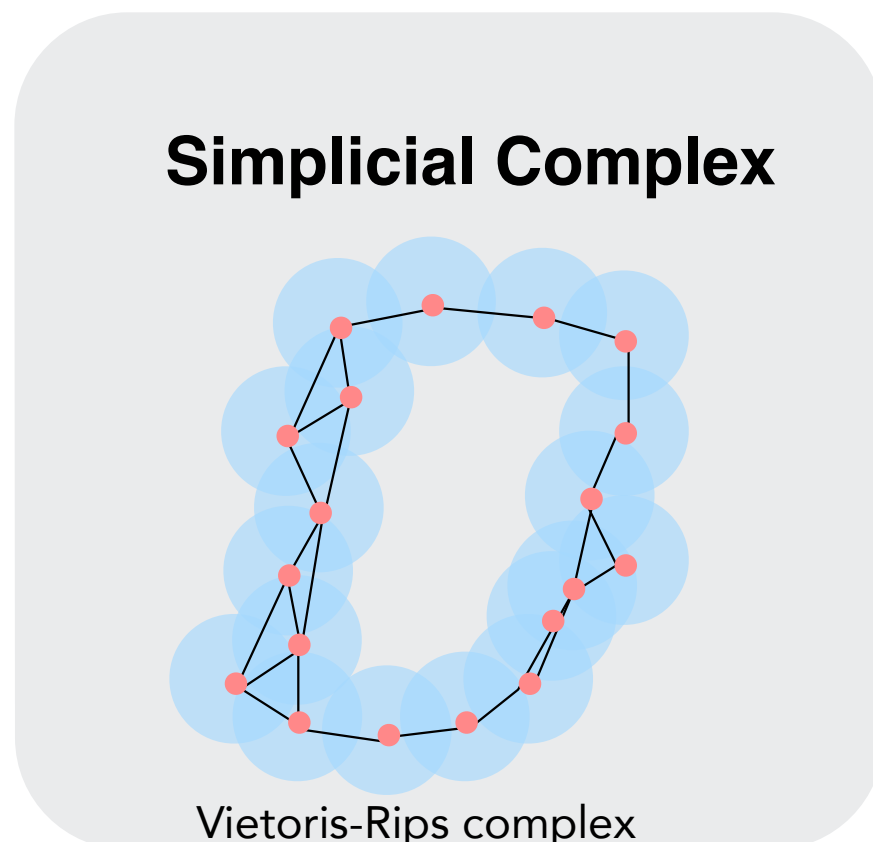
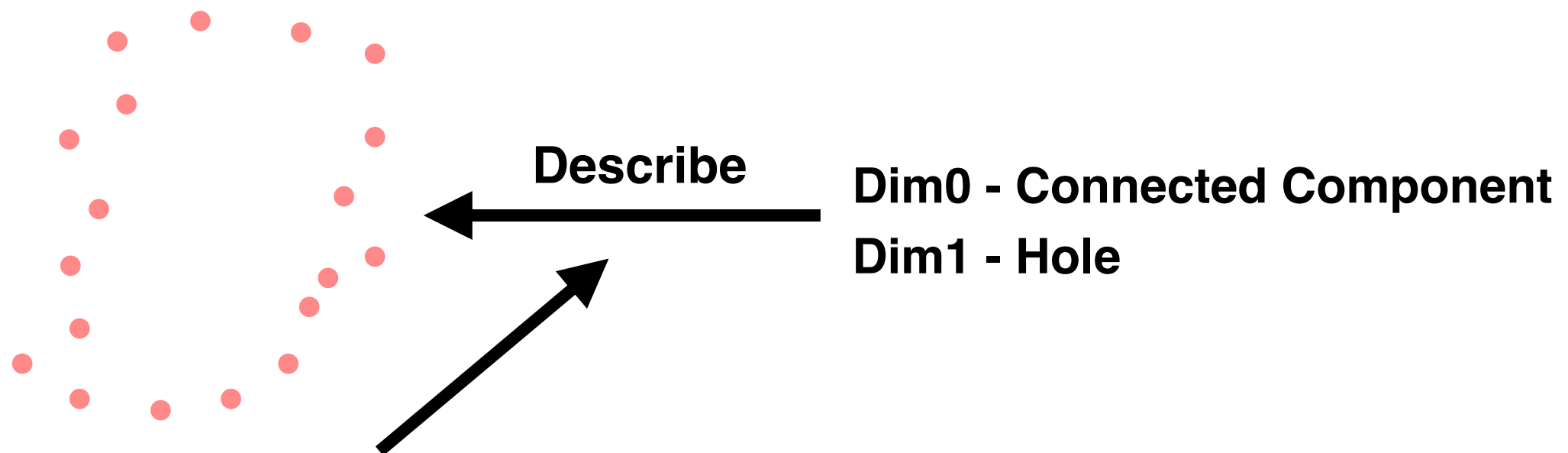
- One connected component
- Two holes

