

Topological Persistence in Computer Vision: Applications to Obstacle Detection and Image Segmentation

Qian Ge

Outline

- ▶ **Introduction**
- ▶ **Image Segmentation Framework**
- ▶ **Persistence Homology**
- ▶ **Consensus-based Image Segmentation**
- ▶ **Obstacle Detection of Outdoor Scene**
- ▶ **Conclusion and Future Work**

Image Segmentation

- Image segmentation clusters the image pixels into a set of groups visually distinct and uniform with respect to some properties.
- Region of interest depends on applications.



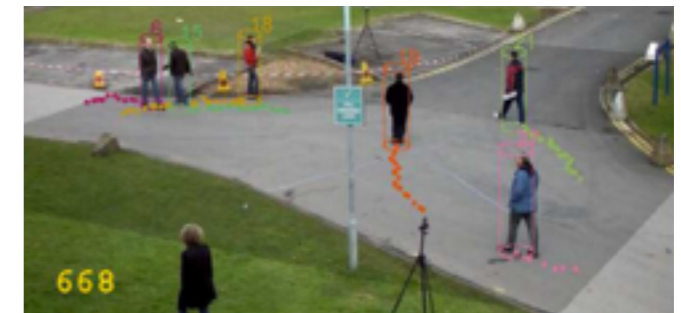
Image Segmentation

- Applications

Object Recognition



Object Tracking



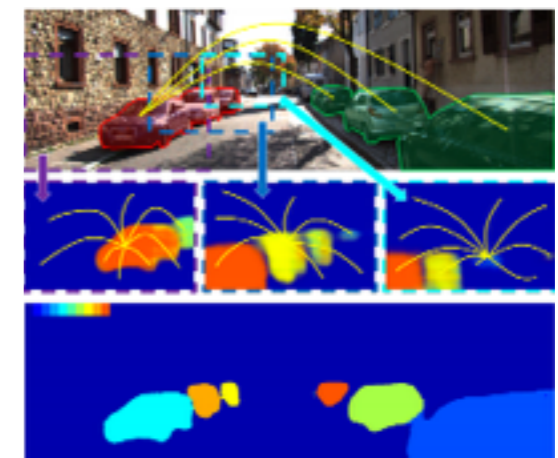
Video Surveillance



Image Segmentation



Autonomous Driving



Medical Imaging

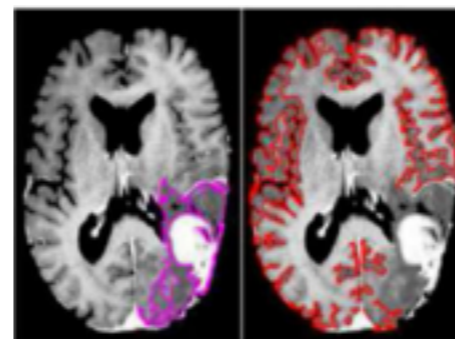


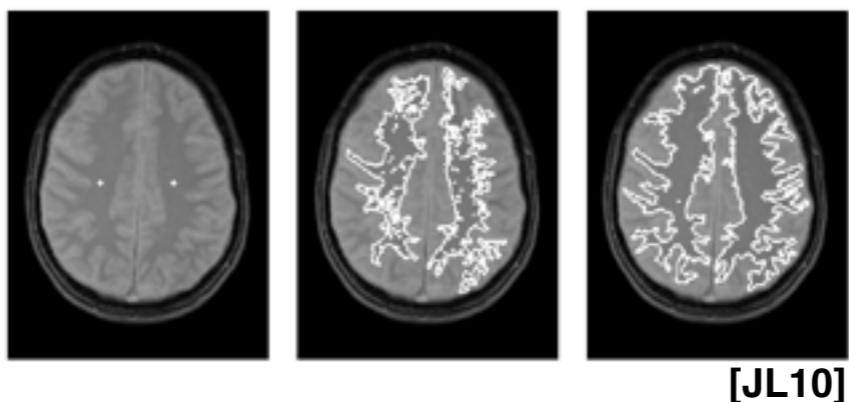
Image Segmentation

- Grouped by methodology:

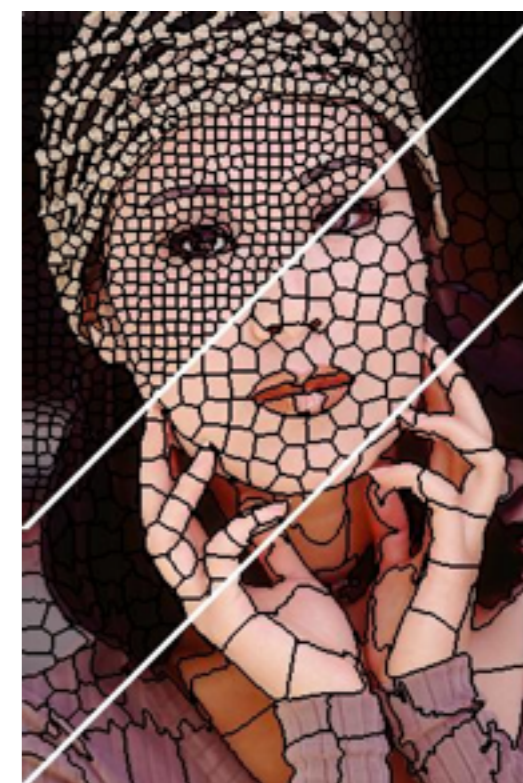
Clustering-based



Region Growing



Superpixel-based



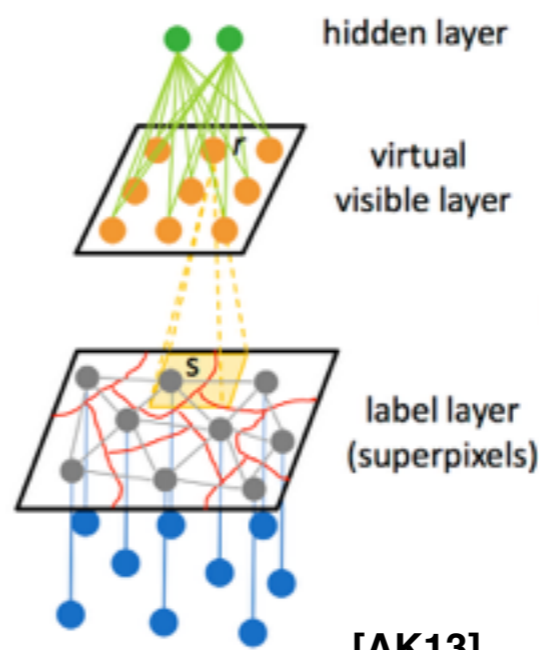
[RA12]

Edge-based



<http://www.roborealm.com/help/Canny.php>

Graph-based



[DC02] Dorin Comaniciu and Peter Meer. 2002. Mean Shift: A Robust Approach Toward Feature Space Analysis. IEEE Trans. Pattern Anal. Mach. Intell. 24, 5 (May 2002), 603-619.

[AK13] A. Kae, K. Sohn, H. Lee and E. Learned-Miller, "Augmenting CRFs with Boltzmann Machine Shape Priors for Image Labeling," 2013 IEEE Conference on Computer Vision and Pattern Recognition, Portland, OR, 2013, pp. 2019-2026.

[JL10] J. L. Rose, T. Grenier, C. Revol-Muller and C. Odet, "Unifying variational approach and region growing segmentation," 2010 18th European Signal Processing Conference, Aalborg, 2010, pp. 1781-1785.

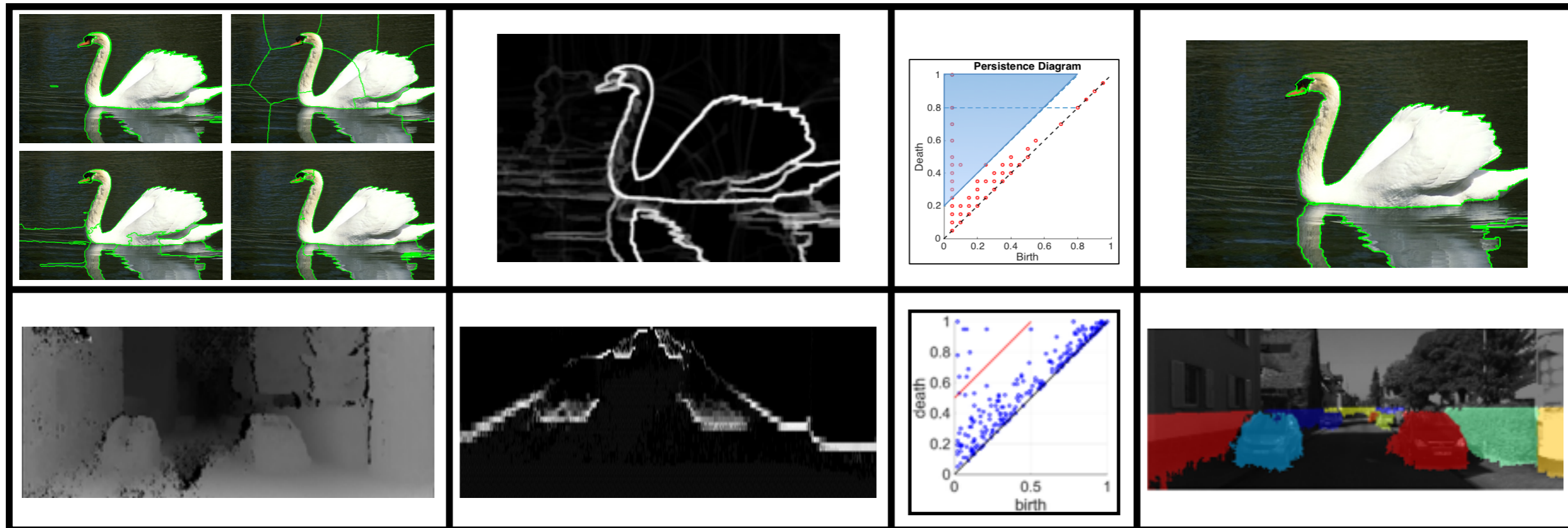
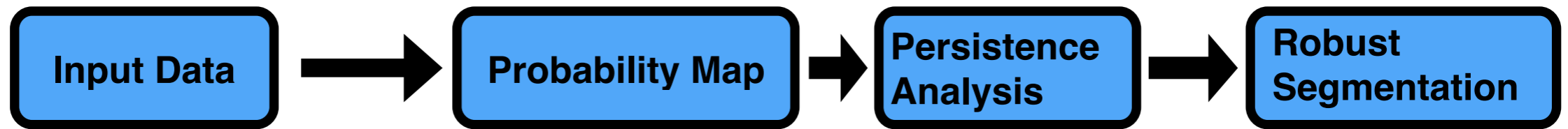
[RA12] Radhakrishna Achanta, Appu Shaji, Kevin Smith, Aurelien Lucchi, Pascal Fua, and Sabine Susstrunk. 2012. SLIC Superpixels Compared to State-of-the-Art Superpixel Methods. IEEE Trans. Pattern Anal. Mach. Intell. 34, 11 (November 2012), 2274-2282.

Why Robust?

- **Robust to noise, parameter selection, image quality and resolution**
 - ▶ Medical images are often polluted noisy.
 - ▶ User inputs cannot be the same every time.
 - ▶ Outdoor scene images quality varies over time.

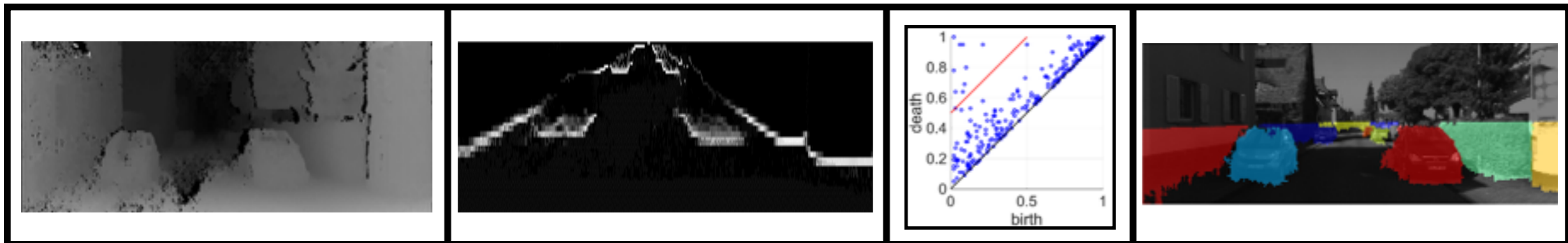
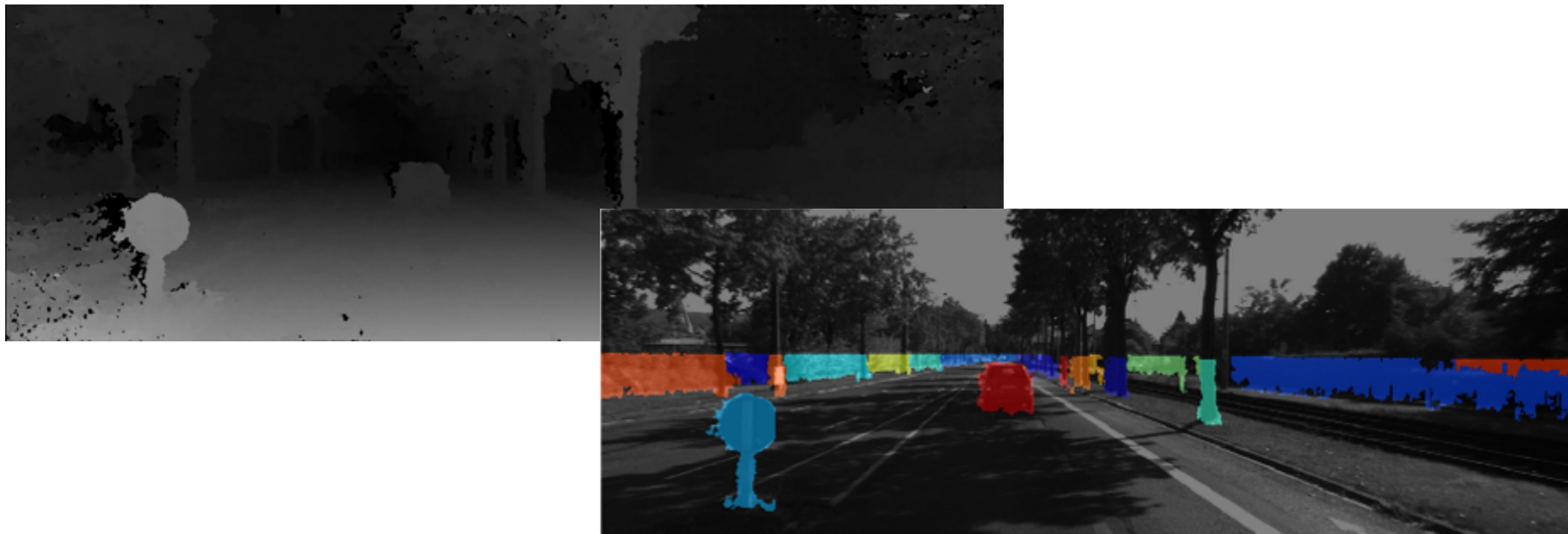


Framework of Robust Segmentation



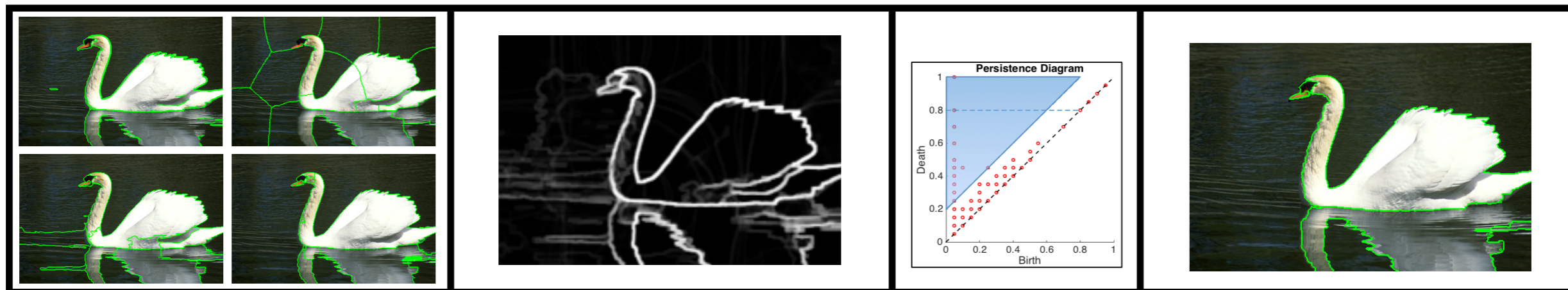
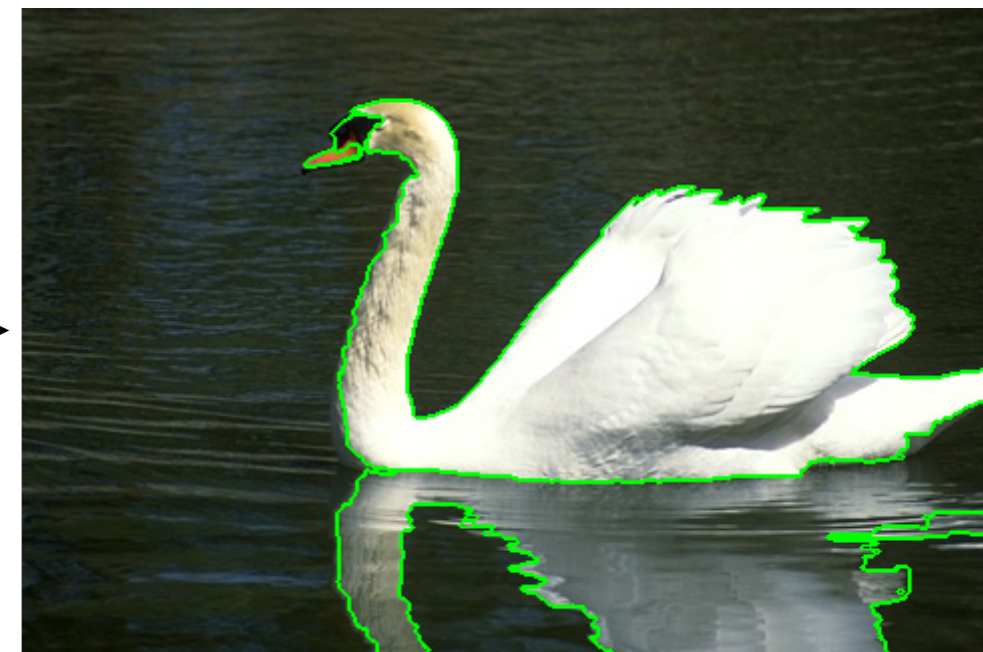
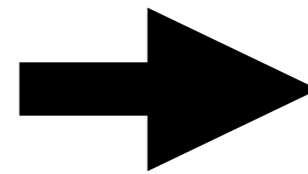
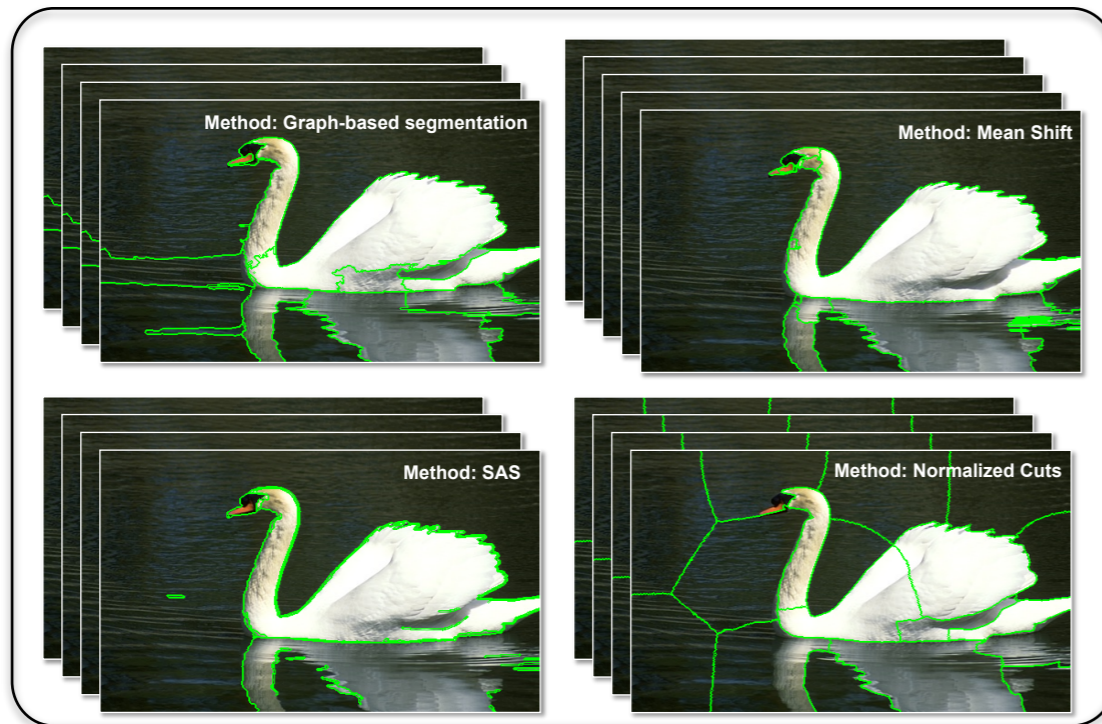
Framework of Robust Segmentation