Persistent Homology

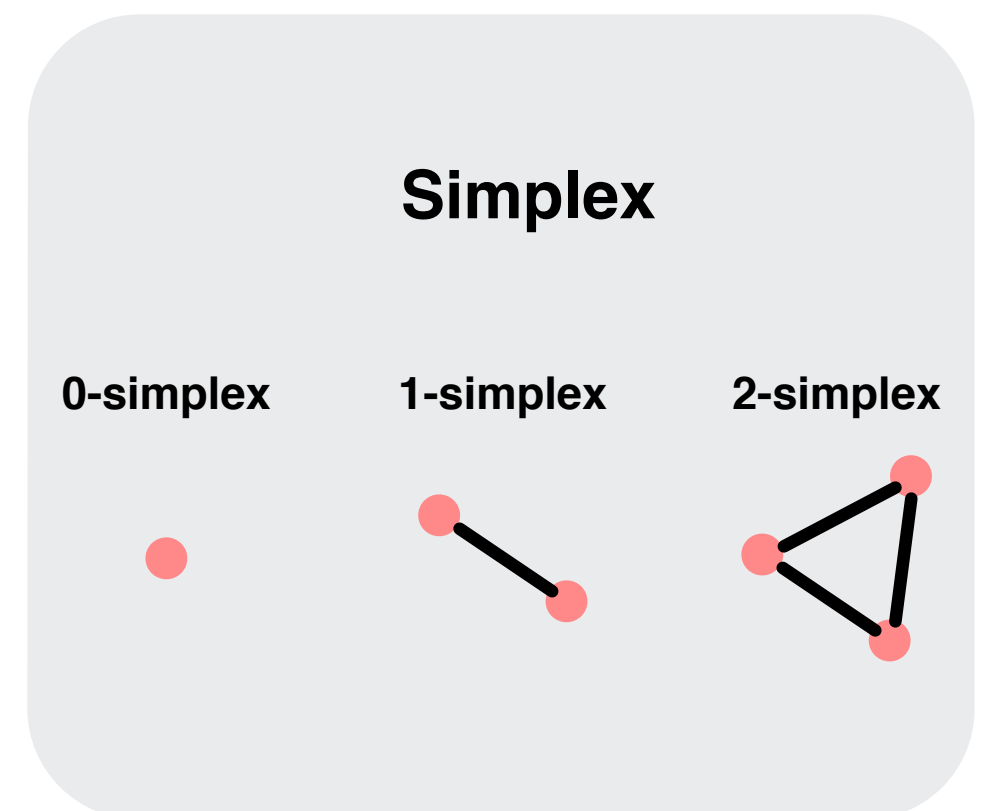
- Sample topological space by point cloud



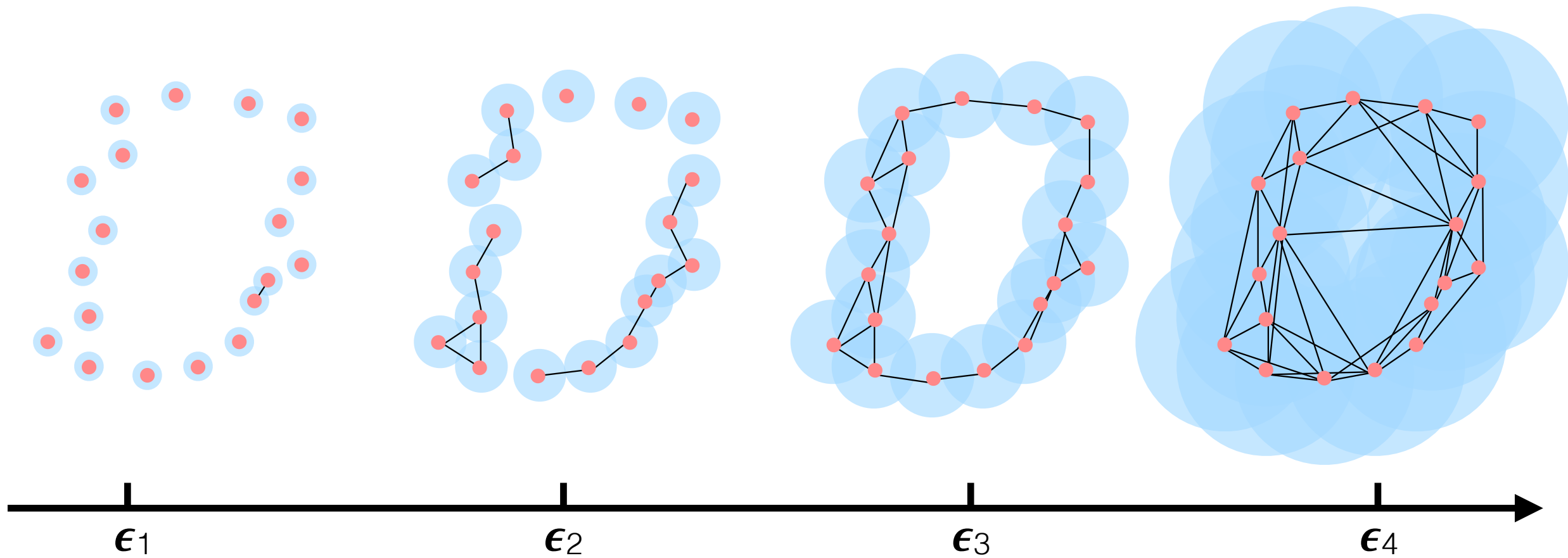
Persistent Homology



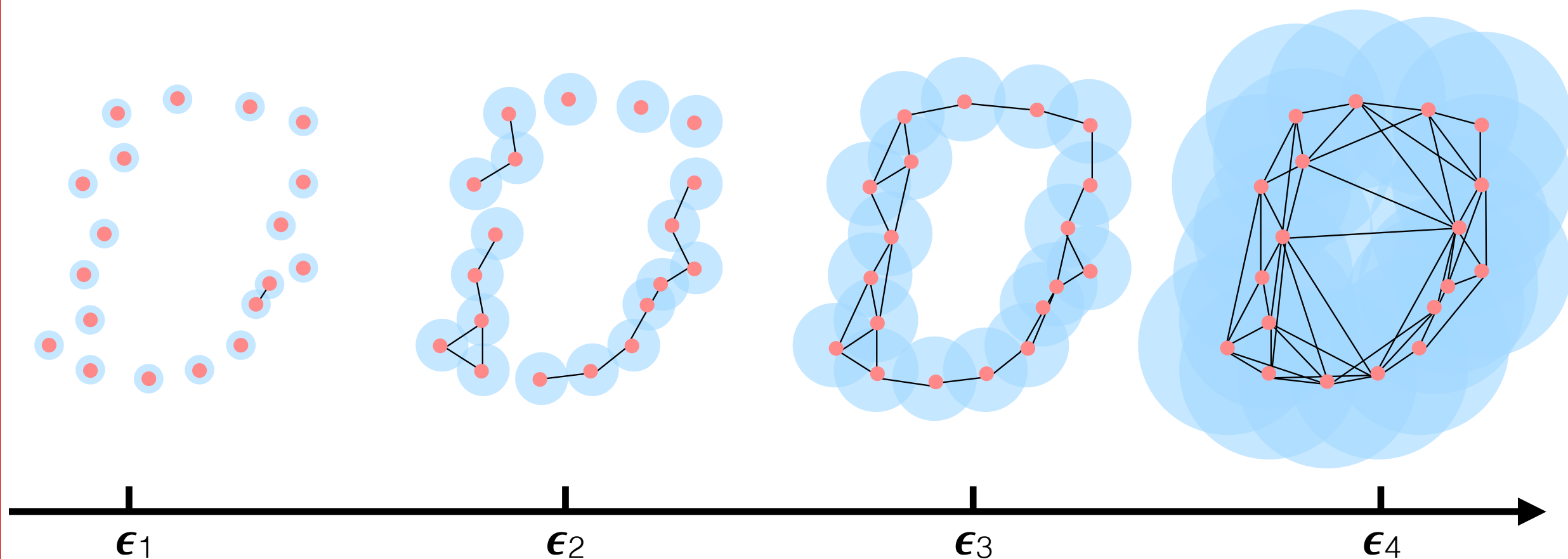
Finite Collection



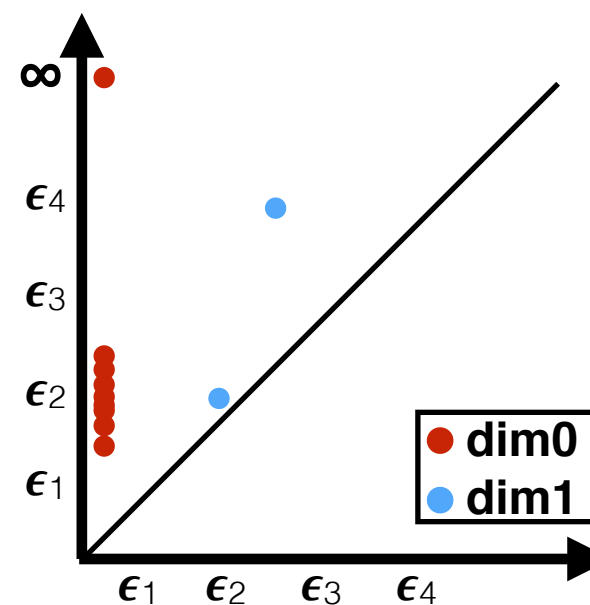
Persistent Homology