- Obstacle segmentation of outdoor scene



Framework of Robust Segmentation

- Consensus-based image segmentation

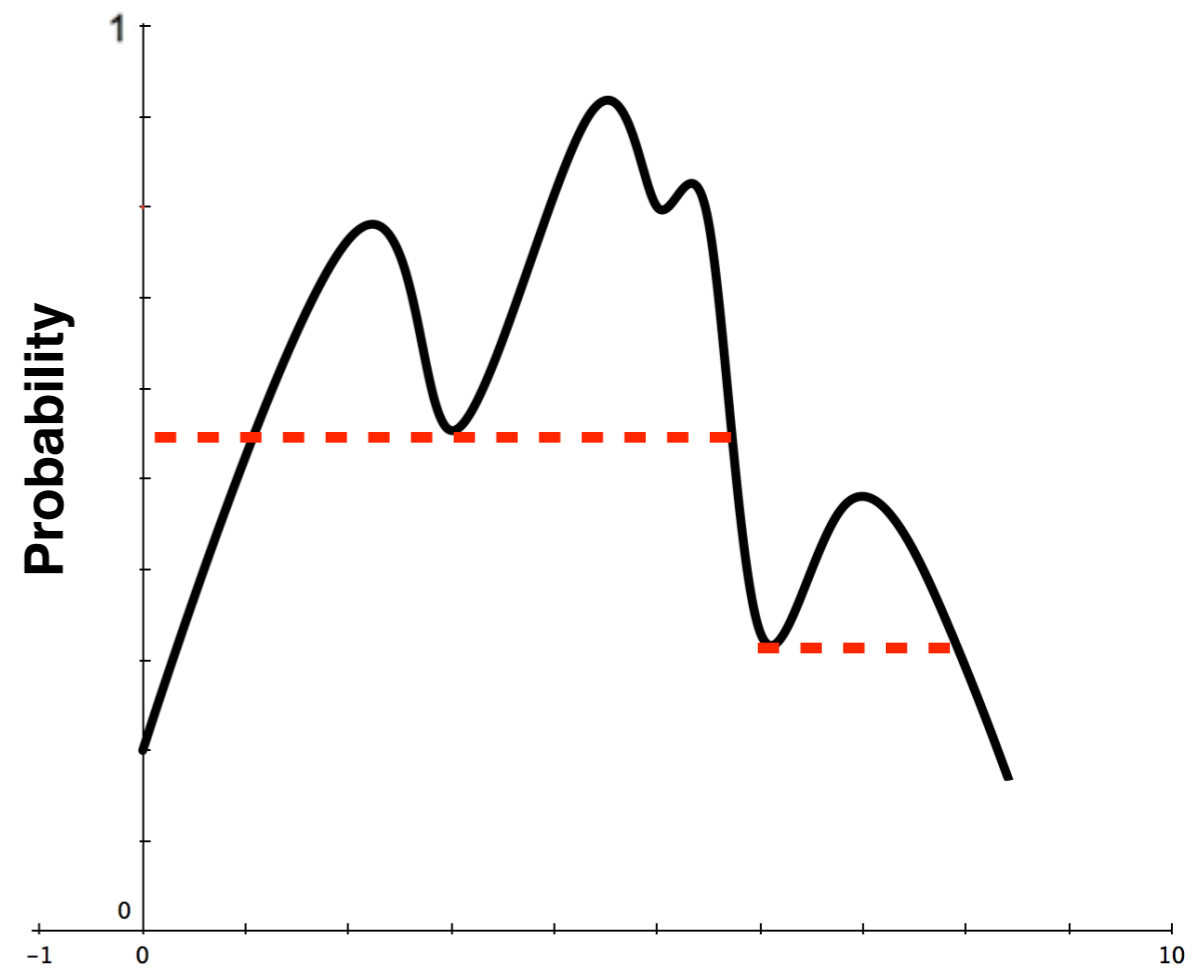
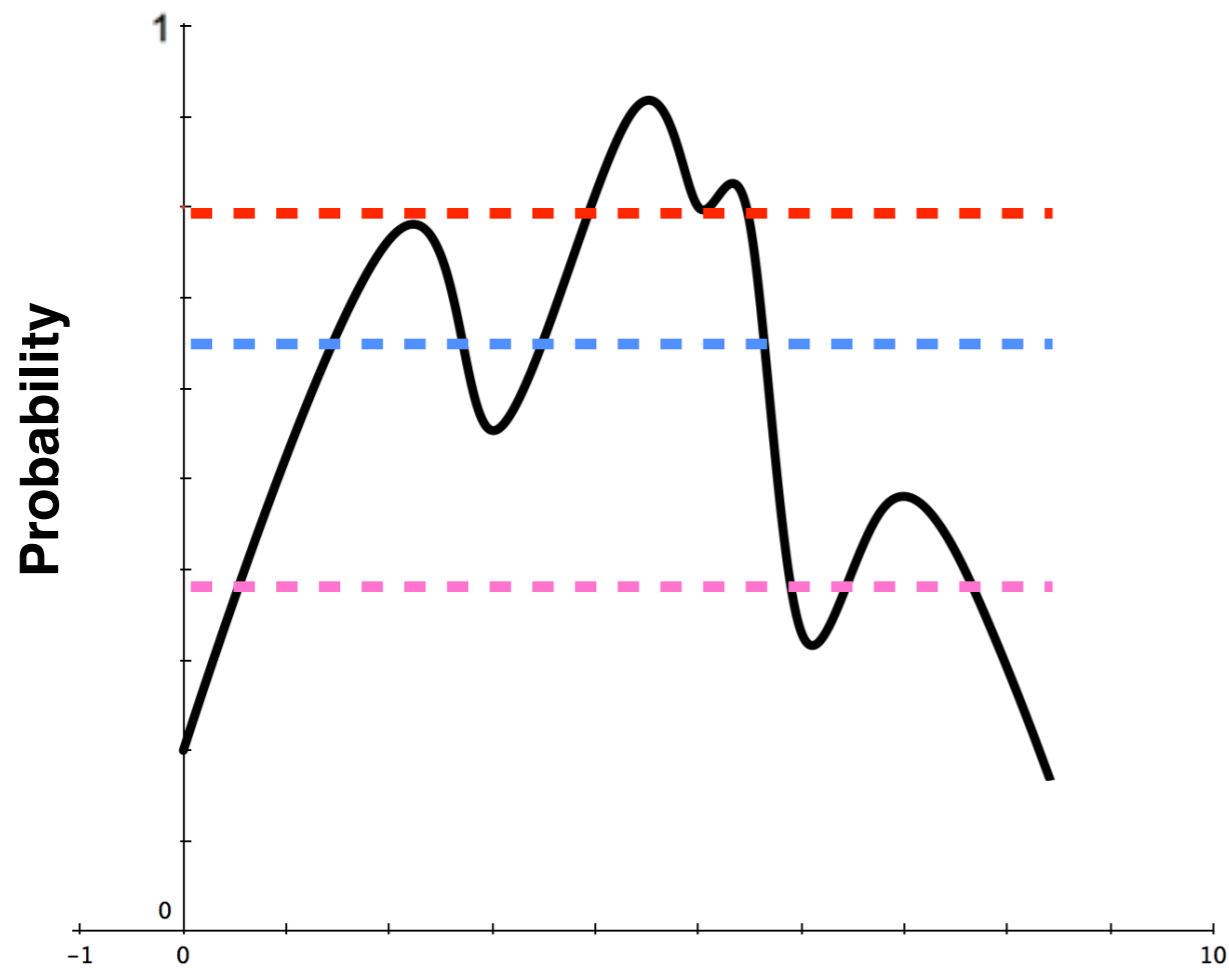


Contribution

- ▶ Present an innovative framework for image segmentation based on topological persistence which is robust to image conditions and parameter selection.
- ▶ Applied to obstacle detection in outdoor scene for autonomous driving which is robust to parameter selection.
- ▶ Applied to consensus-based image segmentation which is able to get better segmentation results.

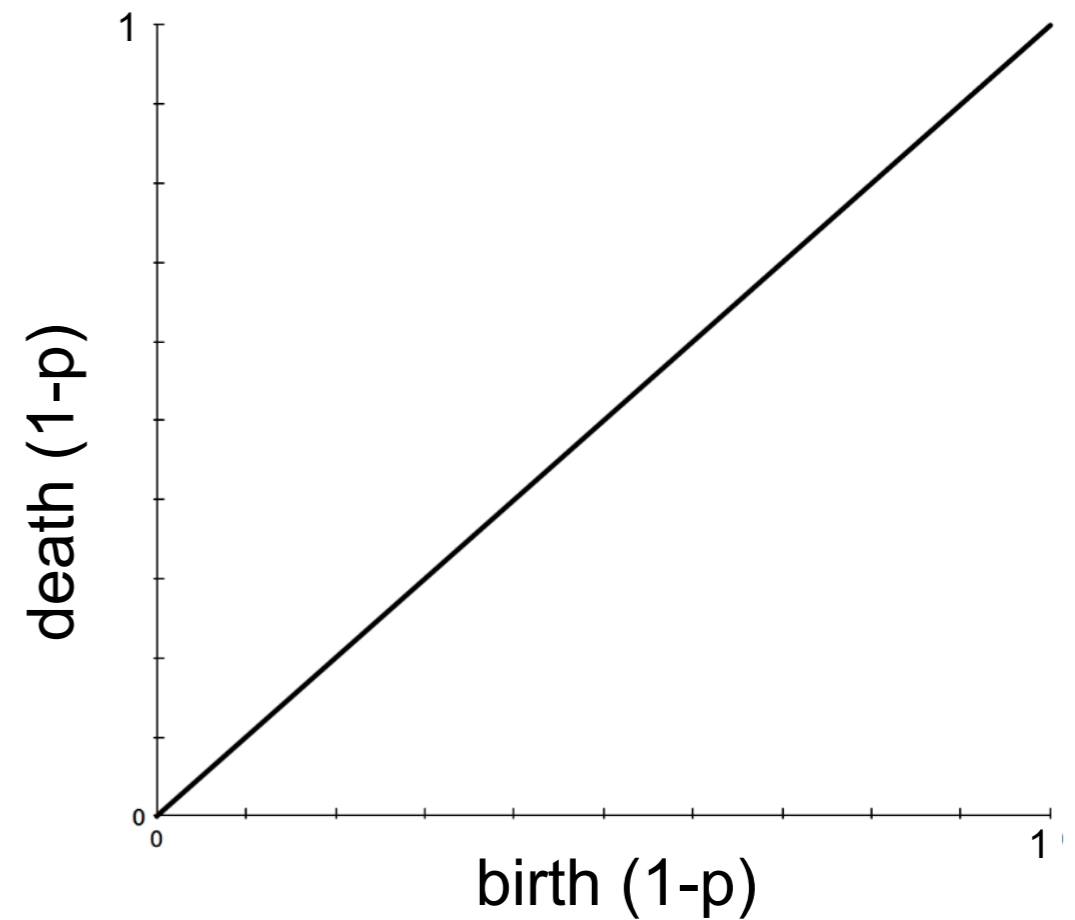
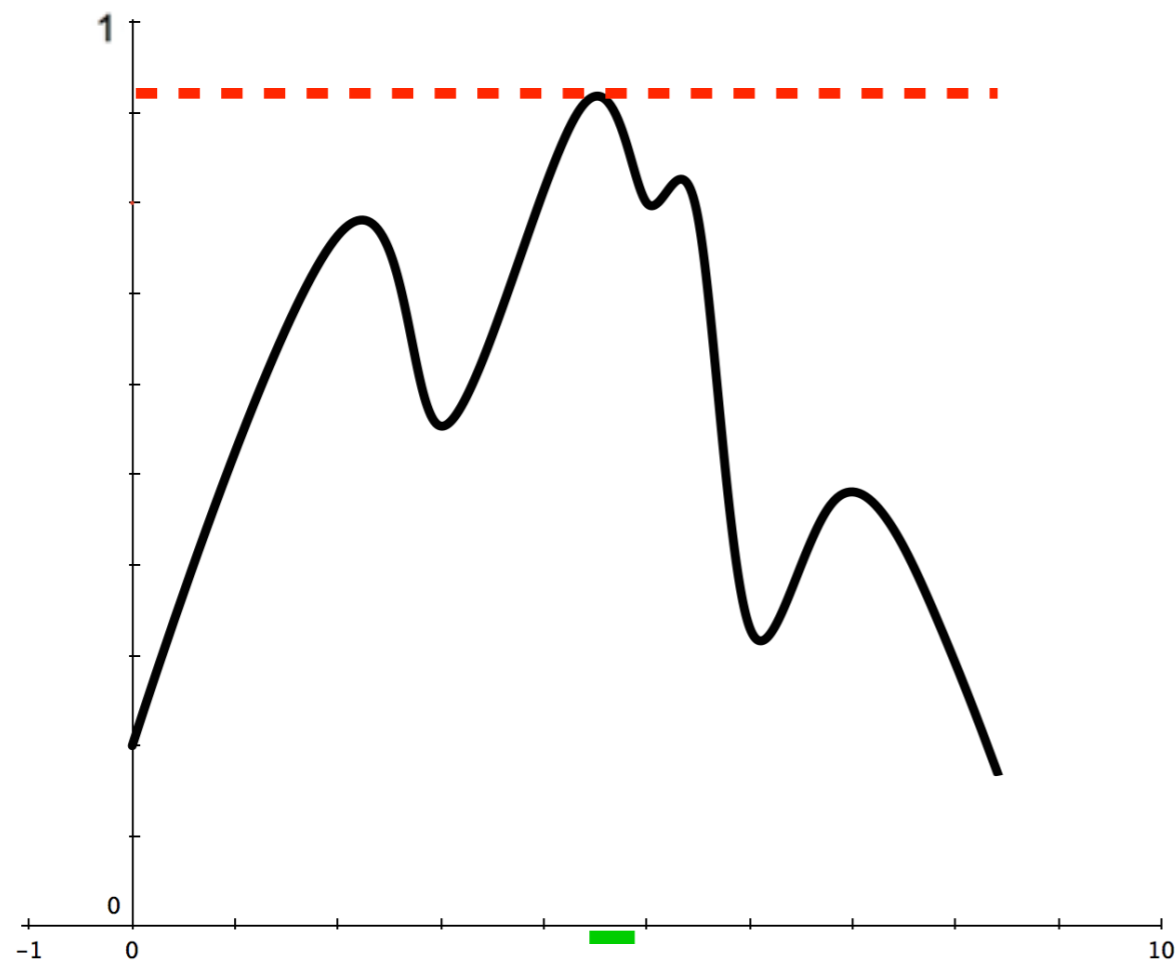
Persistent Homology

- For image segmentation, we borrow the concept of persistent homology to extract persistence regions and avoid noise.



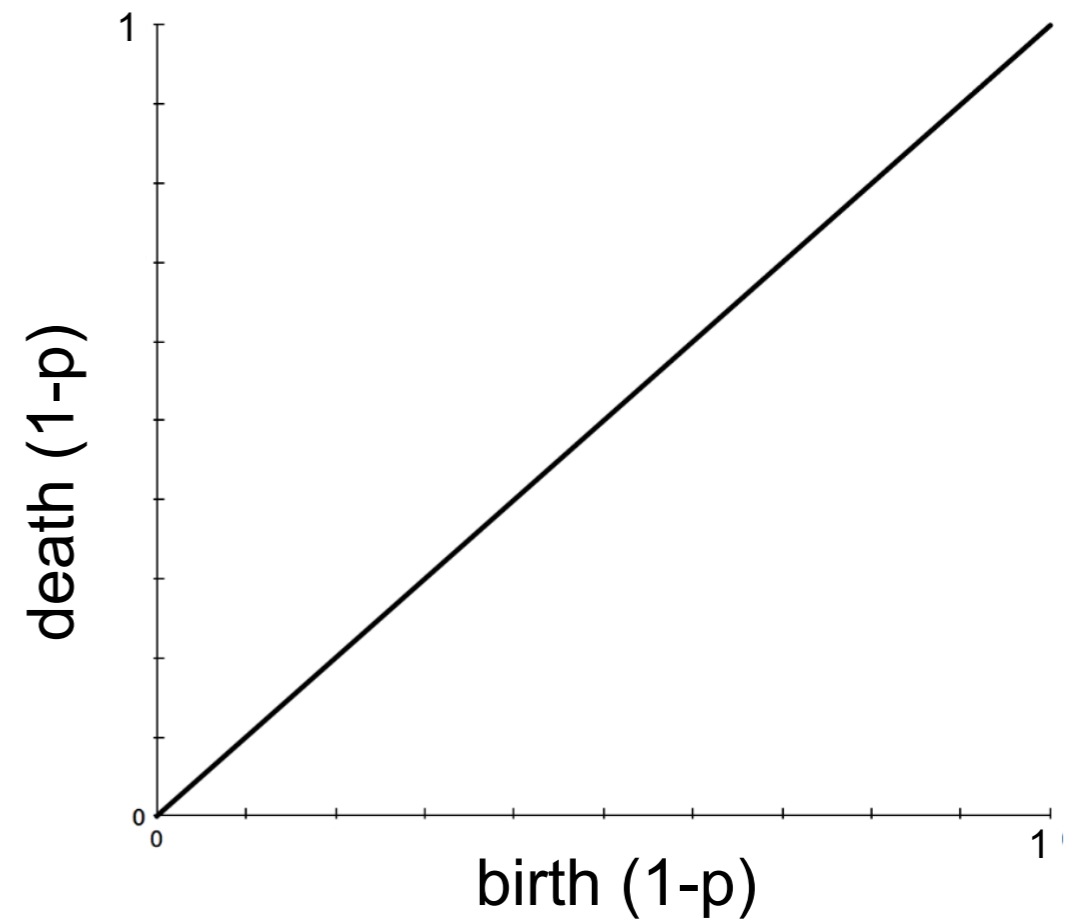
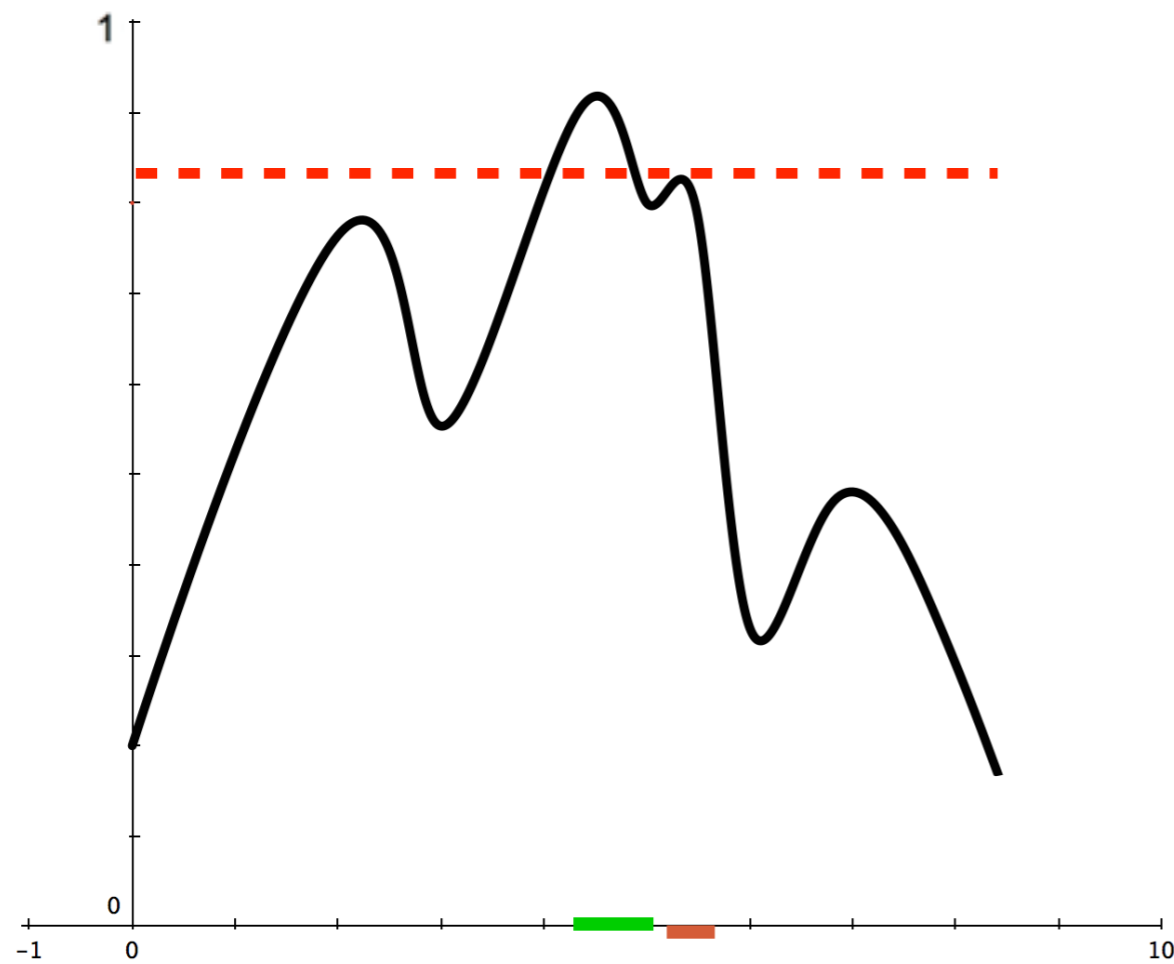
Persistent Homology