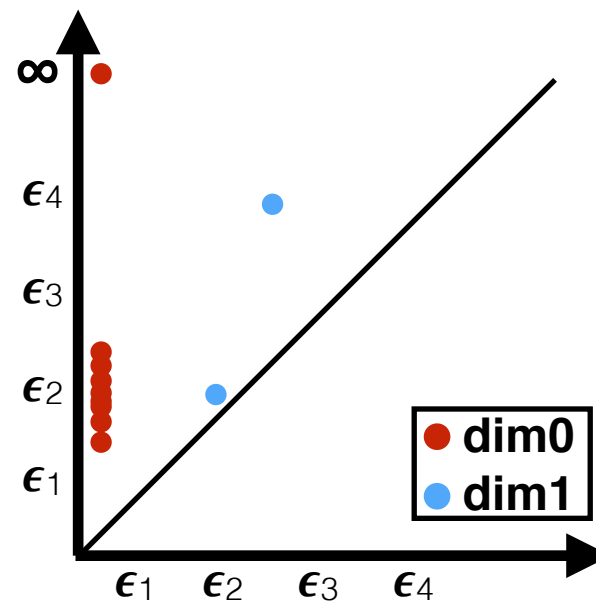
Persistent Homology



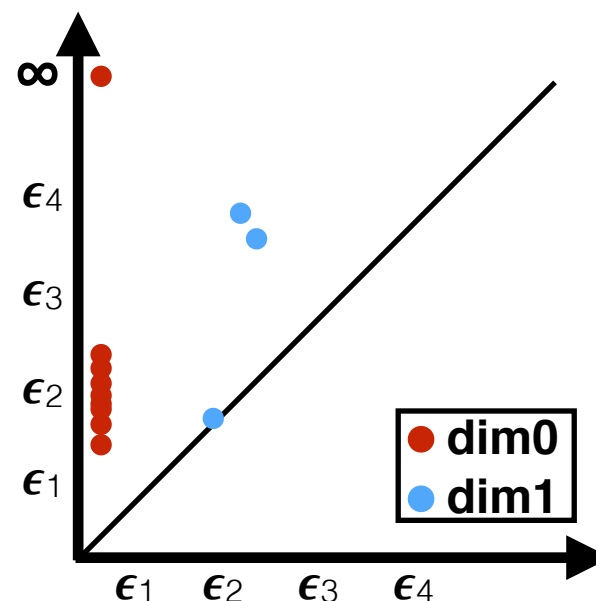
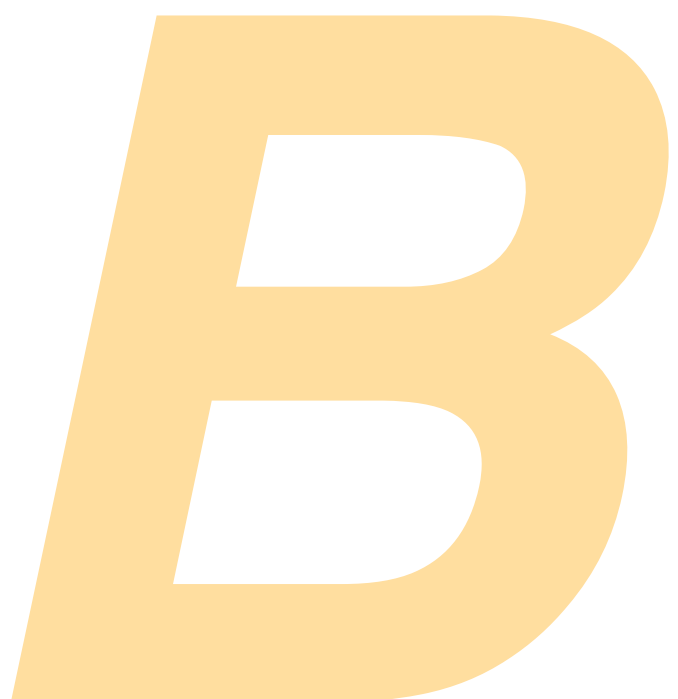
Persistence Diagram



Persistent Homology



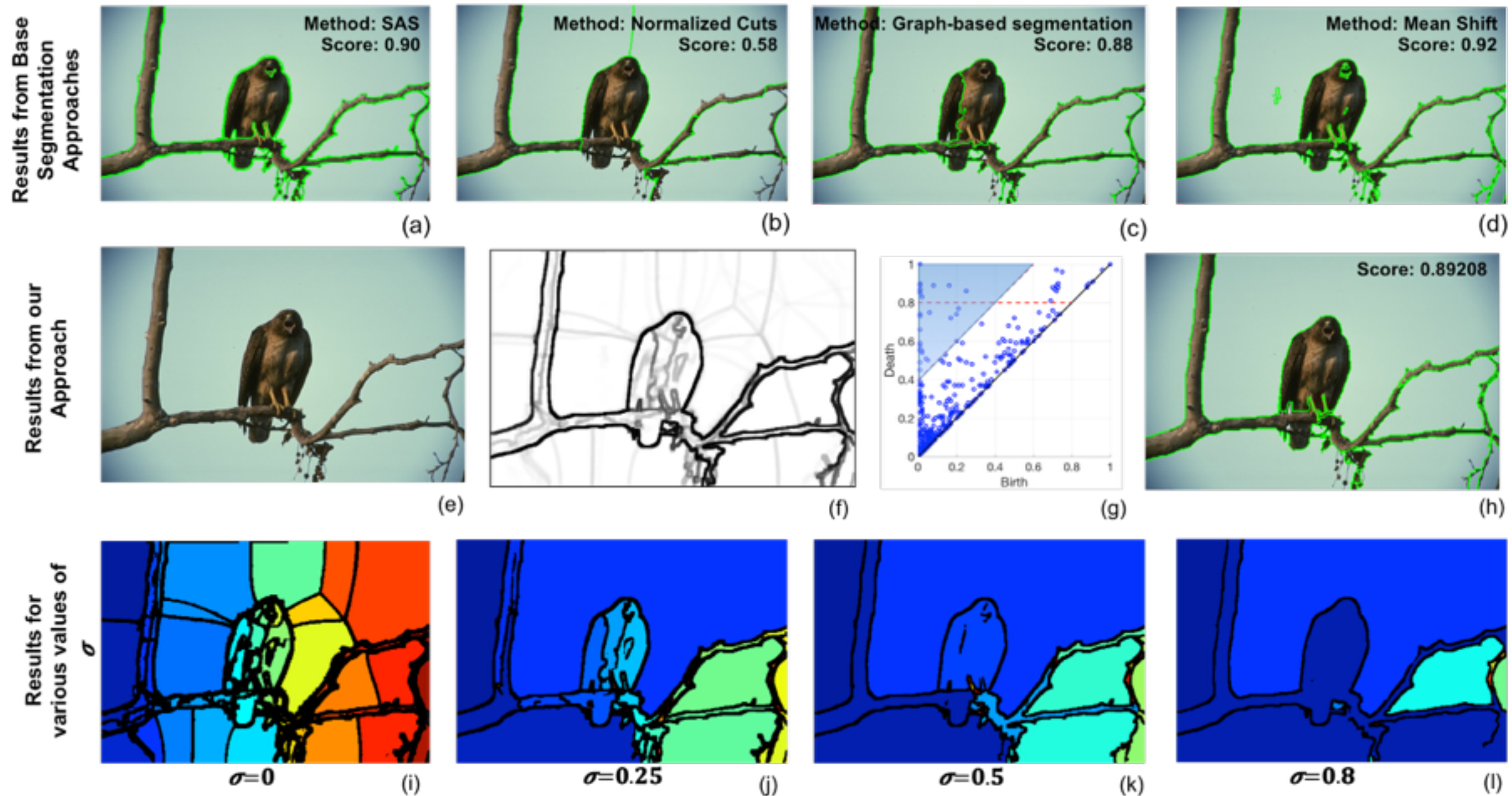
One connected component
One hole



One connected component
Two holes

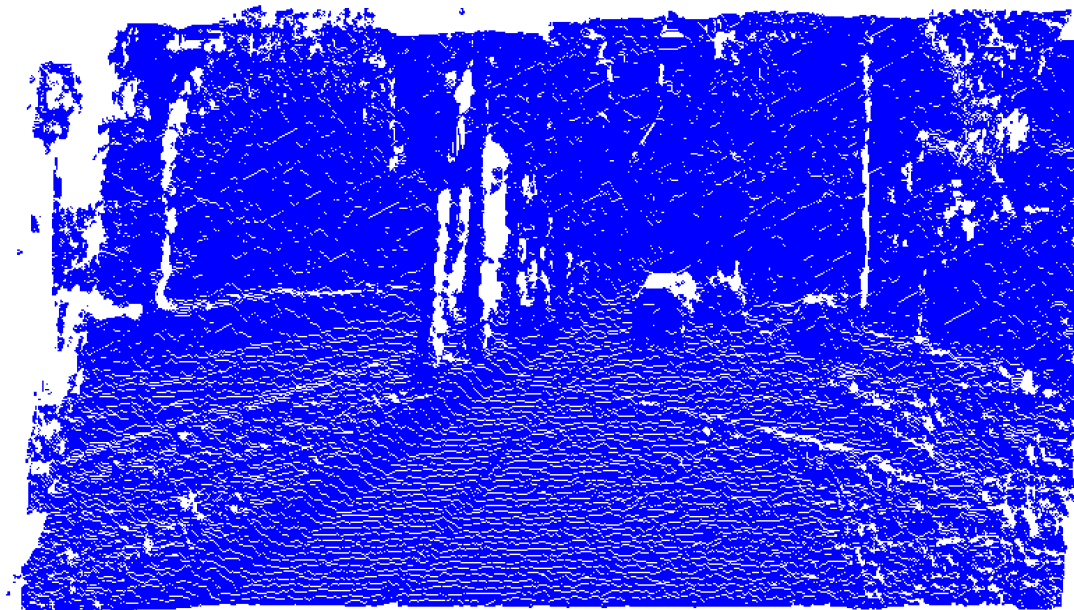
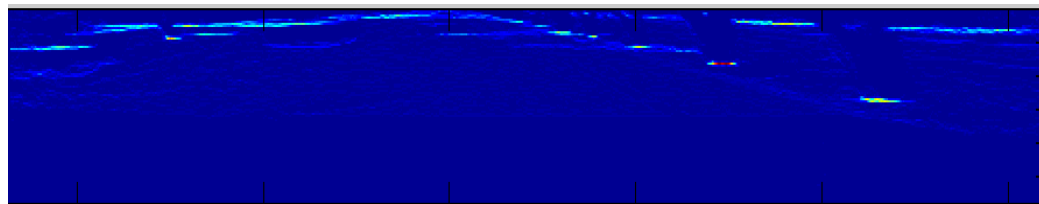
Consensus-based Image Segmentation