- Topological persistence



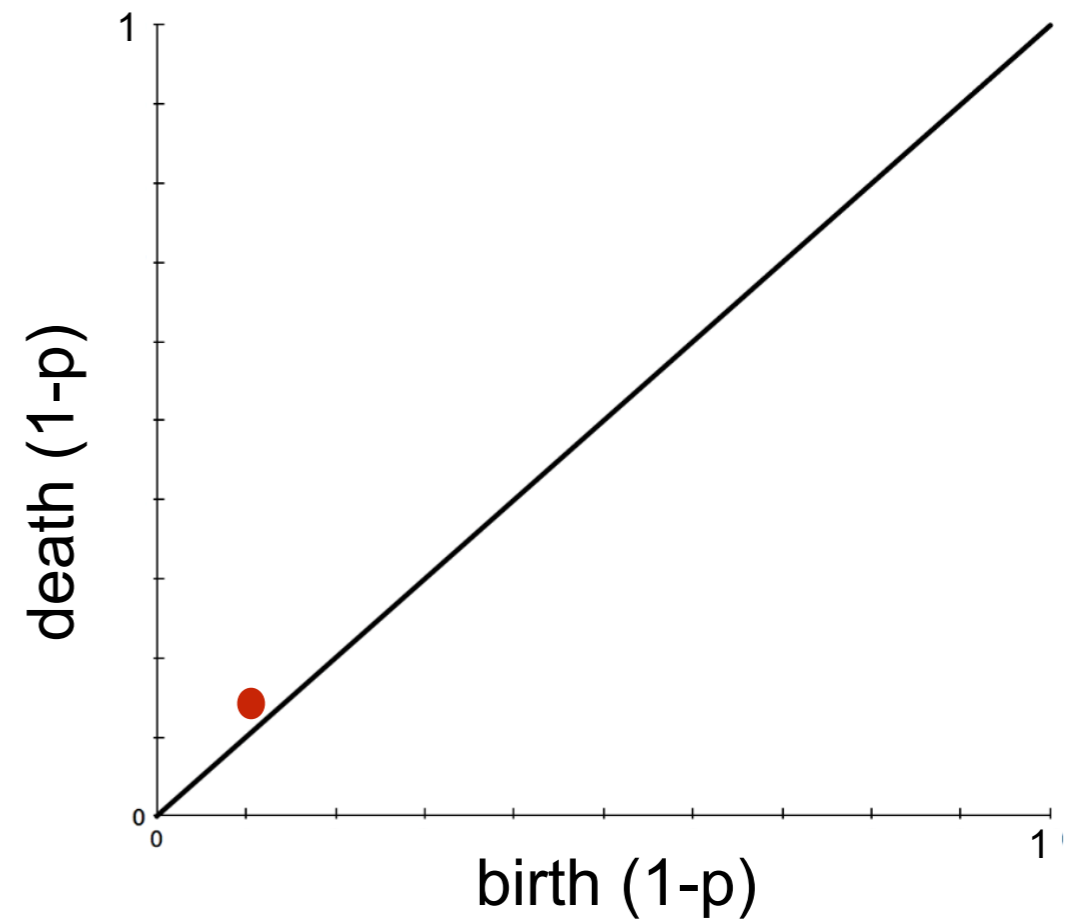
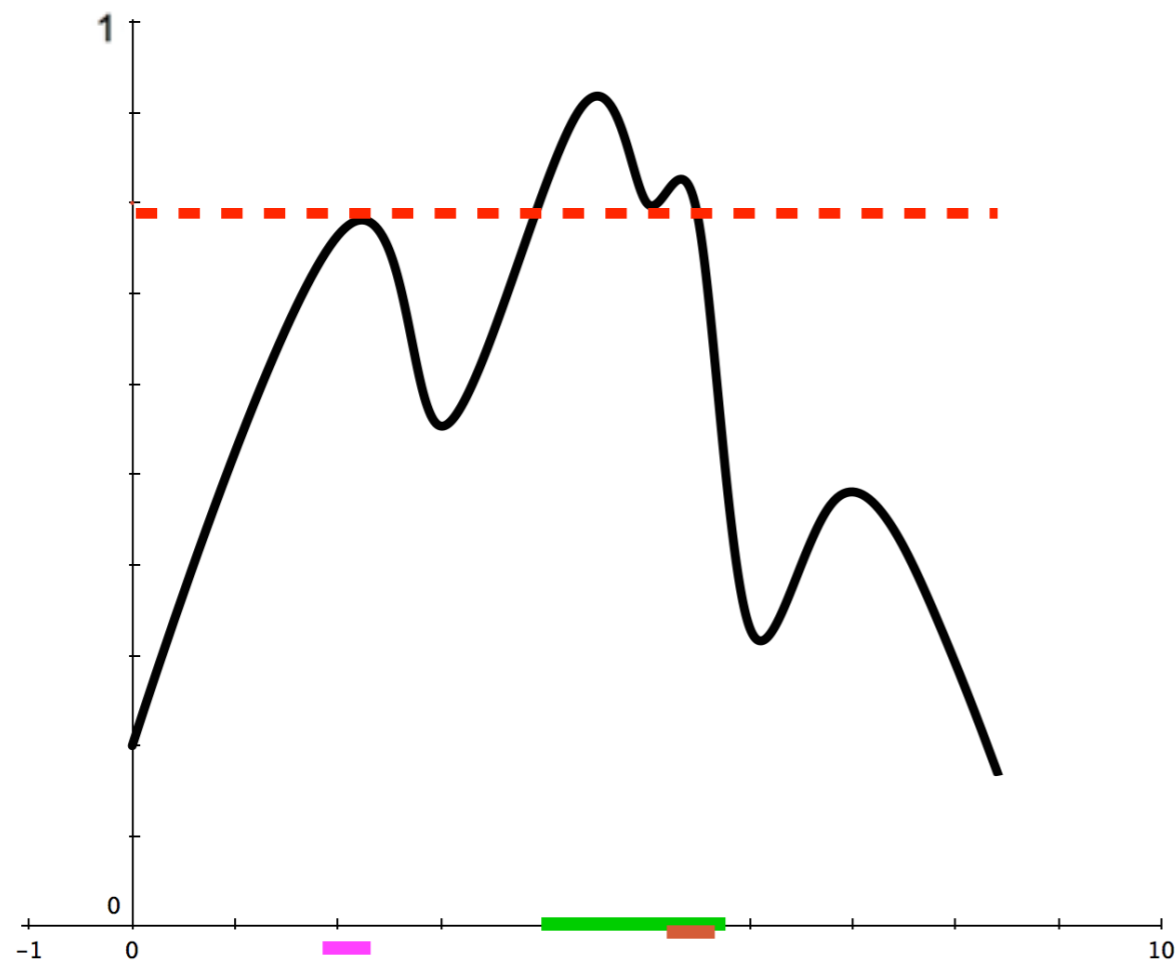
Persistent Homology

- Topological persistence



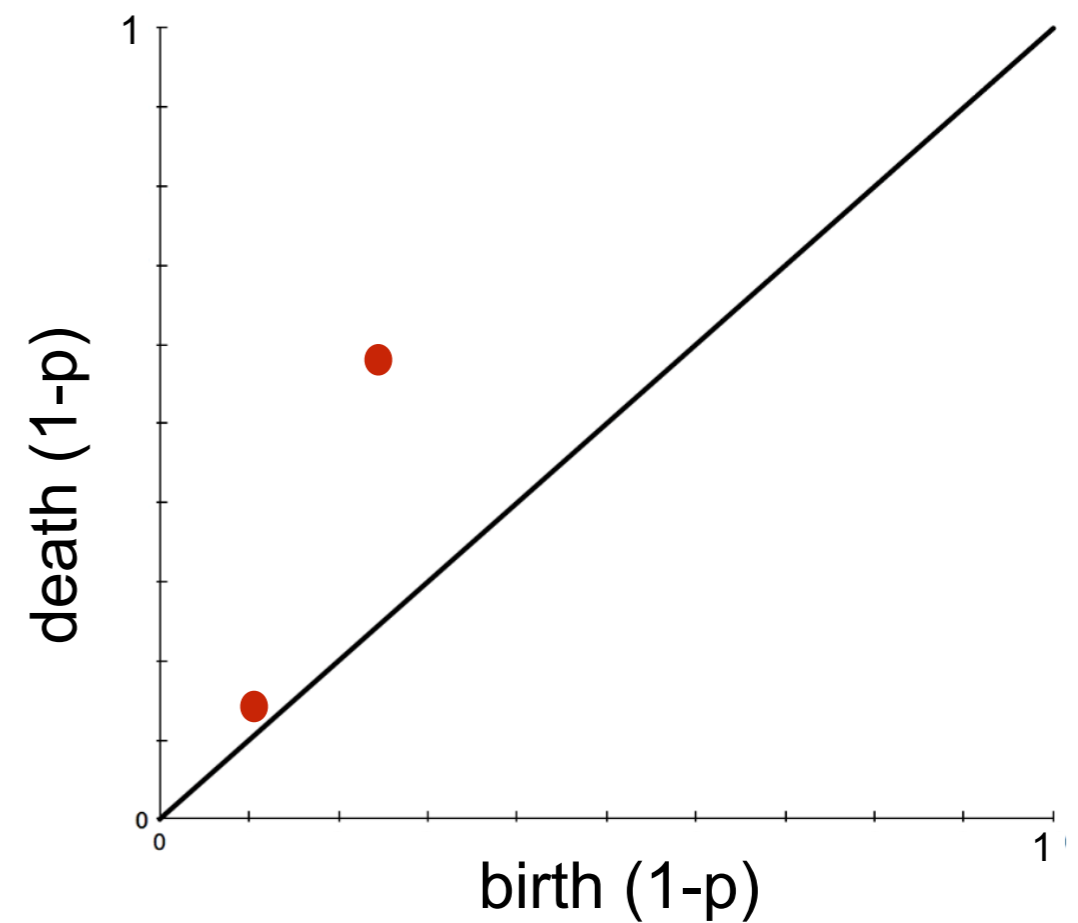
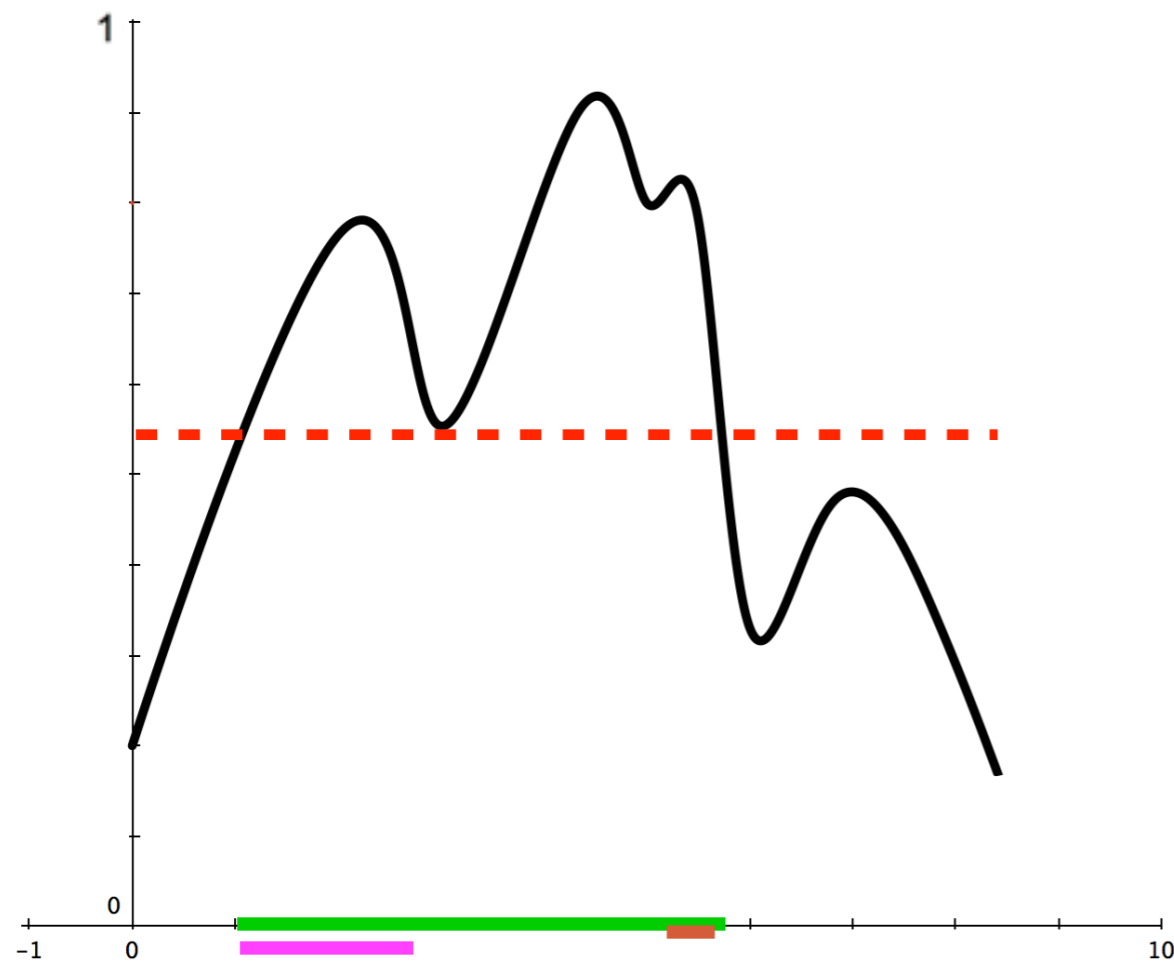
Persistent Homology

- Topological persistence



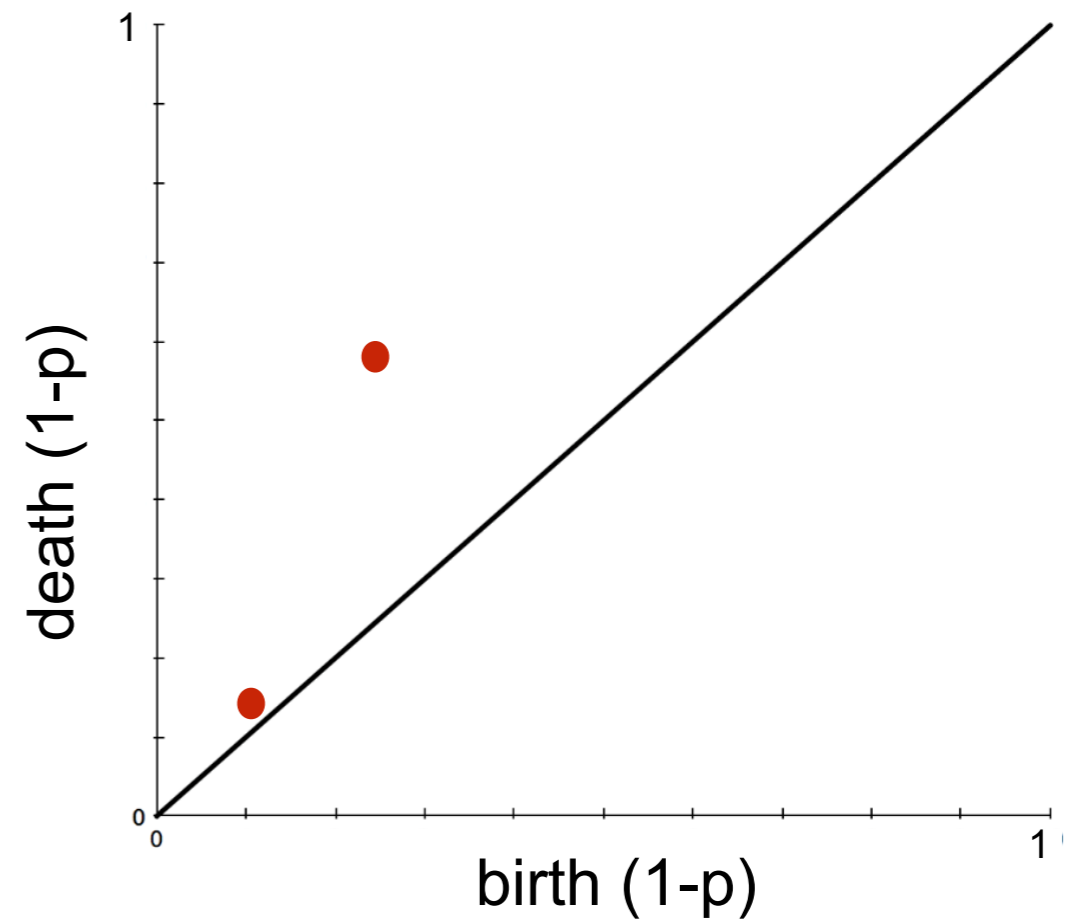
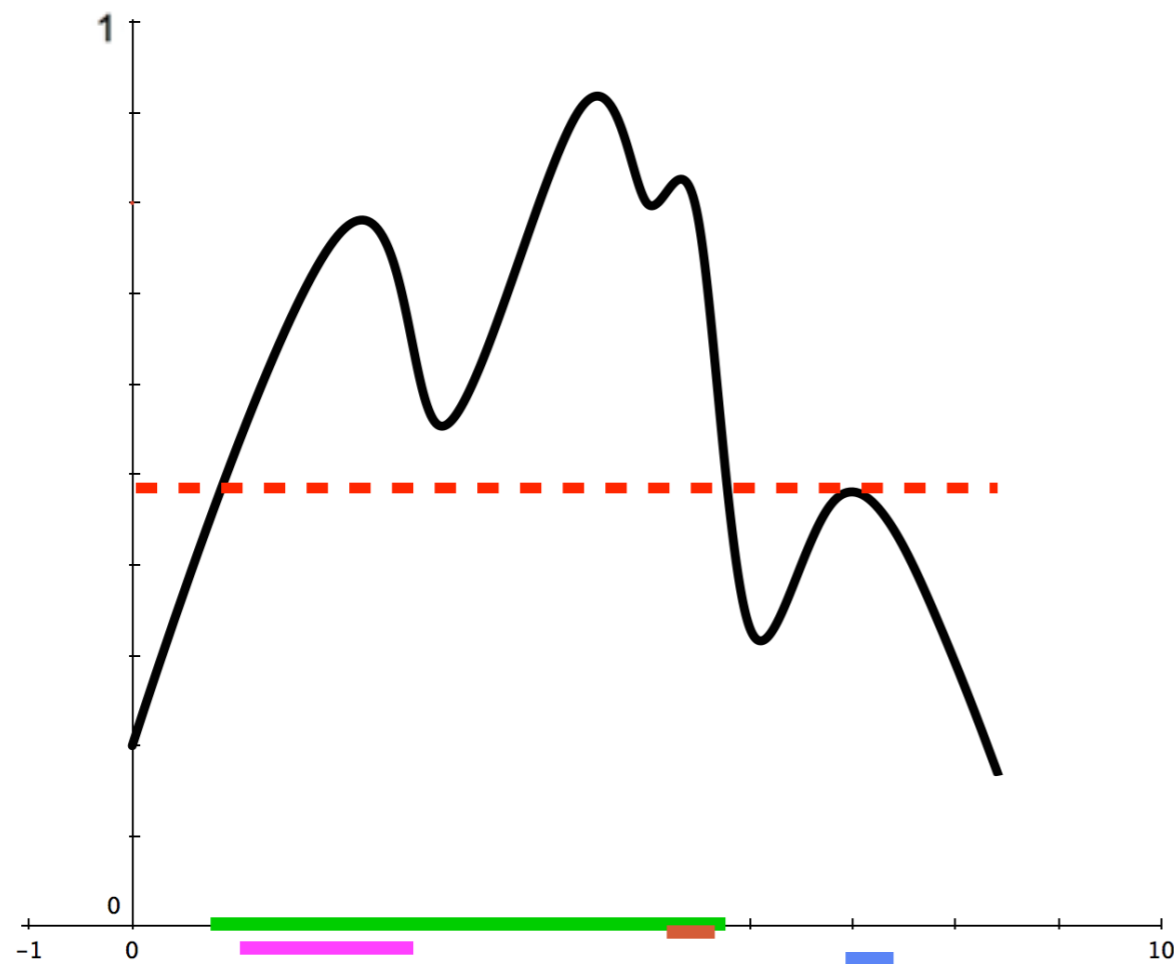
Persistent Homology