- Experiment - Result

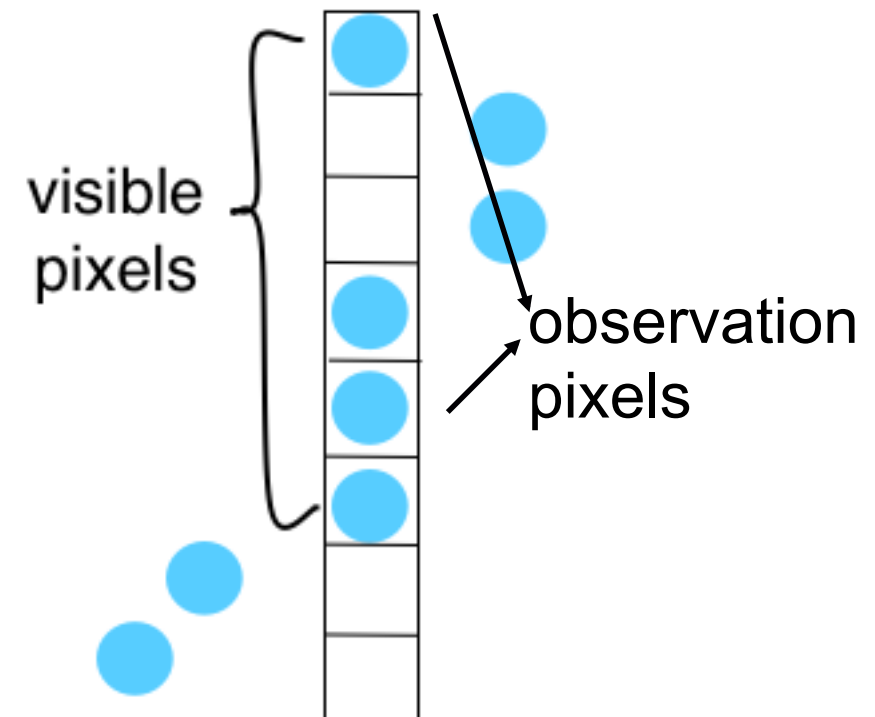


Obstacle Segmentation of Outdoor Scene

- Occupancy computation



One column in point cloud



Obstacle Segmentation of Outdoor Scene

- Occupancy computation

$$P(O_s) = \sum_{v,c} P(V_s = v, C_s = c) P(O_s | V_s = v, C_s = c)$$

$$P(V_s = 1) = N_v(s) / N_p(s)$$

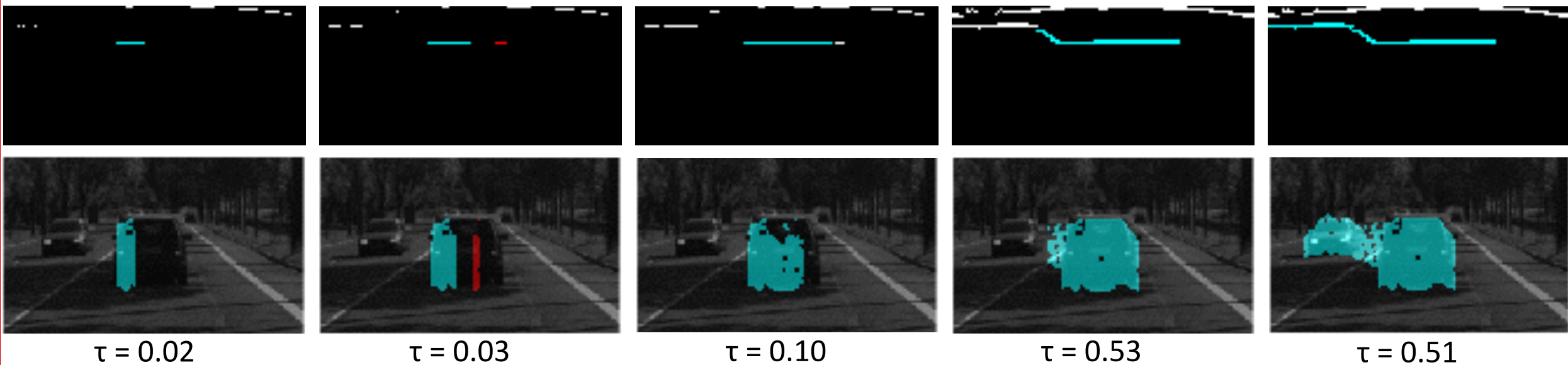
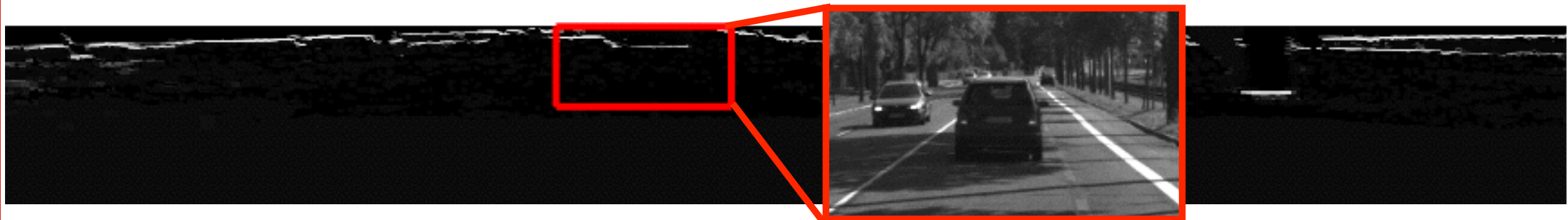
$$P(C_s = 1) = 1 - e^{-\lambda \frac{N_o(s)}{N_v(s)}}$$

Let $P_v := N_v(s) / N_p(s)$ and $P_o := N_o(s) / N_v(s)$. Then, we have

$$\begin{aligned} P(O_s) &= P(V_s)P(C_s)(1 - P_{FP}) + P(V_s)(1 - P(C_s))P_{FN} + \frac{1}{2}(1 - P(V_s)) \\ &= \left(\frac{1}{2} - P_{FP}\right)P_v + (P_{FP} + P_{FN} - 1)P_v e^{-\lambda P_o} + \frac{1}{2} \end{aligned}$$

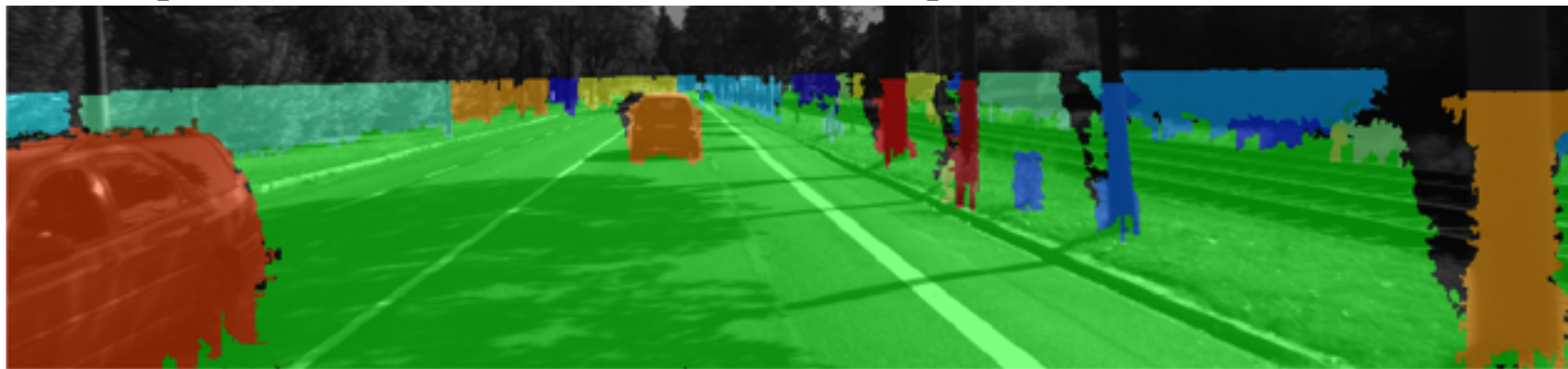
Obstacle Segmentation of Outdoor Scene

- Persistence region extraction

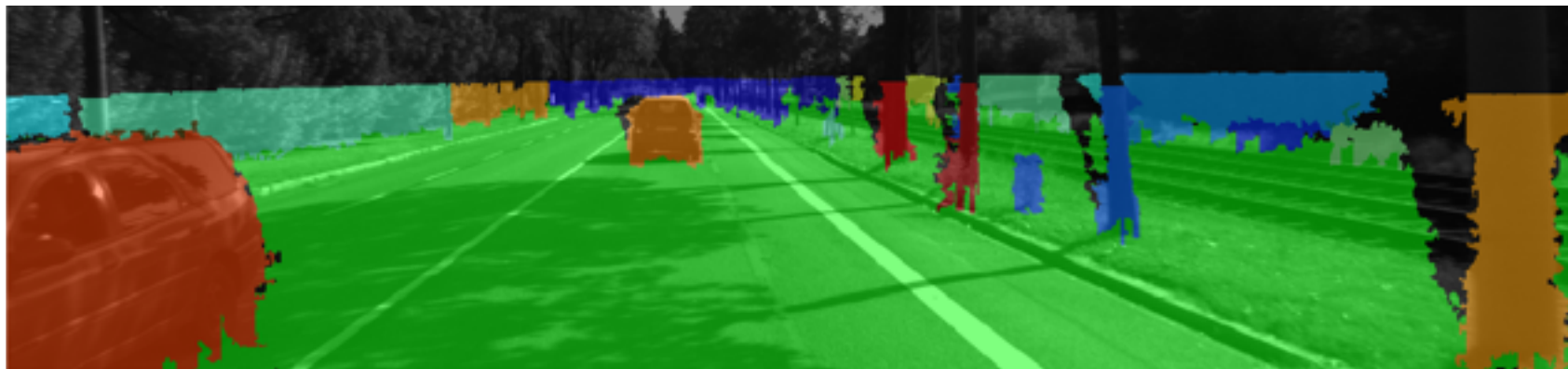


Obstacle Segmentation of Outdoor Scene

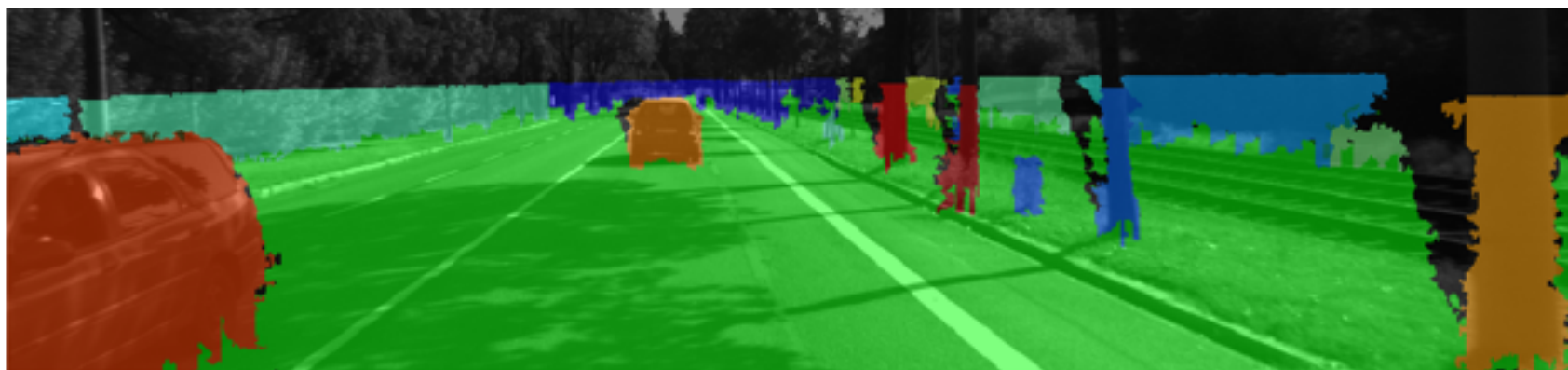
- Experiment - Effect of parameter



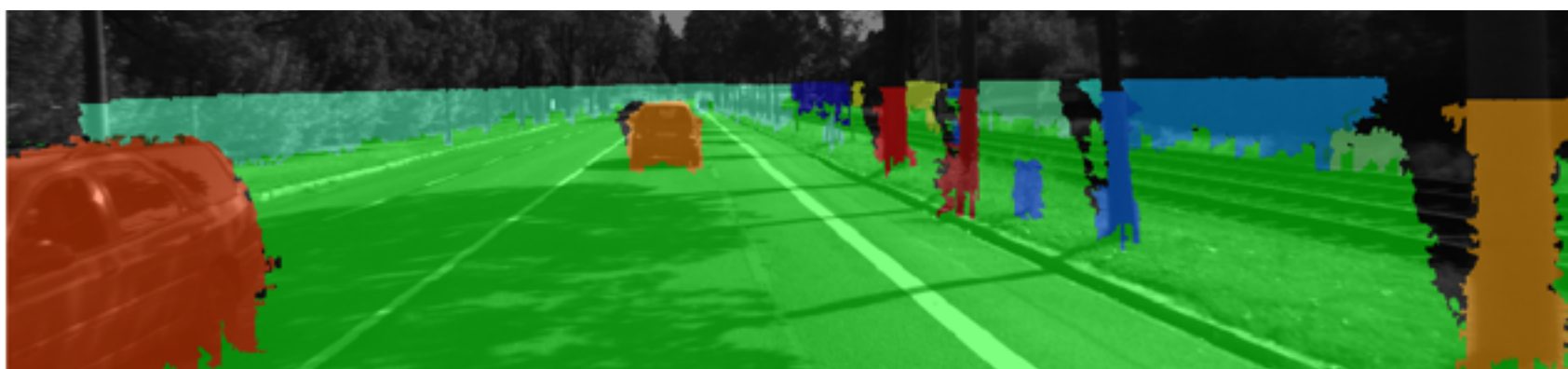
$\gamma = 0.30$



$\gamma = 0.40$



$\gamma = 0.50$



$\gamma = 0.60$

Consensus-based Image Segmentation

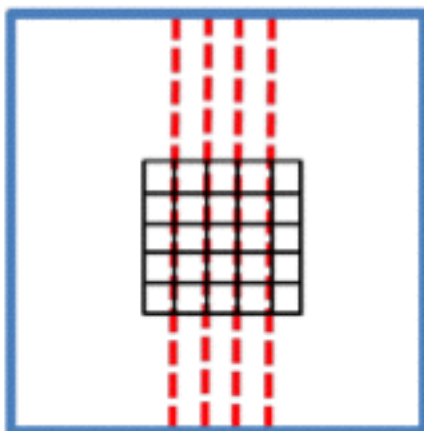
- Effect of patch size n

Let 2σ be the range of perturbation of an edge.