- Topological persistence



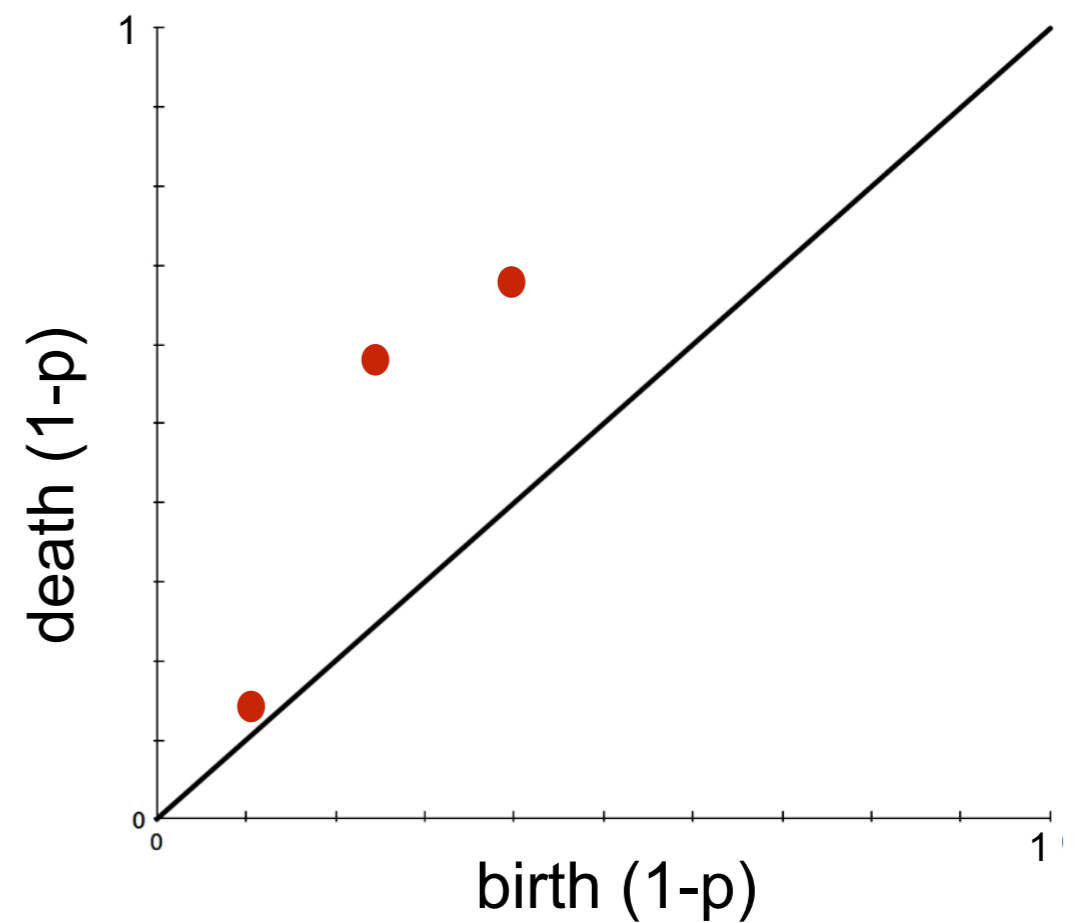
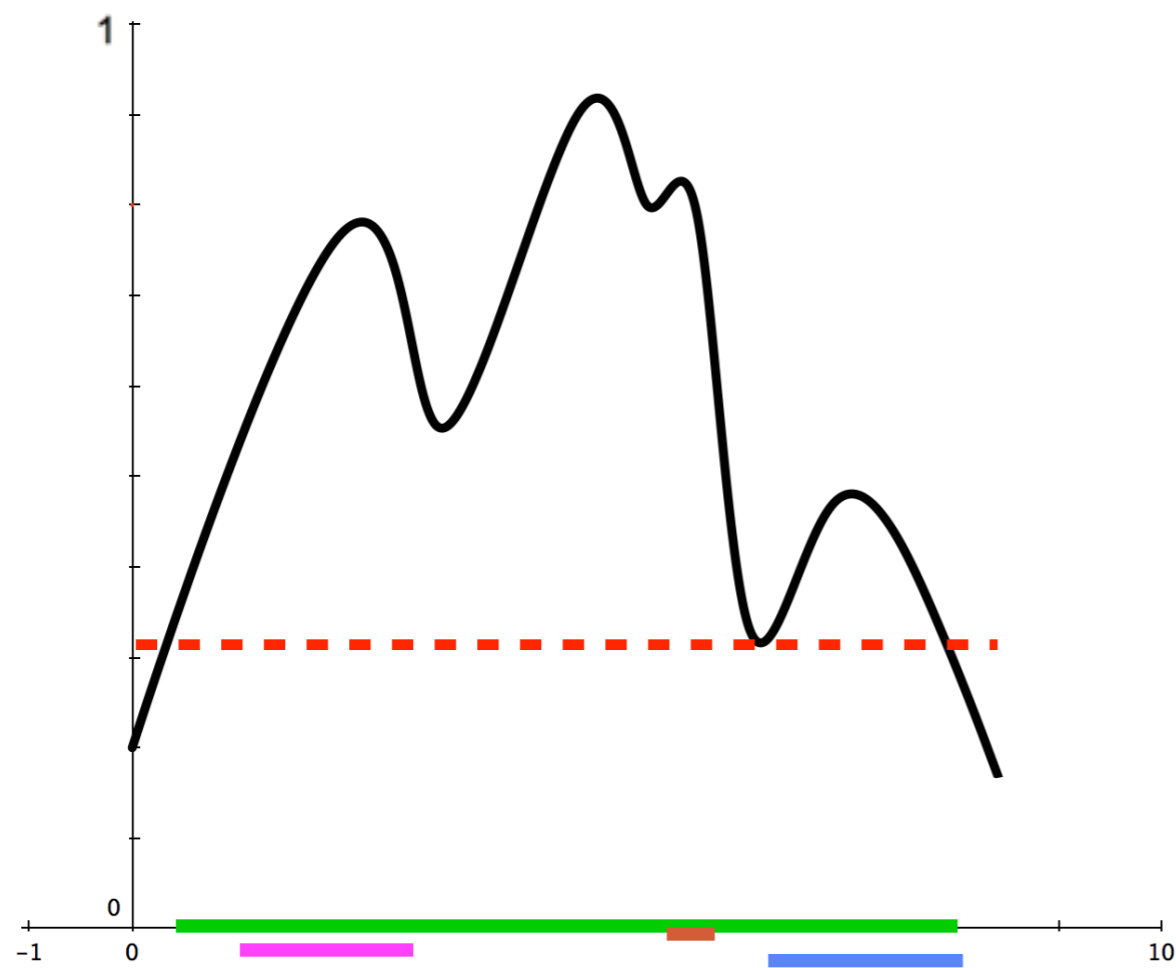
Persistent Homology

- Topological persistence



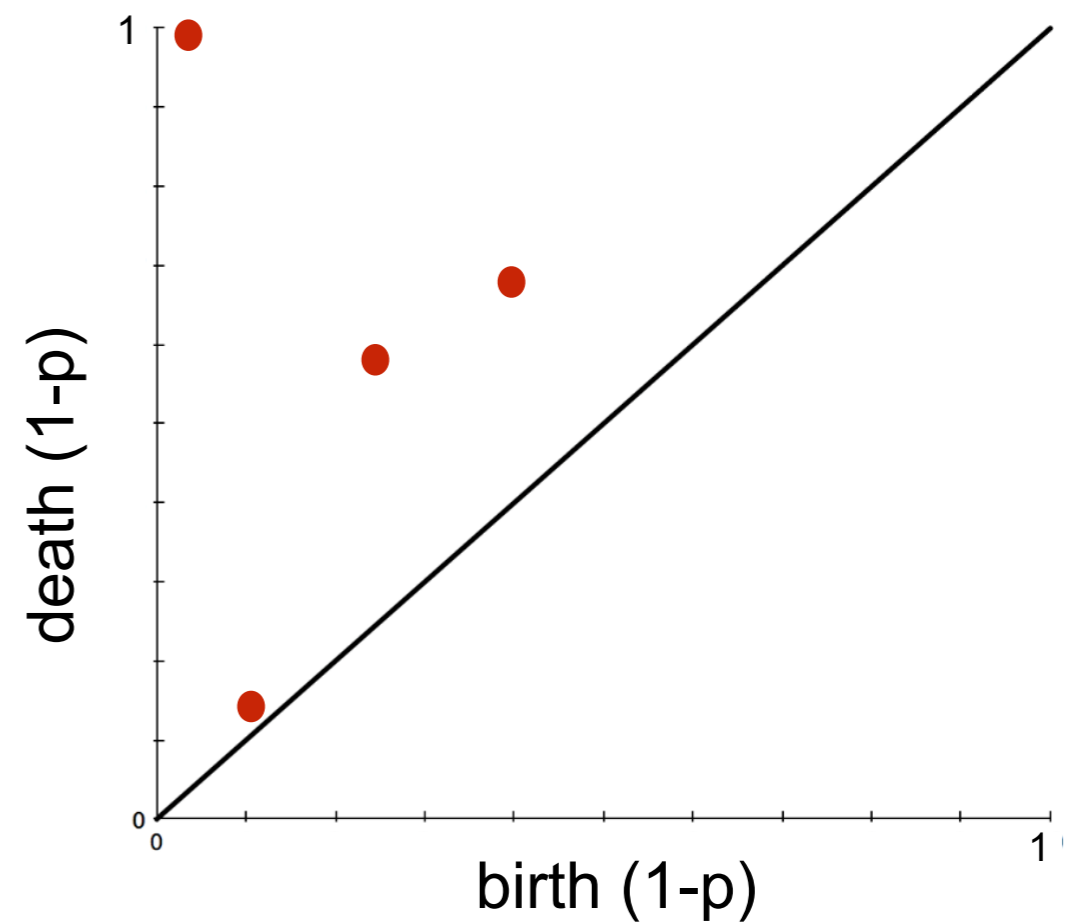
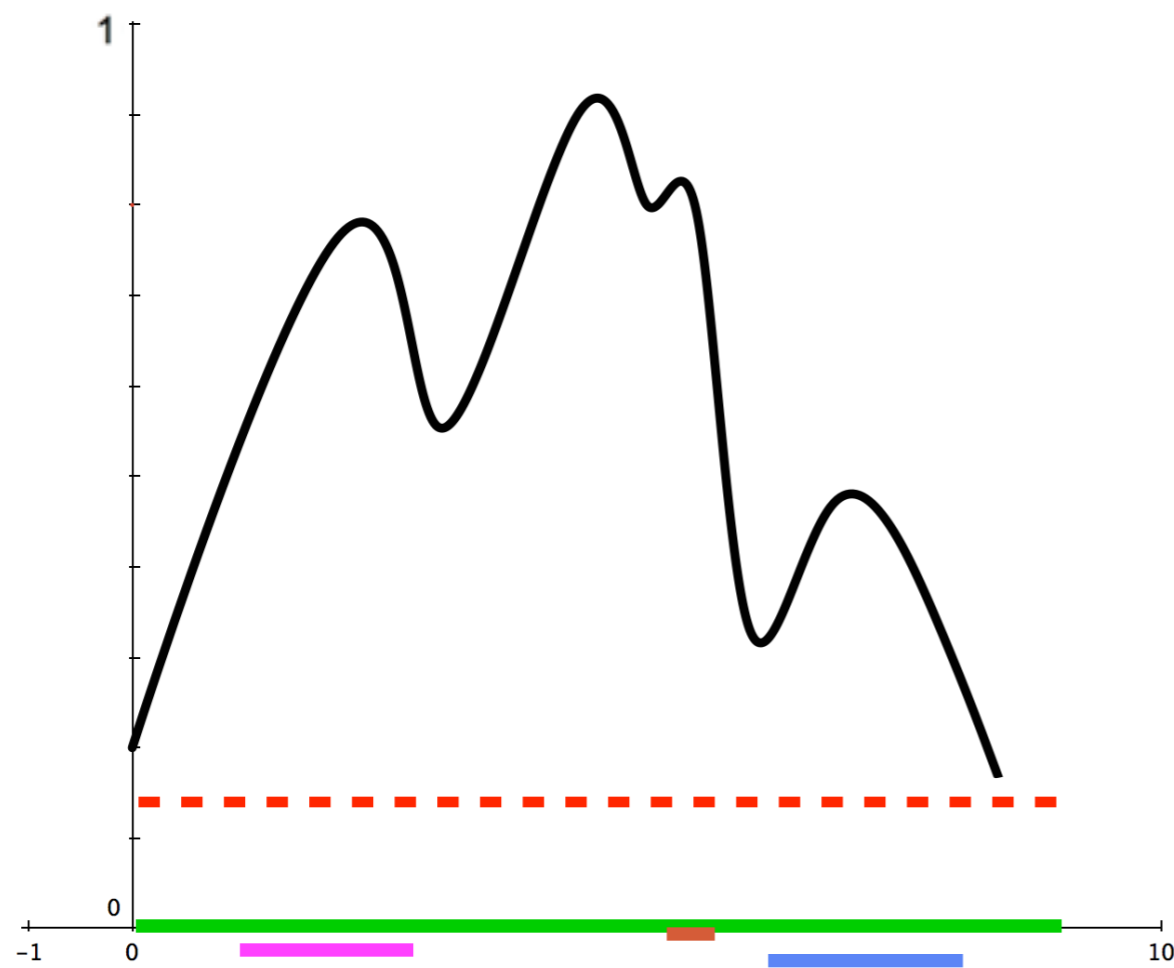
Persistent Homology

- Topological persistence



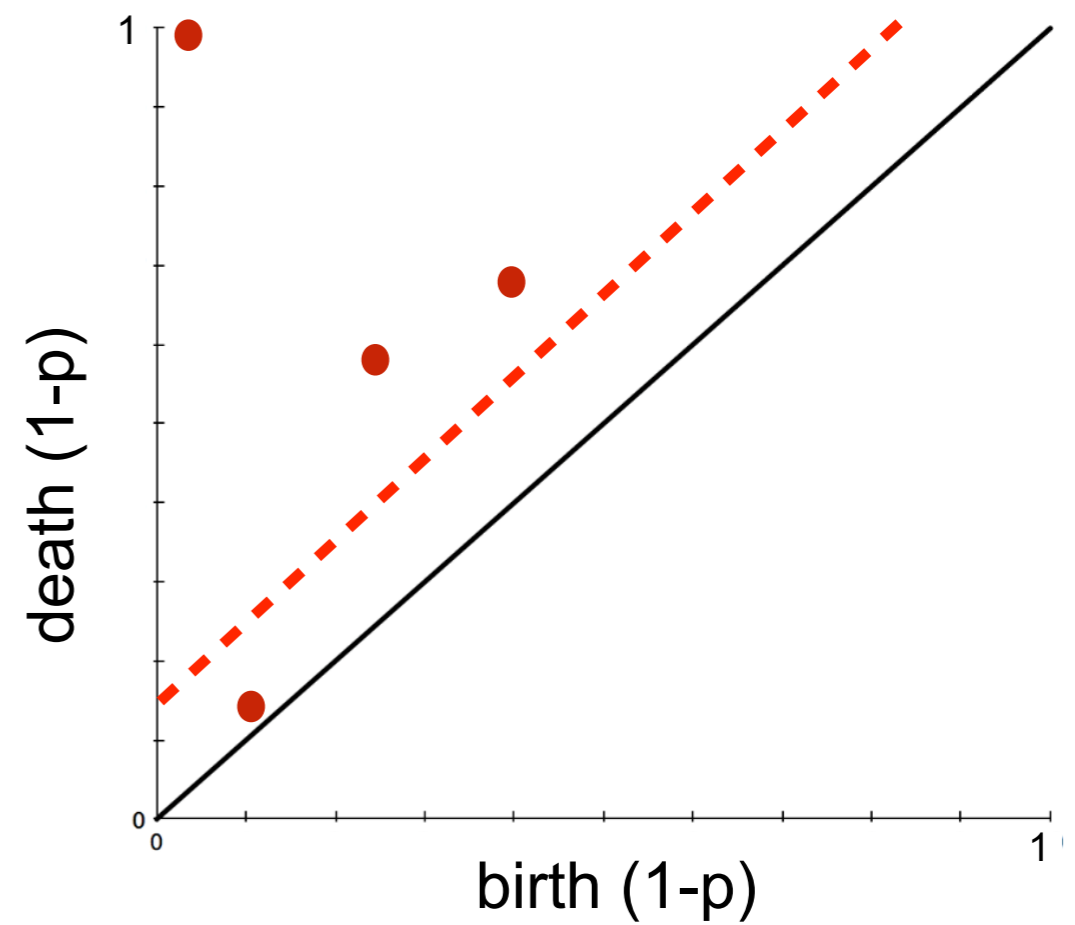
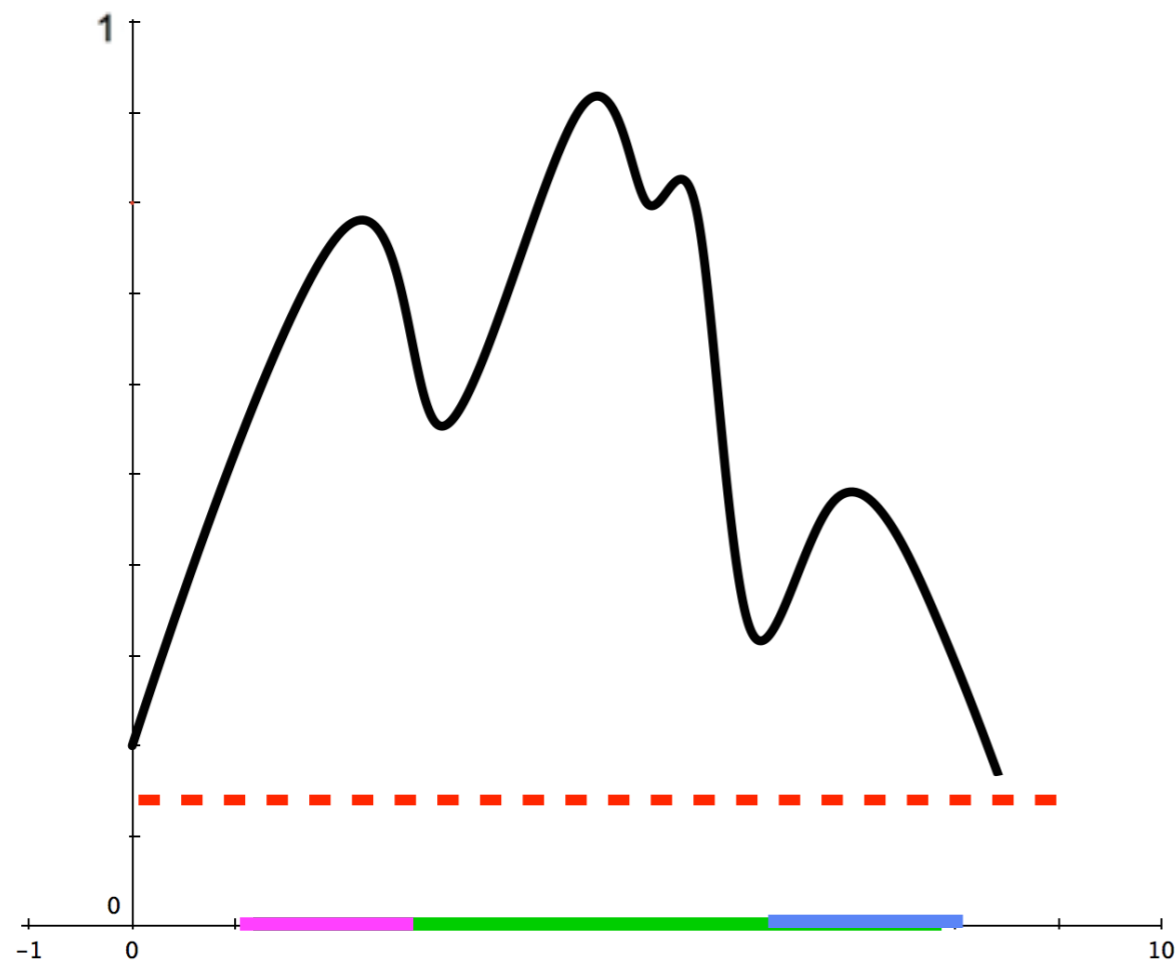
Persistent Homology

- Topological persistence



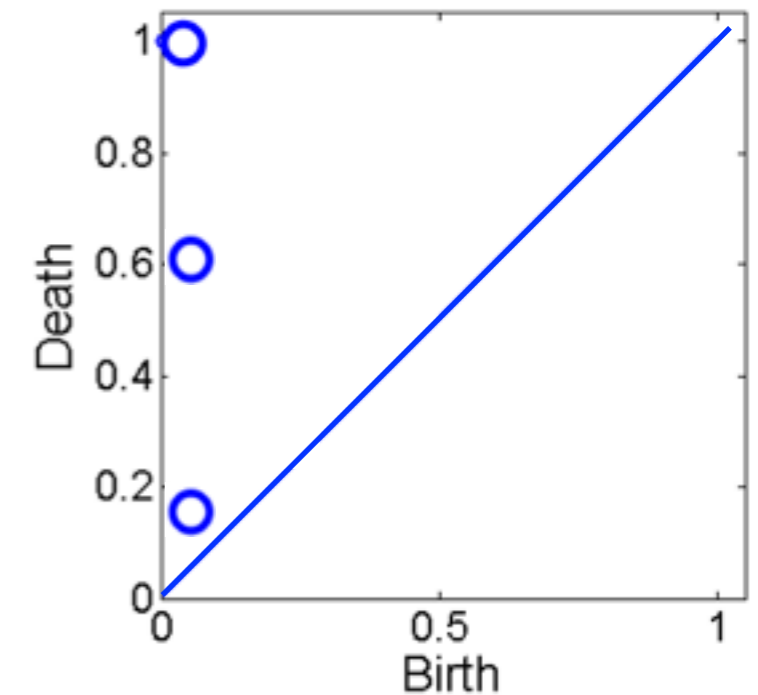
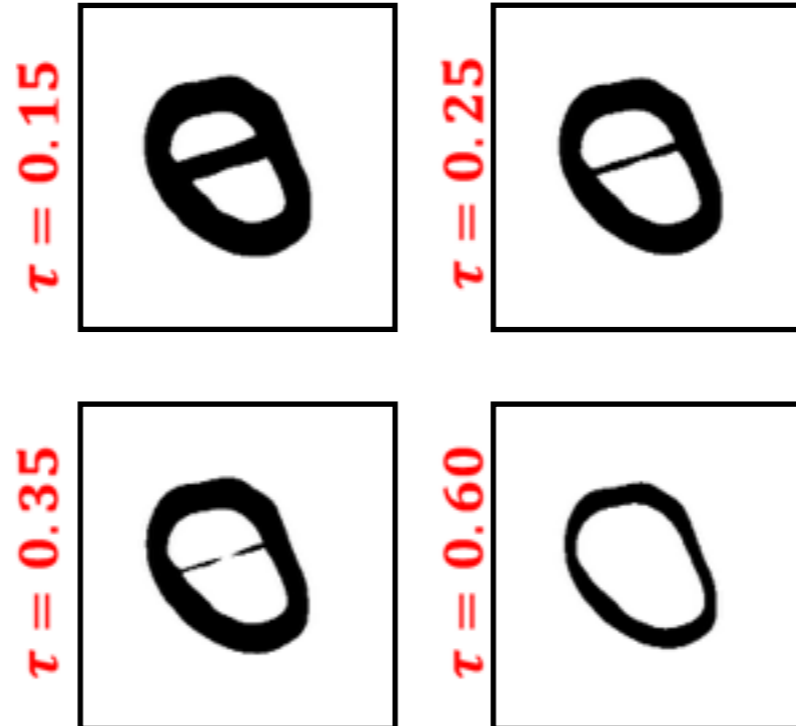
Persistent Homology

- Topological persistence



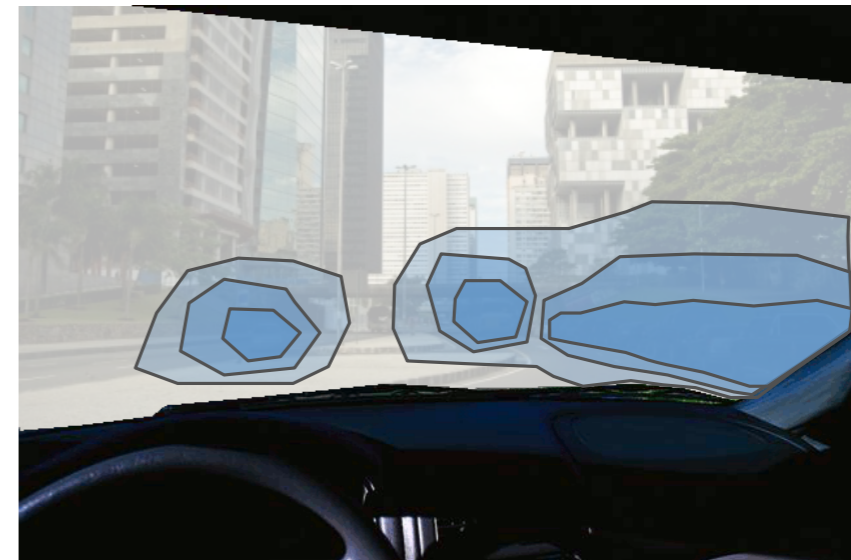
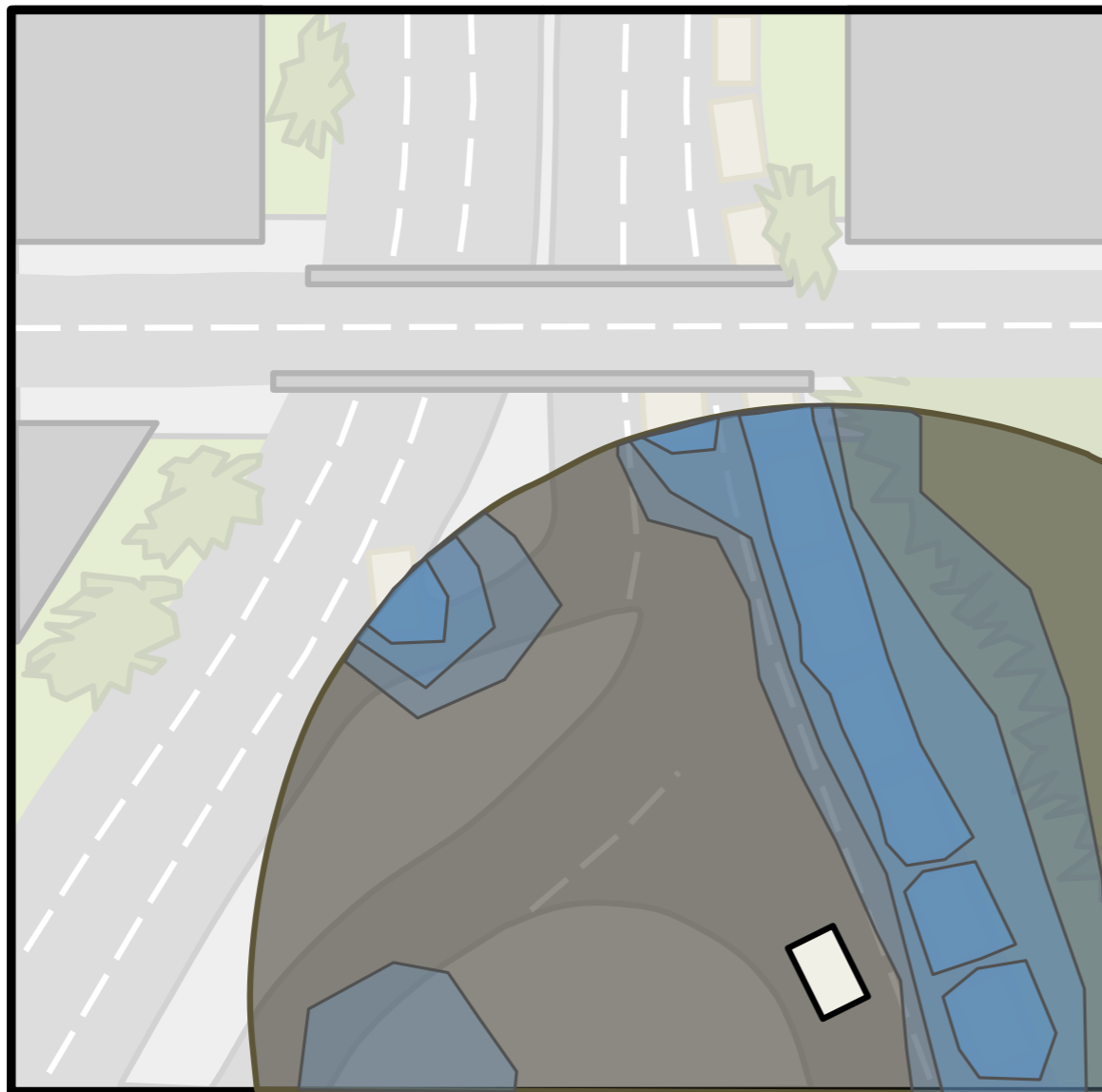
Persistent Homology

- Topological persistence

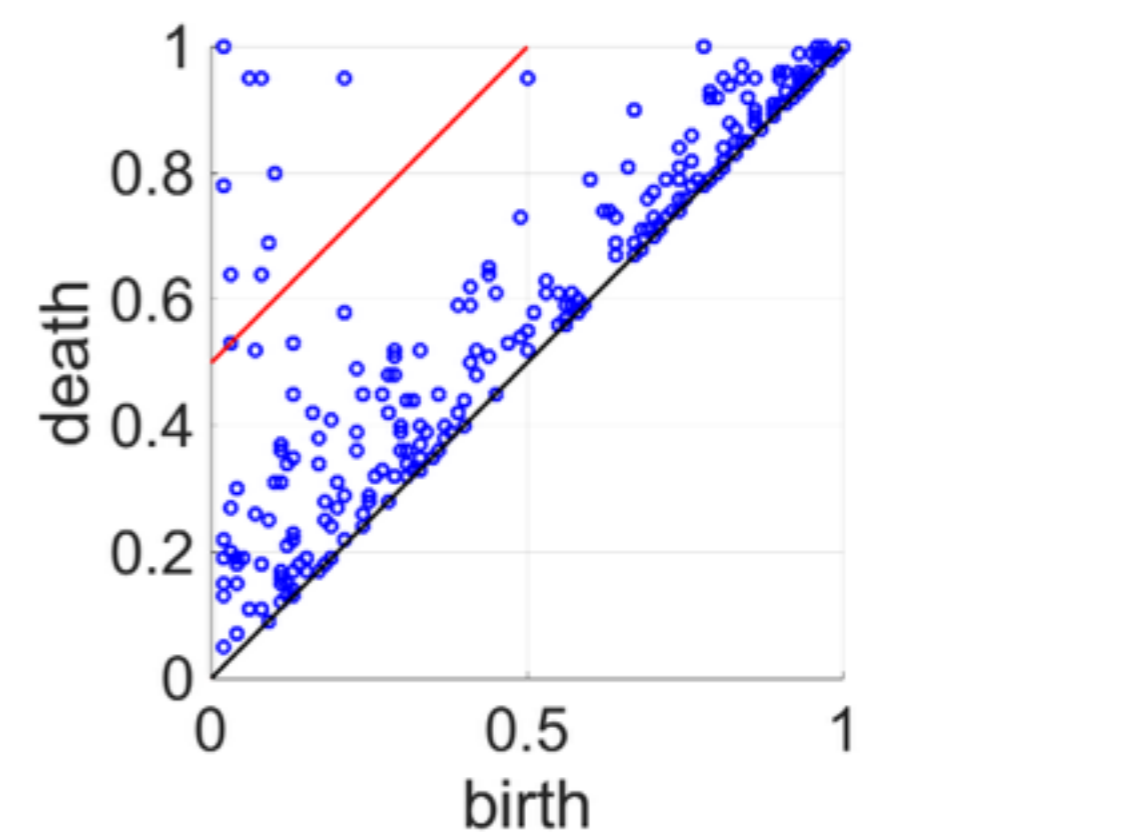
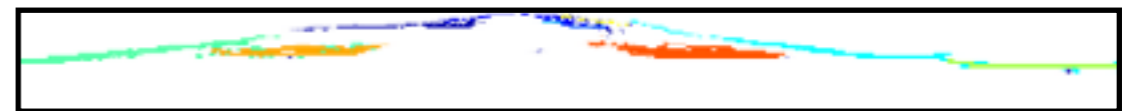
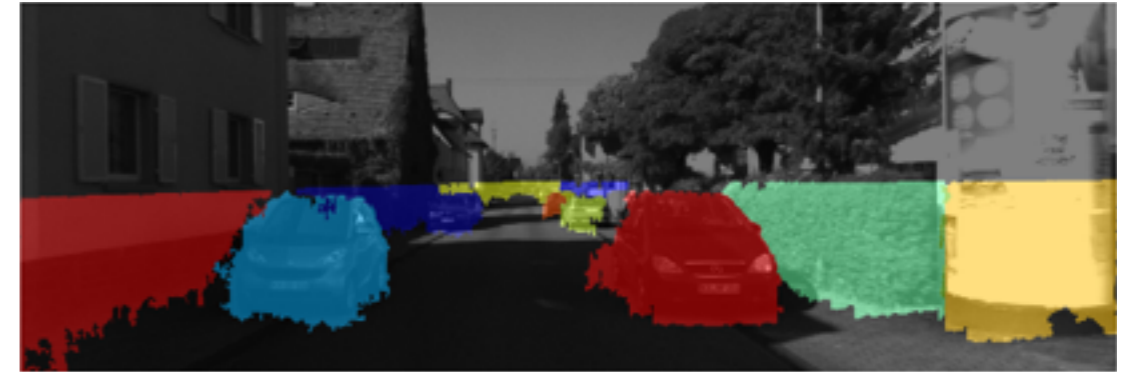
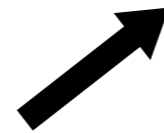
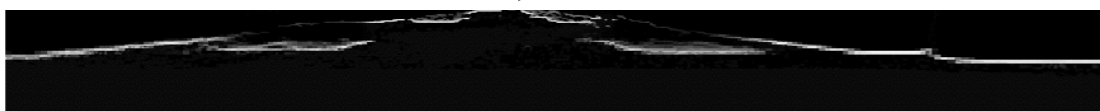