Case 1

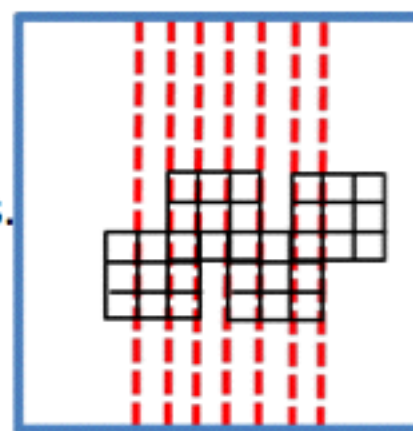
$$n - 2 \geq 2\sigma, D_n^*(x) = p_{ij}.$$

The range can be covered by a single patch.



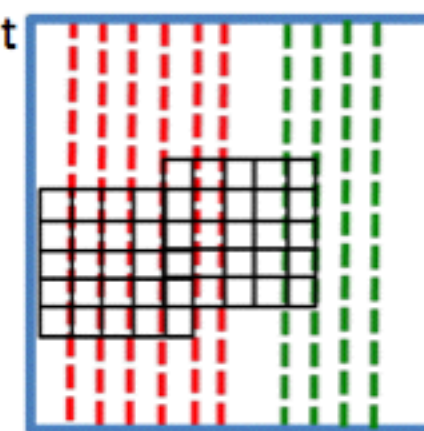
Case 2

$n - 1 < 2\sigma$,
 $p_{ij}/m \leq D_n^*(x) < p_{ij}$,
 where $m = \lceil (2\sigma + 1)/(n - 1) \rceil$.
 The range can be covered by m patches.



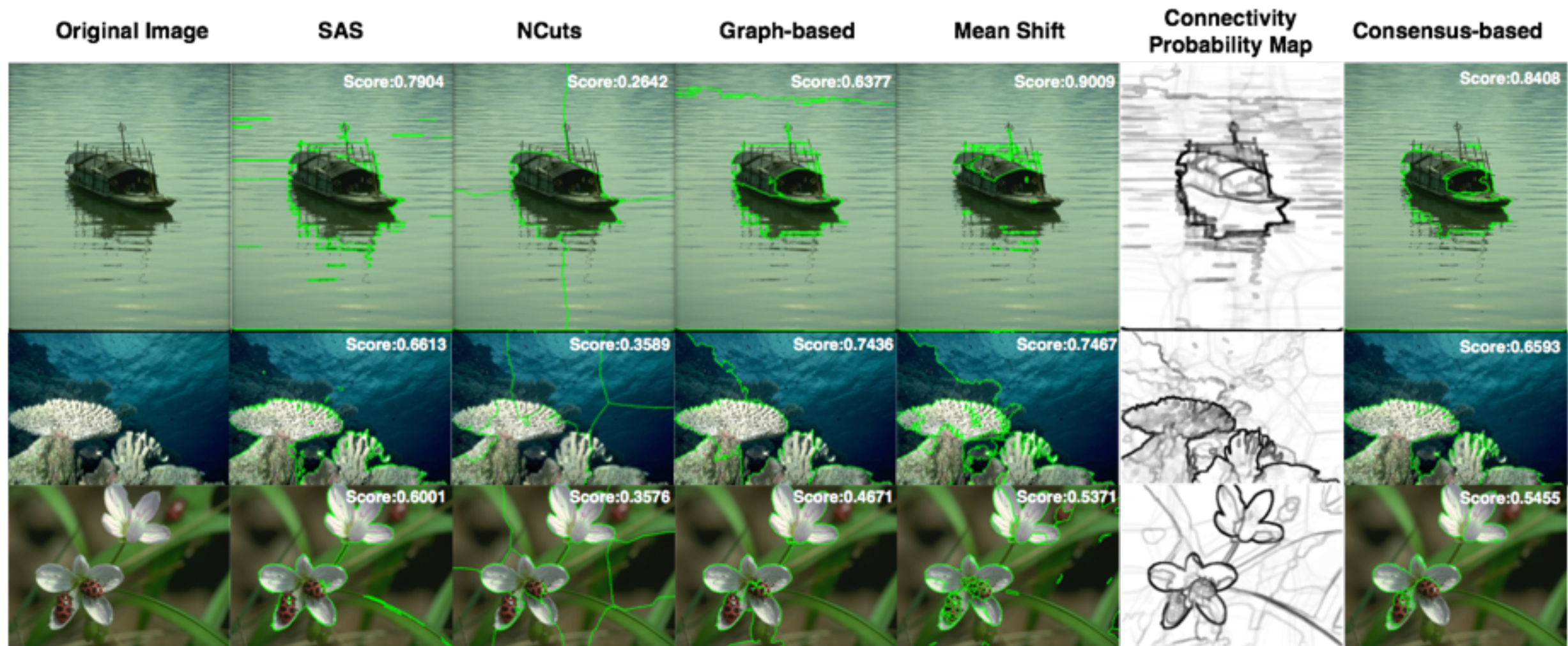
Case 3

Perturbation range of two edges $n-1$ pixels away from each other can be identified without the influence of other edges.



Consensus-based Image Segmentation

- Experiment - Result



Obstacle Segmentation of Outdoor Scene

- Stereo vision setup