Obstacle Segmentation of Outdoor Scene

- **Vision system for autonomous driving**

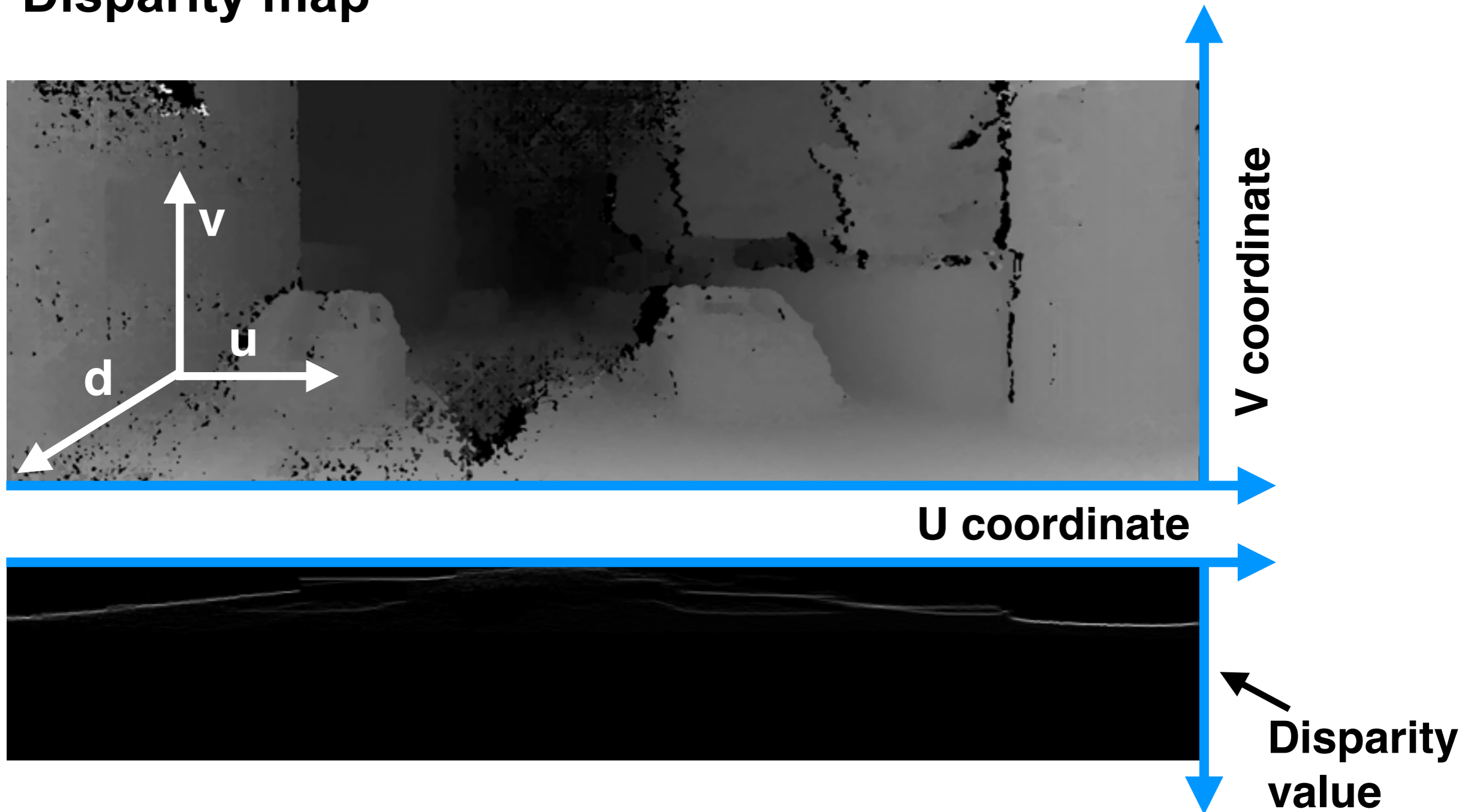


Obstacle Segmentation of Outdoor Scene



Obstacle Segmentation of Outdoor Scene

- Disparity map



Obstacle Segmentation of Outdoor Scene

- **Ground Segmentation**



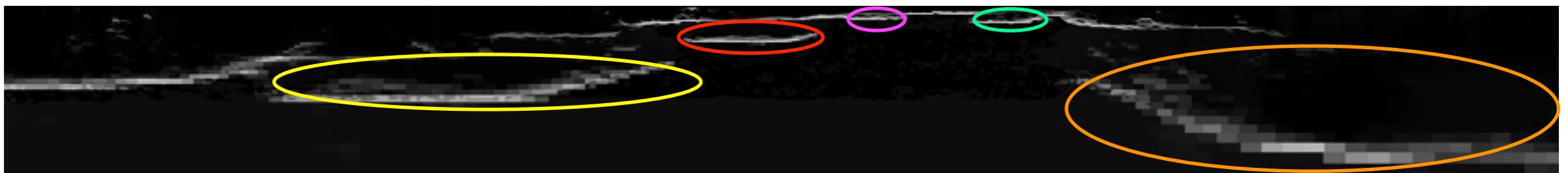
Obstacle Segmentation of Outdoor Scene

- Occupancy computation



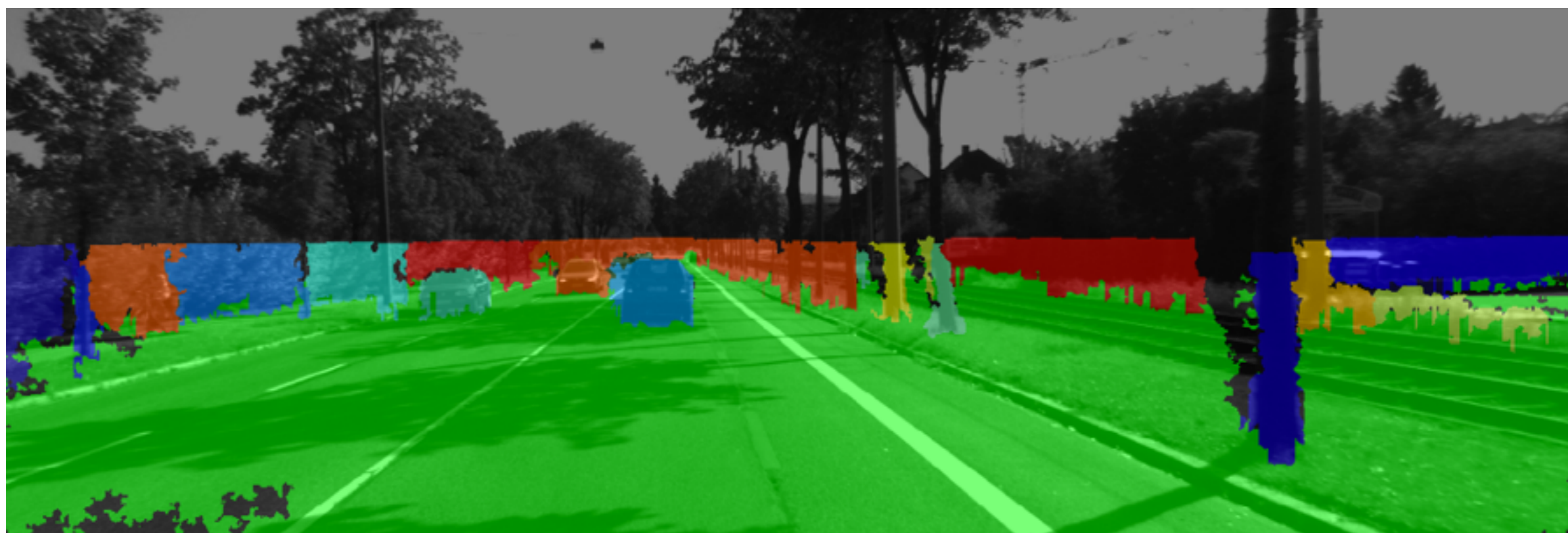
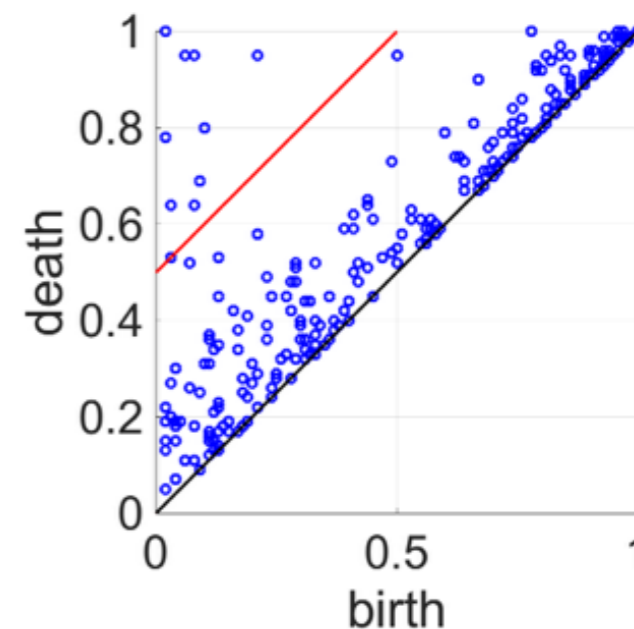
Obstacle Segmentation of Outdoor Scene

- Occupancy computation



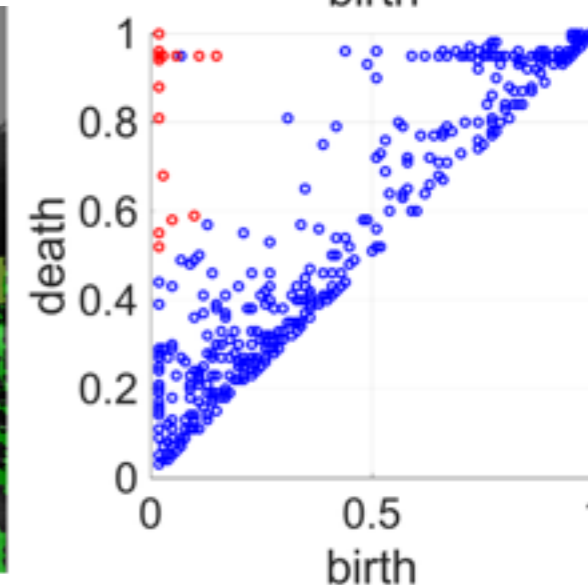
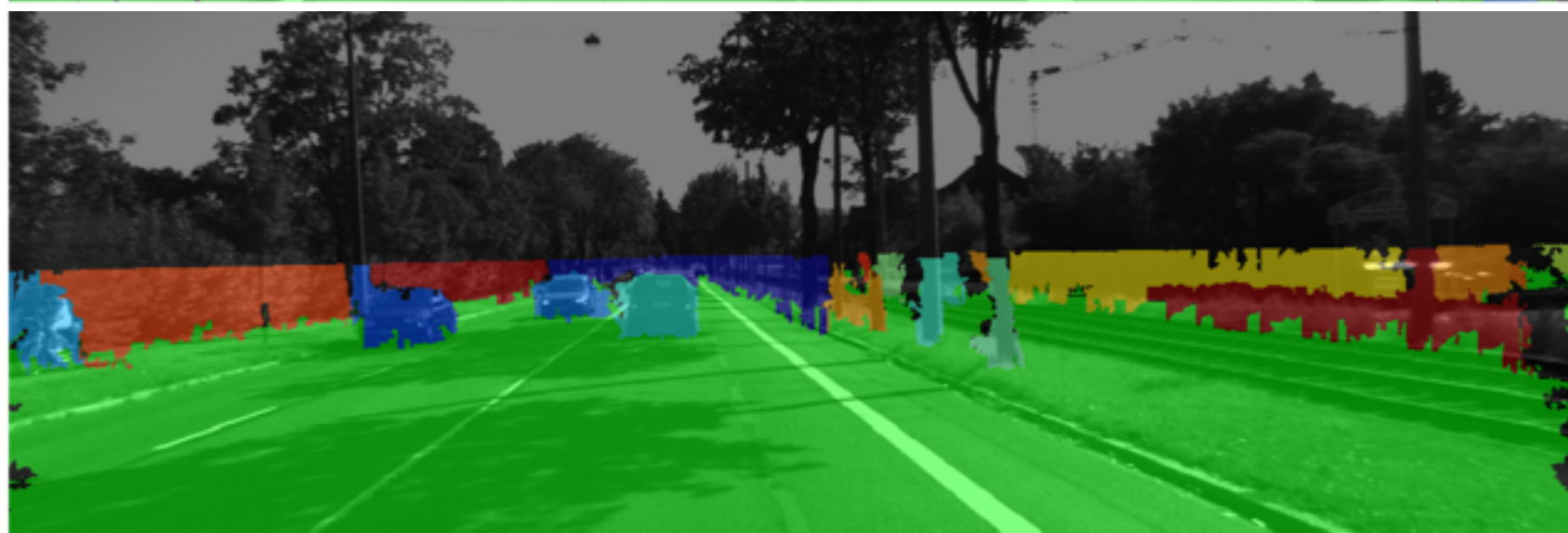
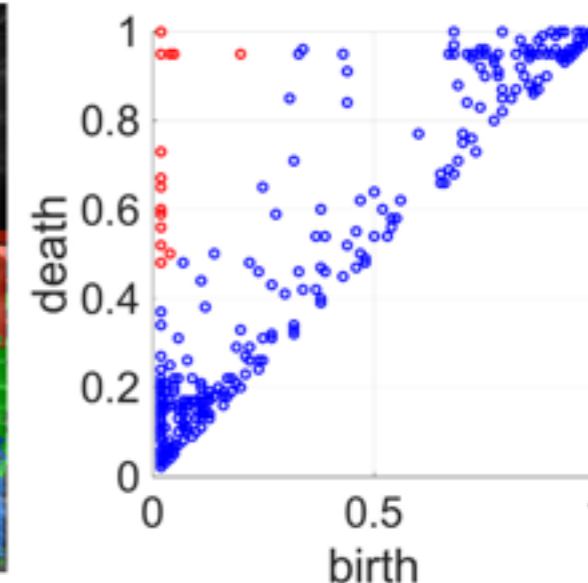
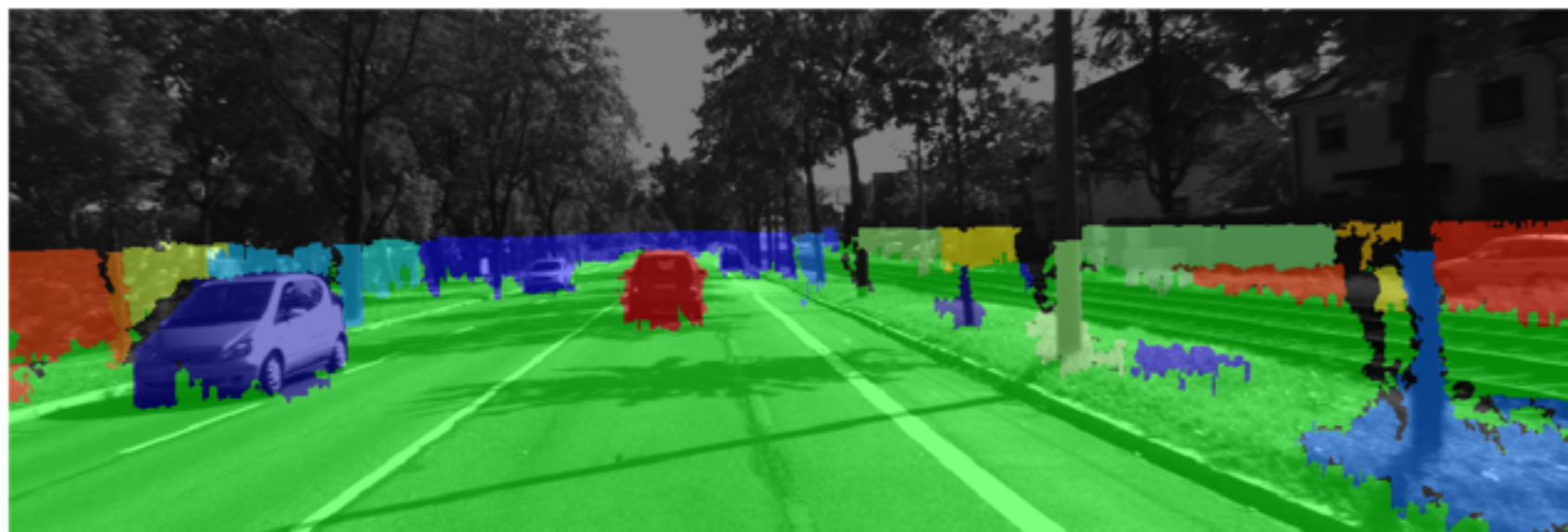
Obstacle Segmentation of Outdoor Scene

- Persistence region extraction



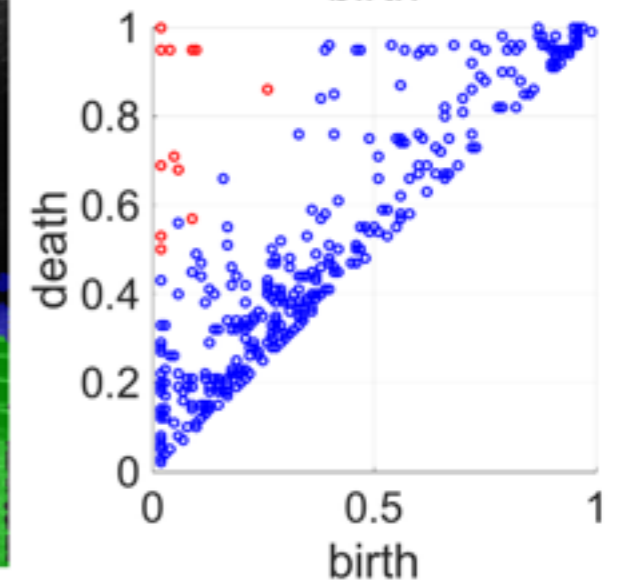
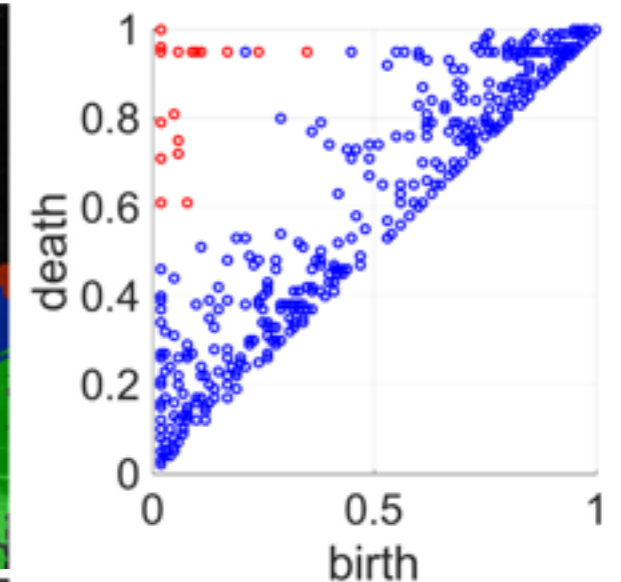
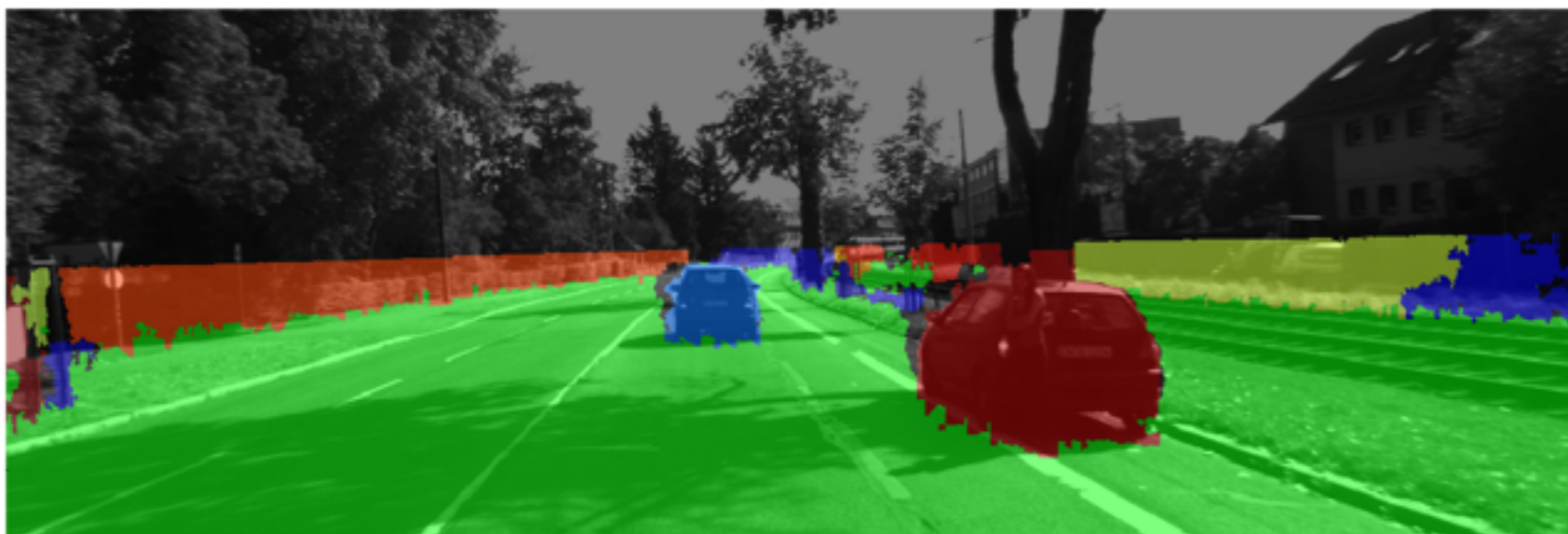
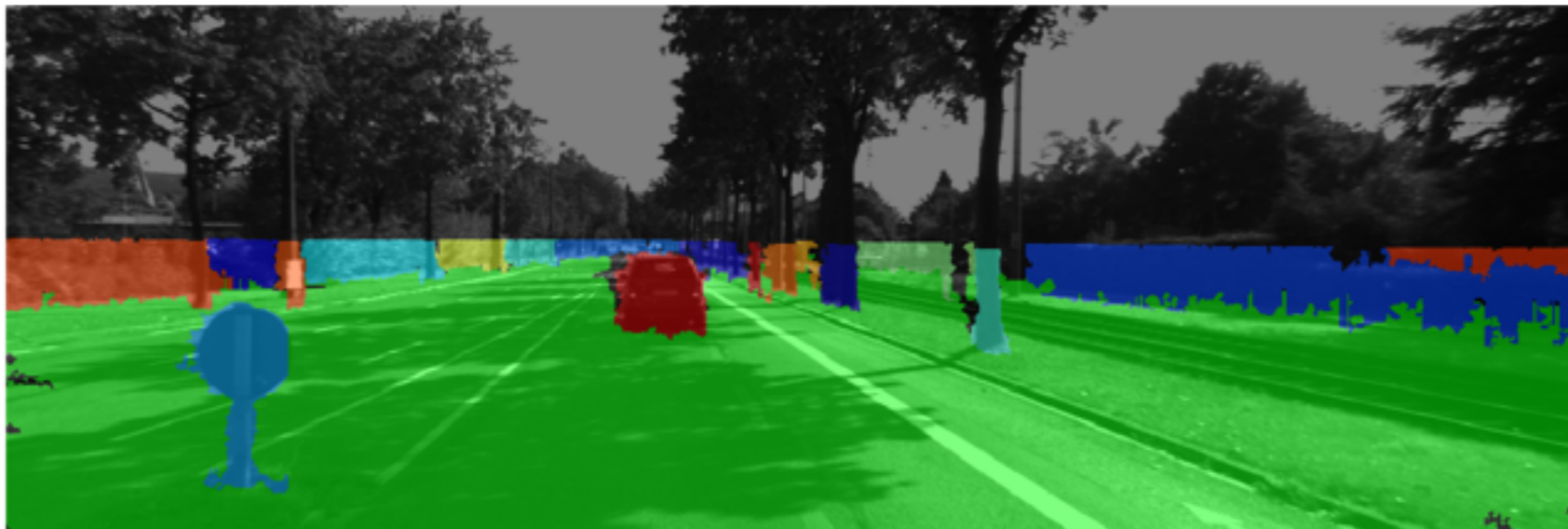
Obstacle Segmentation of Outdoor Scene

- **Experiment**
 - **Dataset - KITTI Vision Benchmark Suite**
 - **Persistence threshold = 0.45**



Obstacle Segmentation of Outdoor Scene

- **Experiment**
 - Dataset - KITTI Vision Benchmark Suite
 - Persistence threshold = 0.45



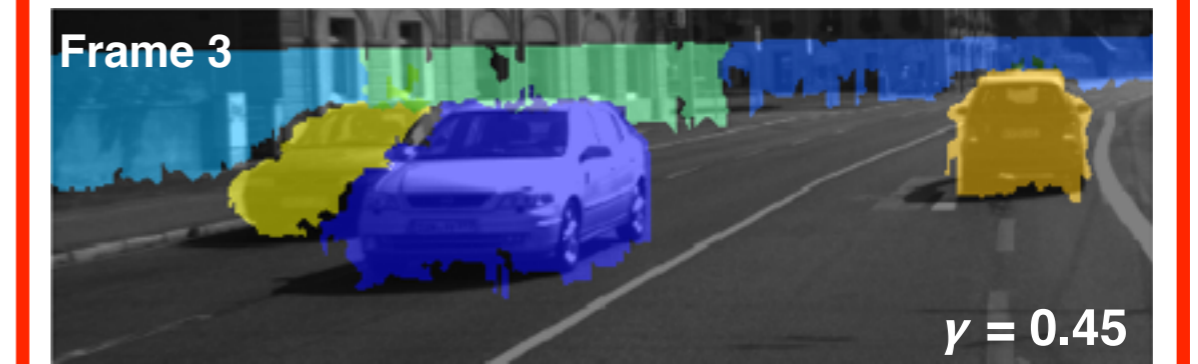
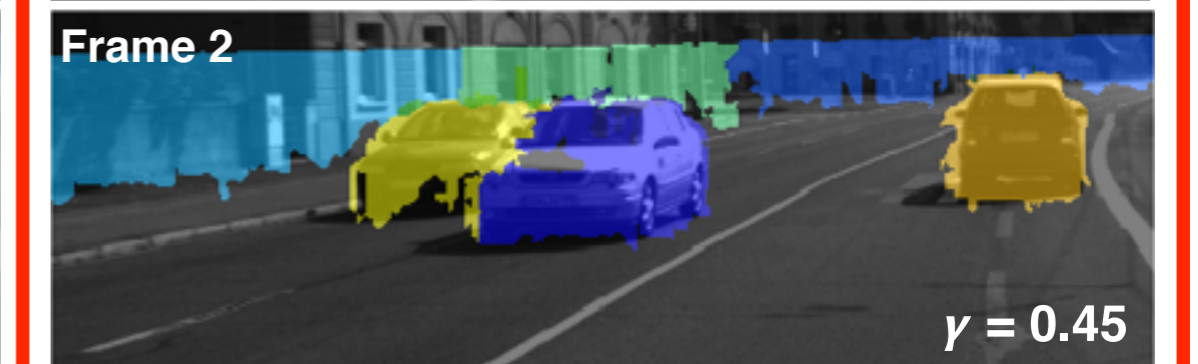
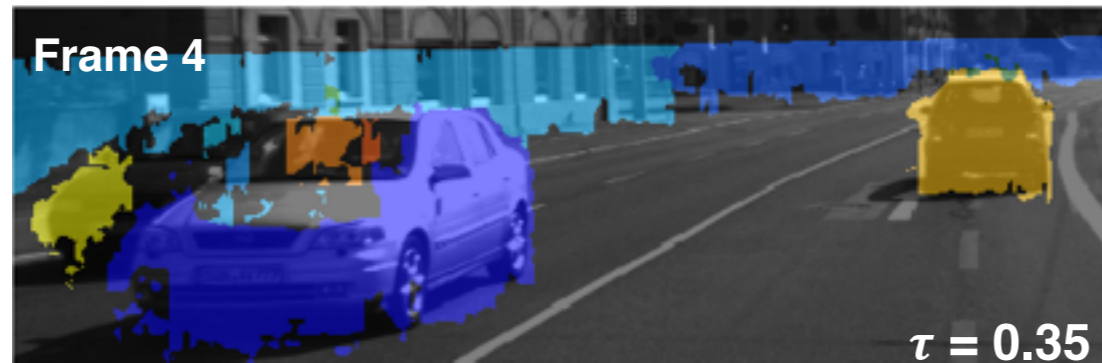
Obstacle Segmentation of Outdoor Scene

- Experiment - Compare with simple thresholding
 - Changing thresholding parameters

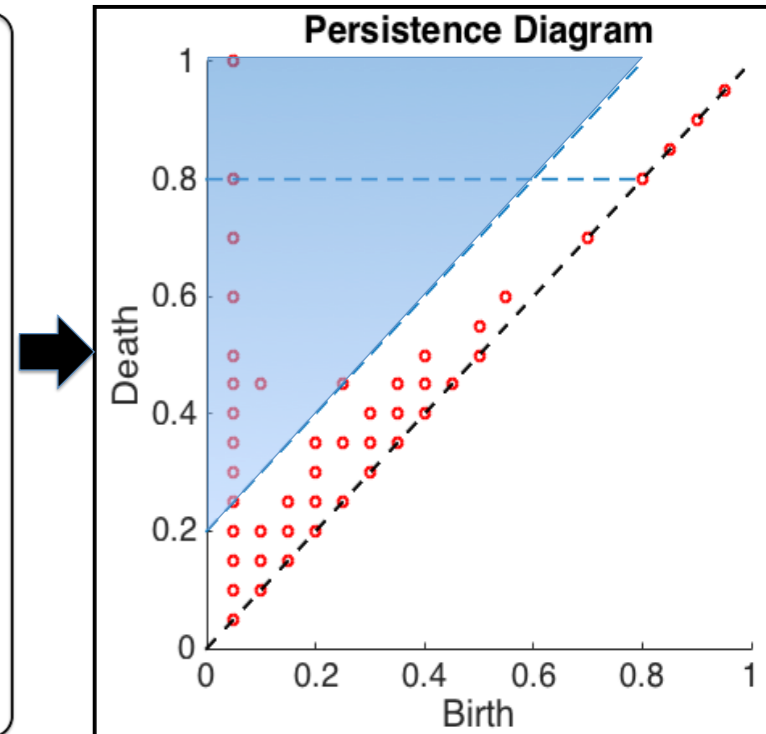
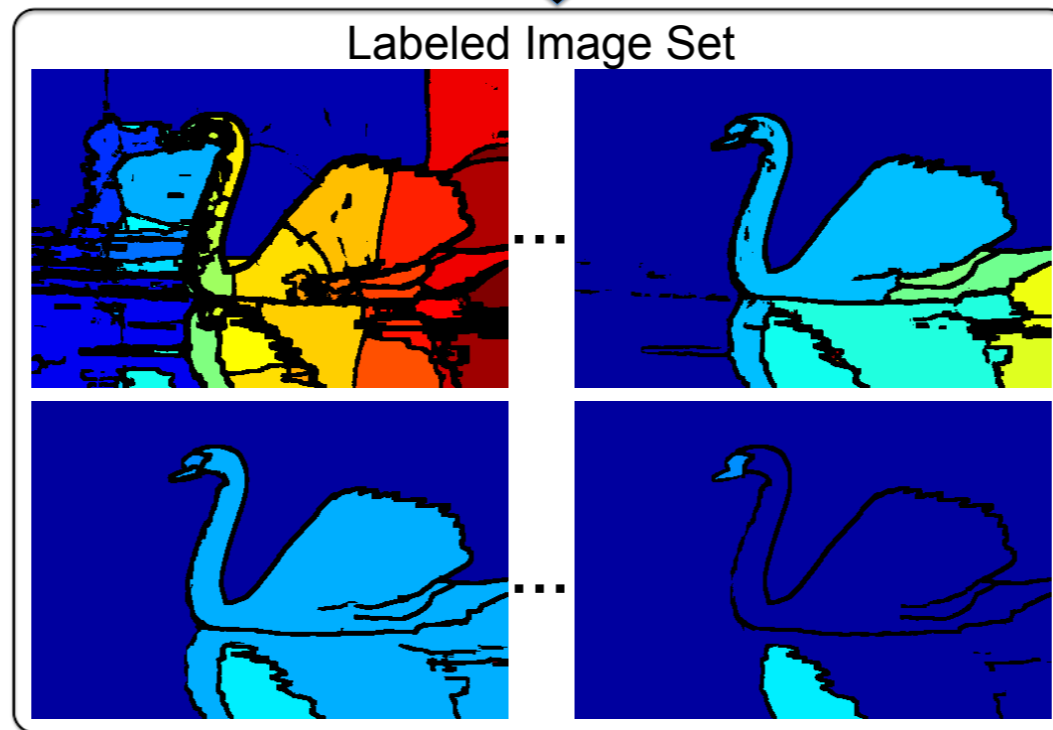
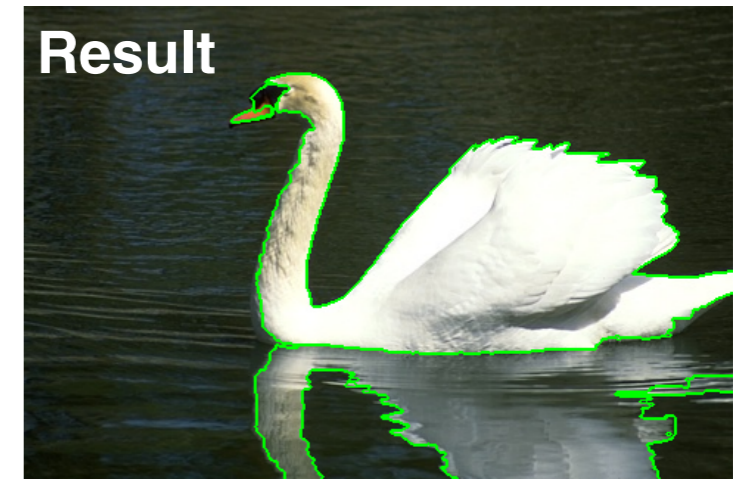
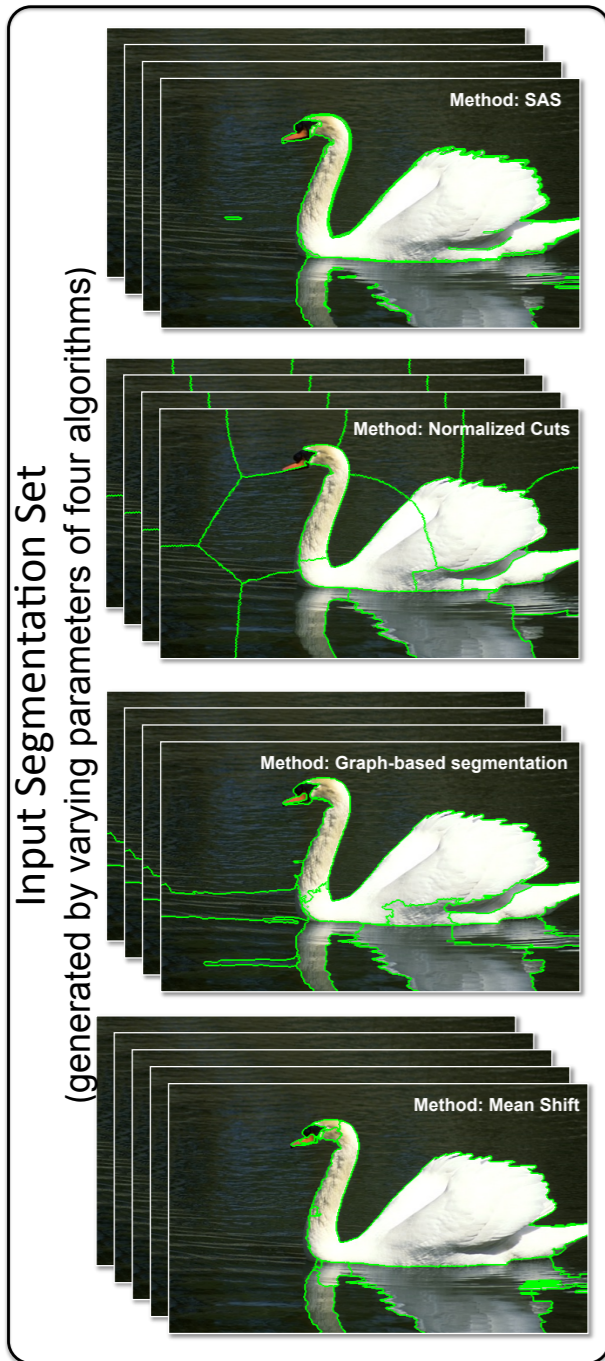


Obstacle Segmentation of Outdoor Scene

- Experiment - Compare with simple thresholding
 - Changing images with the same threshold

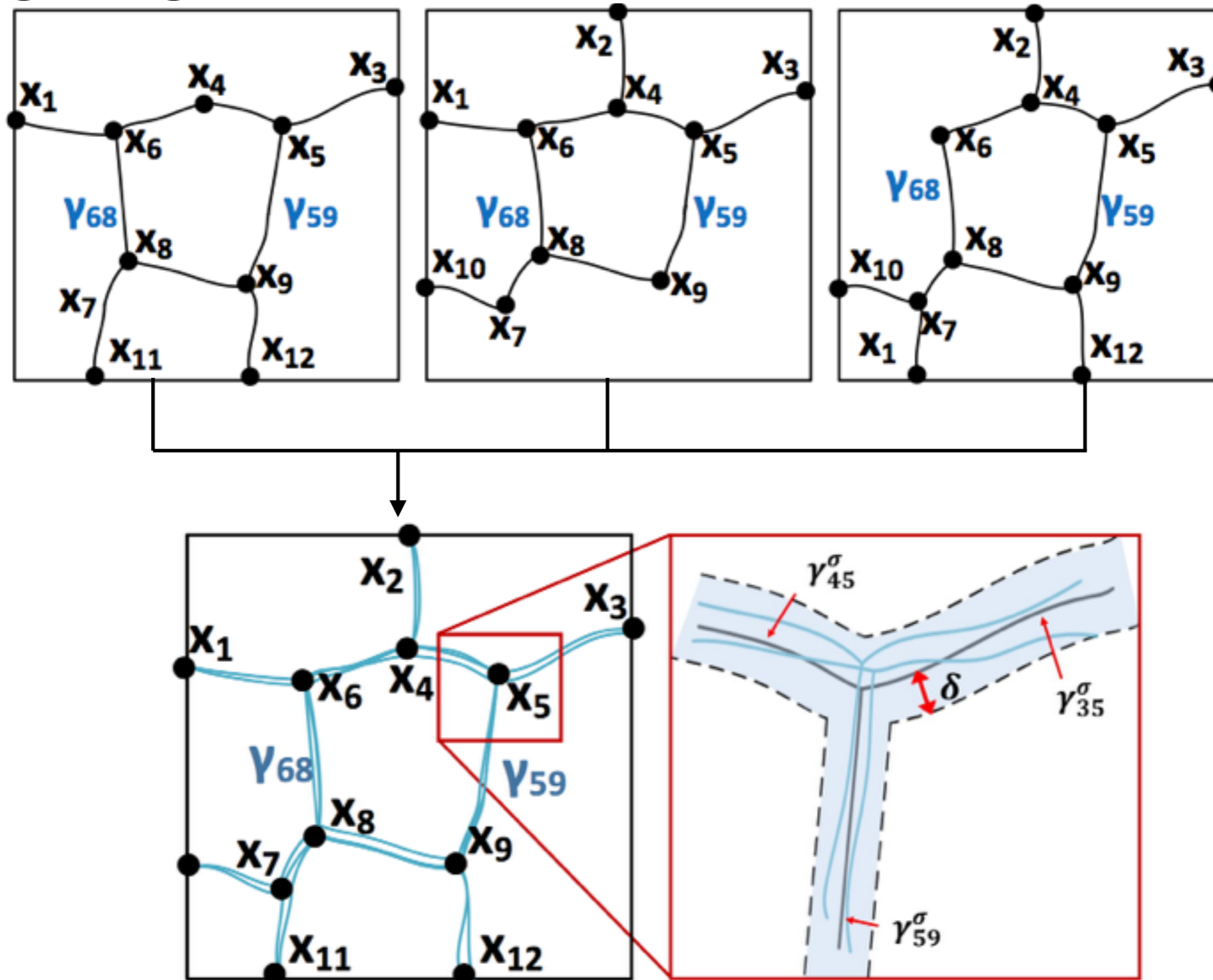


Consensus-based Image Segmentation



Consensus-based Image Segmentation

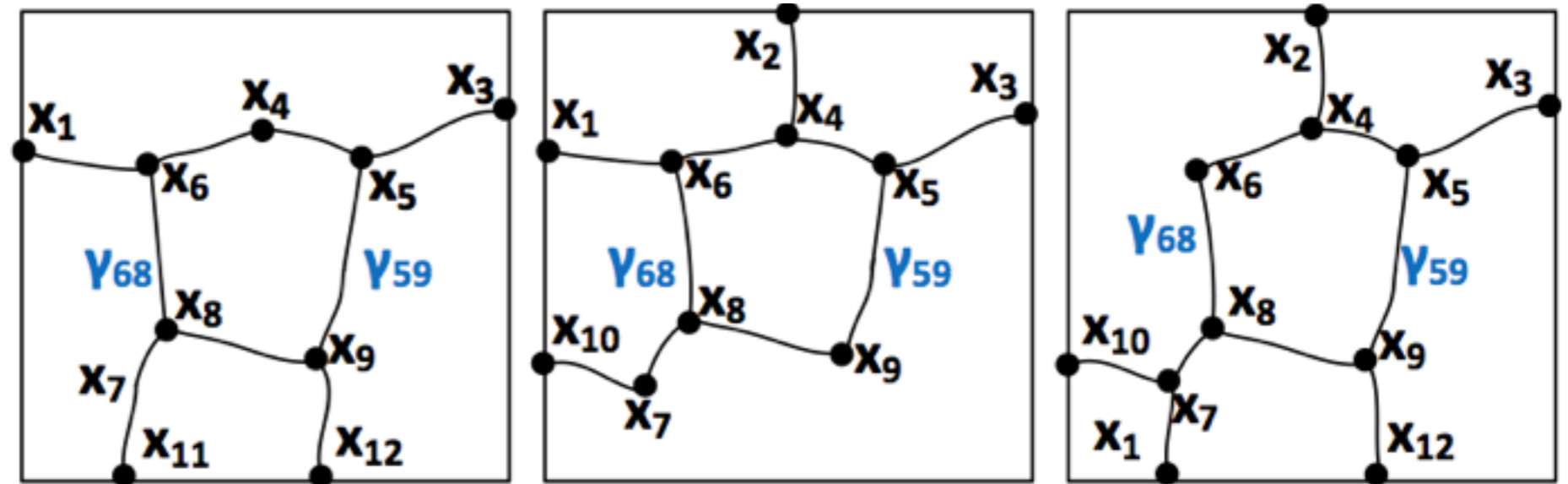
- Image segmentation model



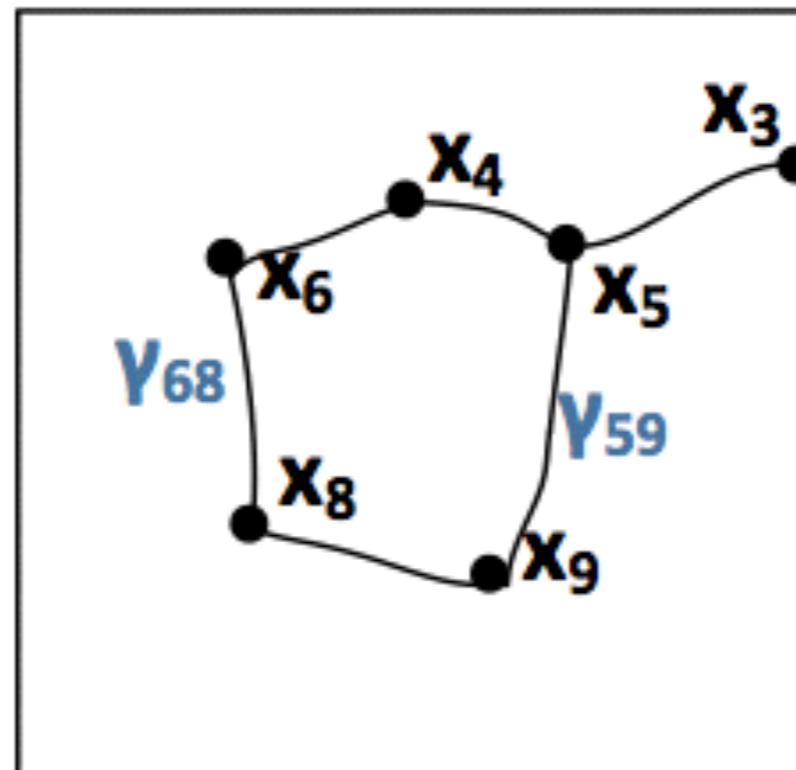
Consensus-based Image Segmentation

- Image segmentation model

Input

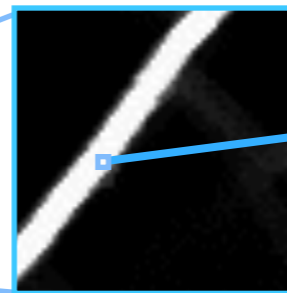
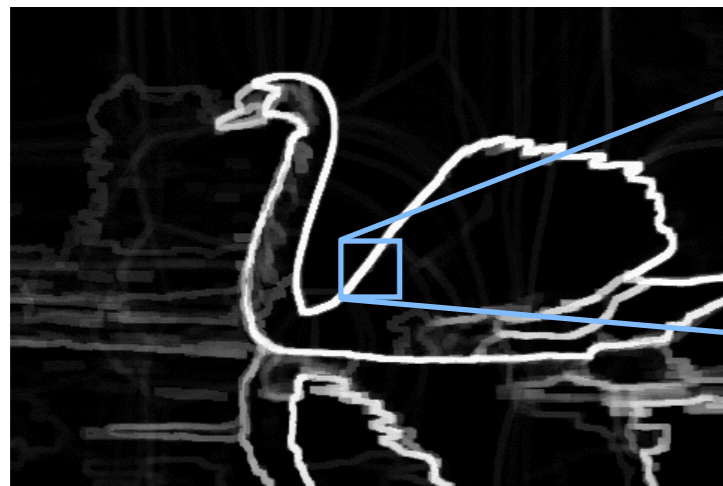


Segmentation Result



Consensus-based Image Segmentation

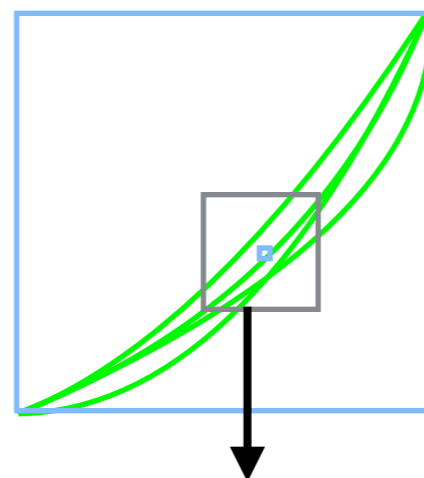
- **Probability map construction**



Probability of edge
at this pixel



Overlay



$$D^*(X) = \frac{\# \text{ edge}}{\# \text{ segmentations}}$$

A small patch around pixel X

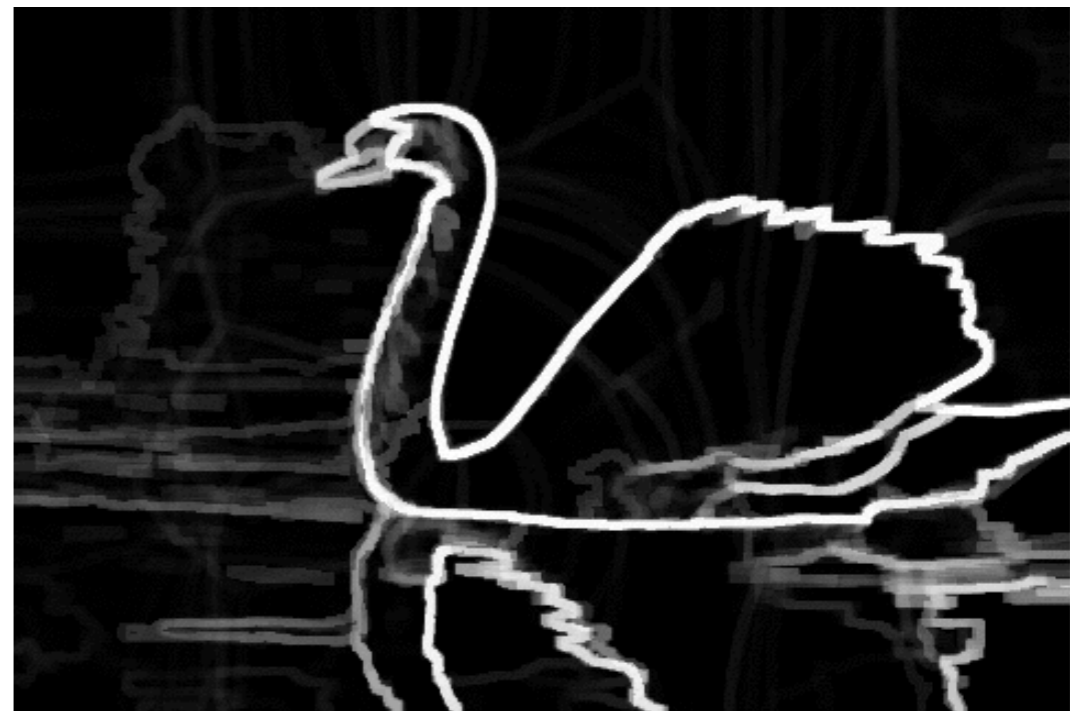
Consensus-based Image Segmentation

- **Probability map construction**



Connection probability map

$$1 - D_n^*(x)$$

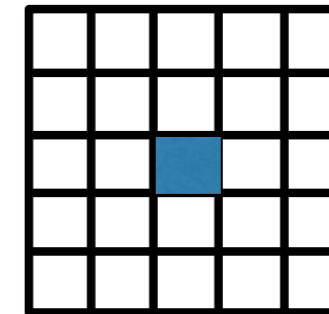
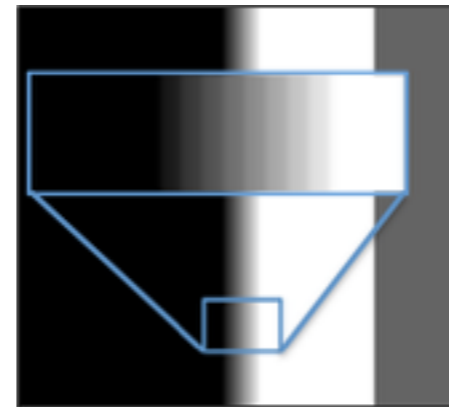


Edge probability map

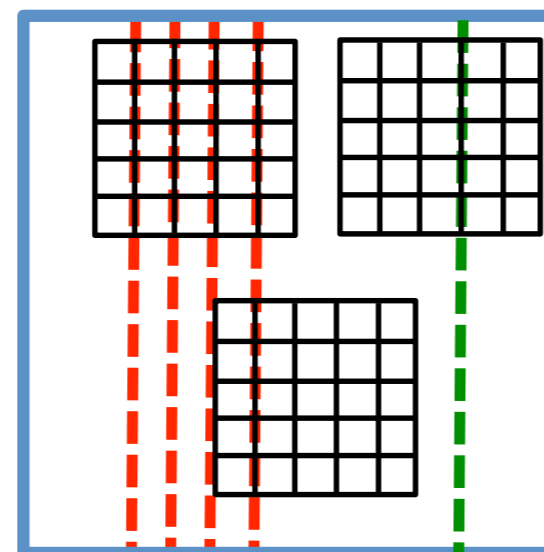
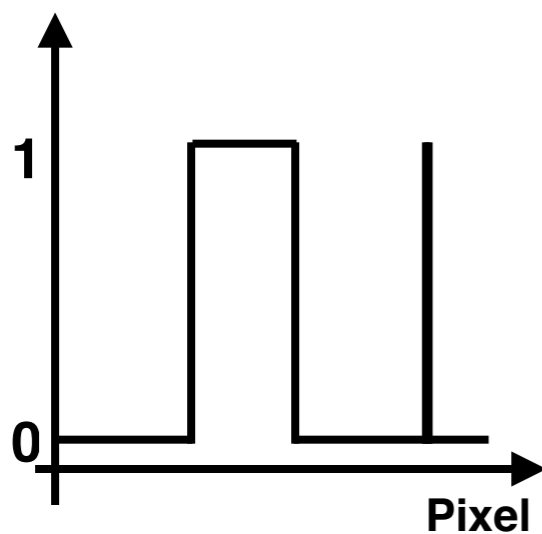
$$D_n^*(x)$$

Consensus-based Image Segmentation

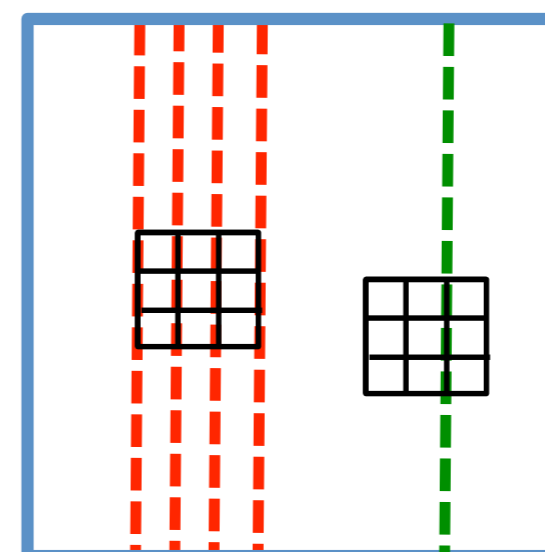
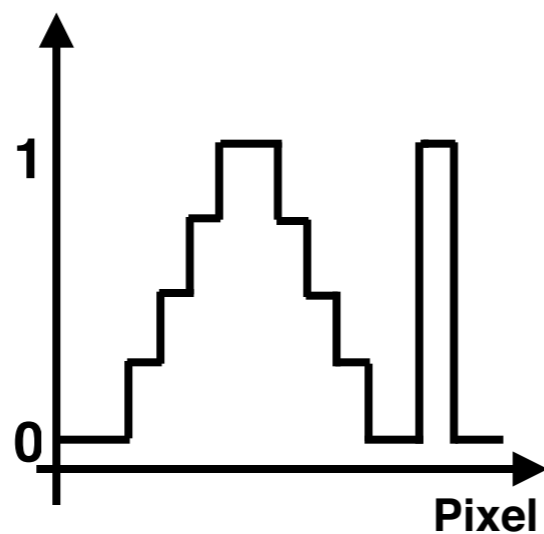
- Effect of patch size n



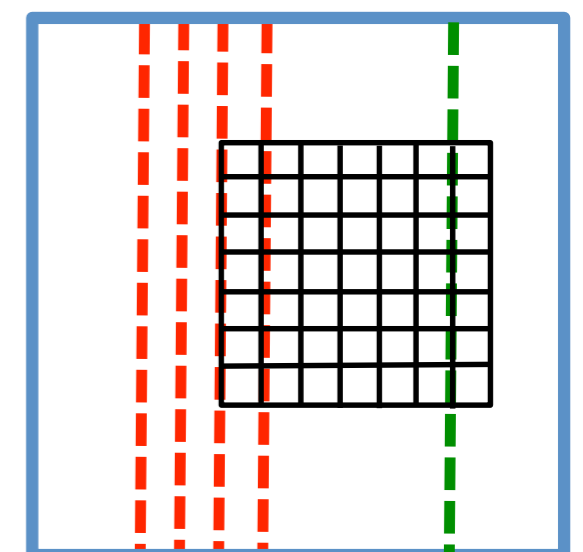
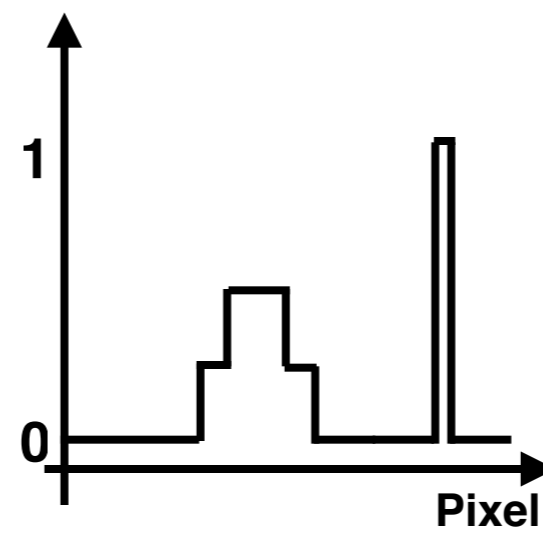
True Probability



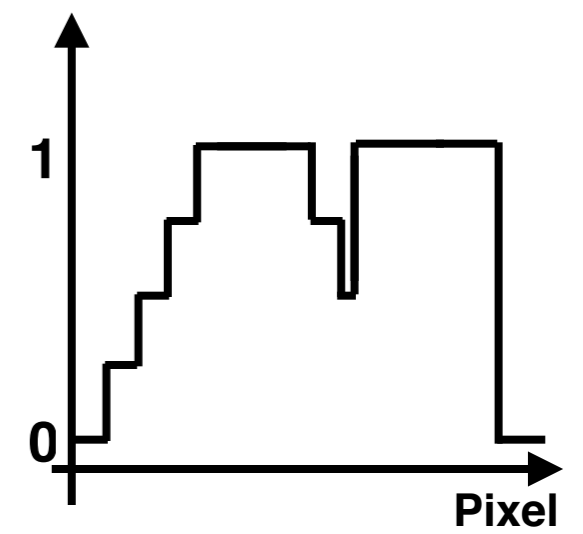
Proper Patch



Small Patch

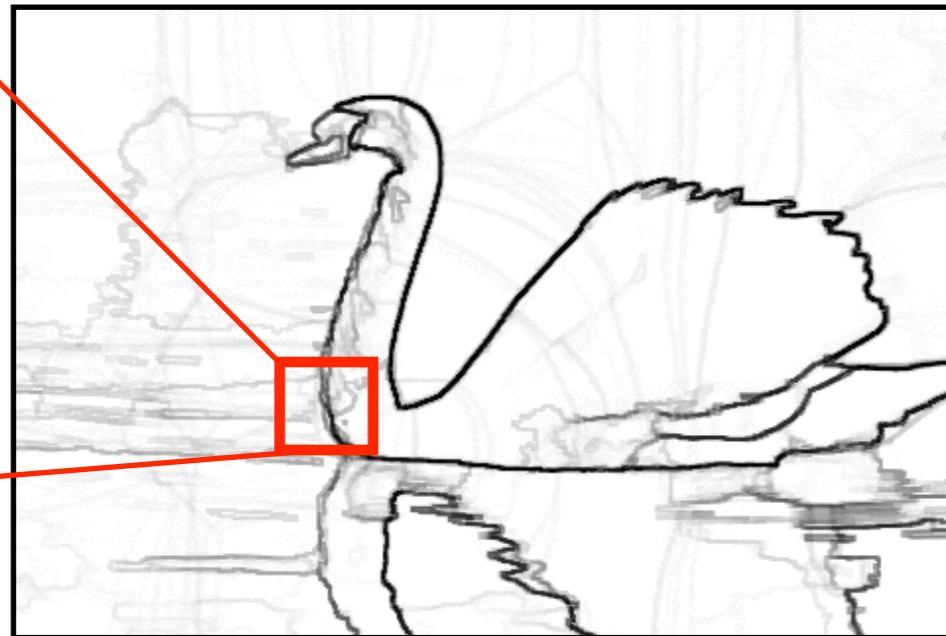


Large Patch



Consensus-based Image Segmentation

- Effect of patch size n



$n=3$



$n=5$



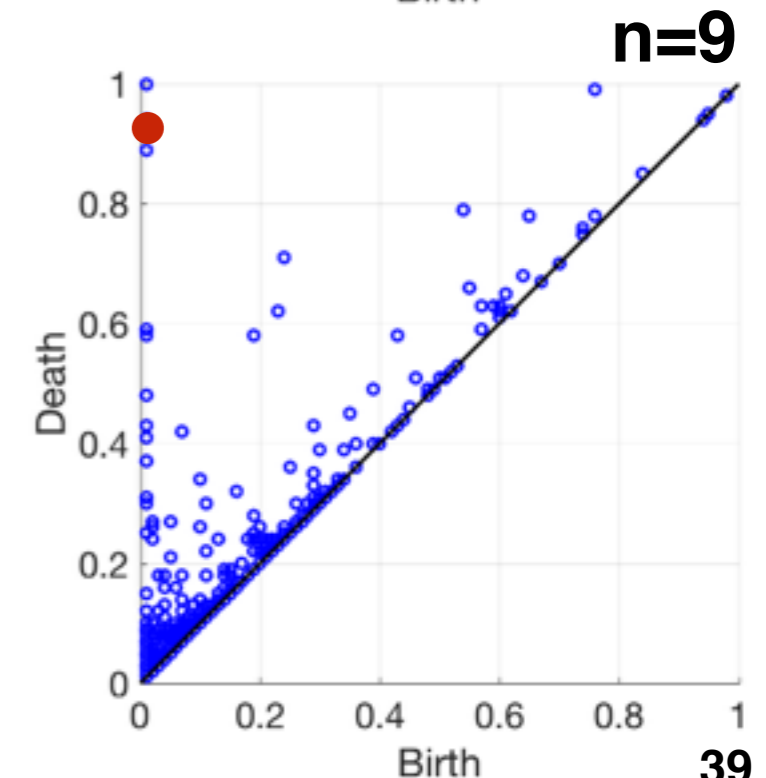
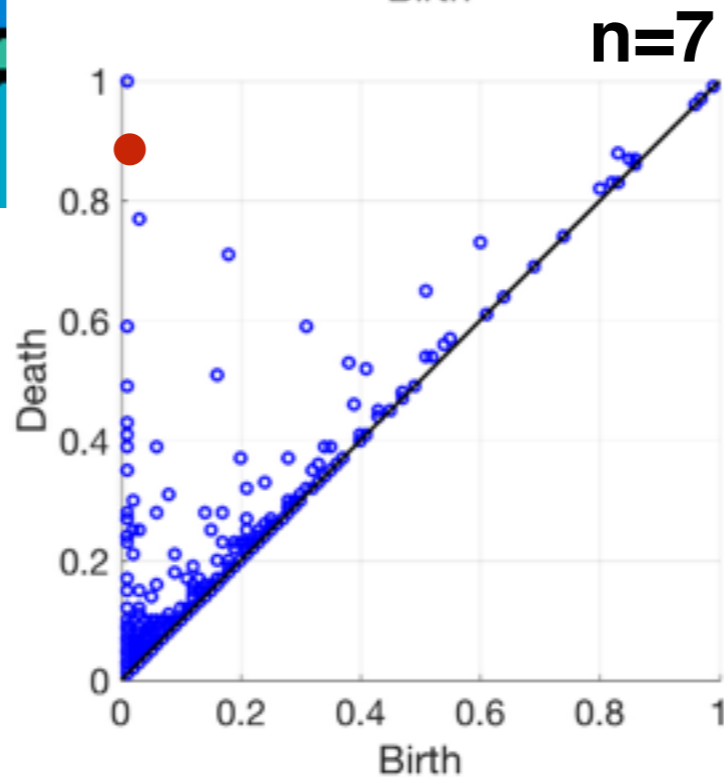
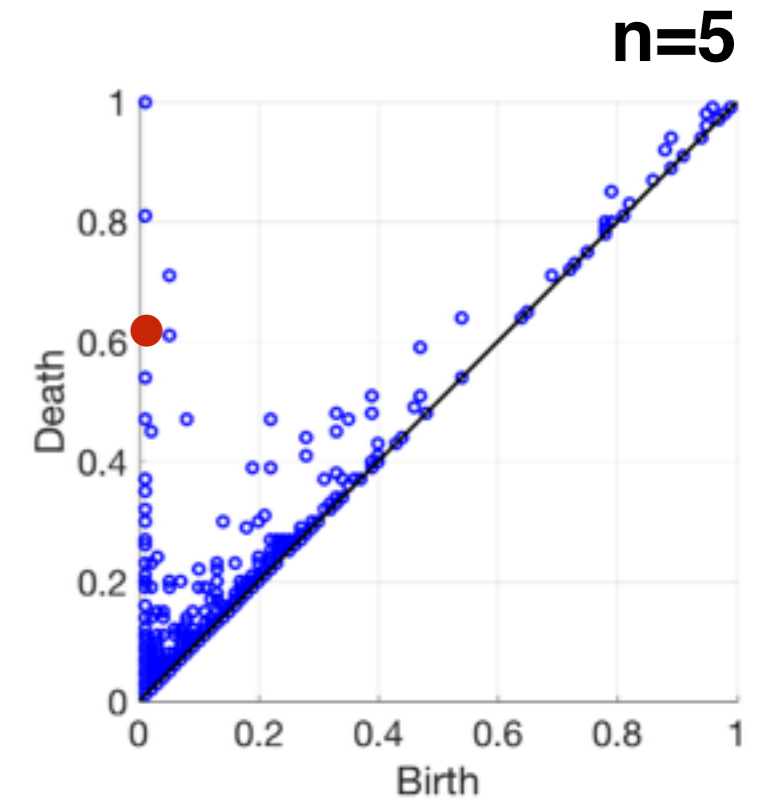
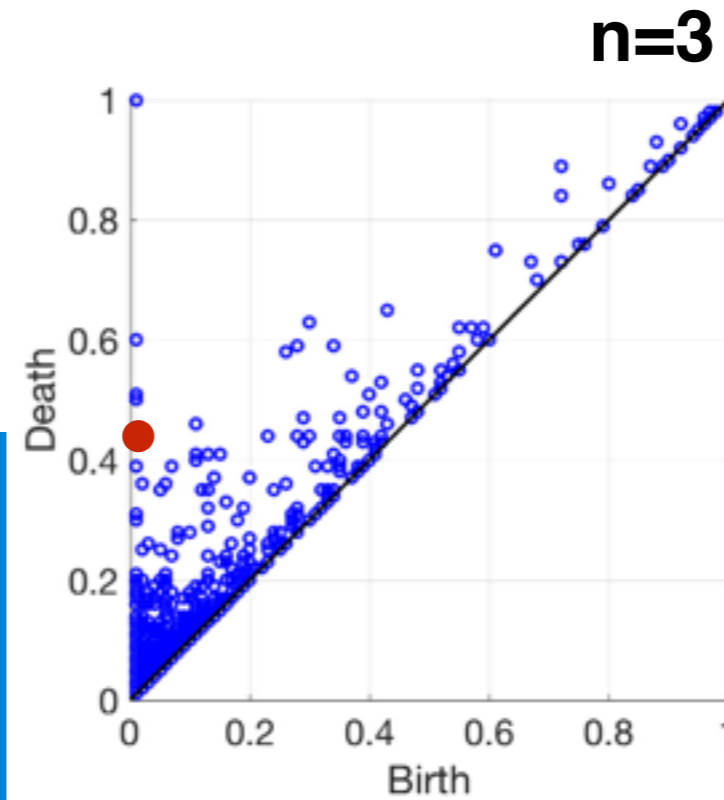
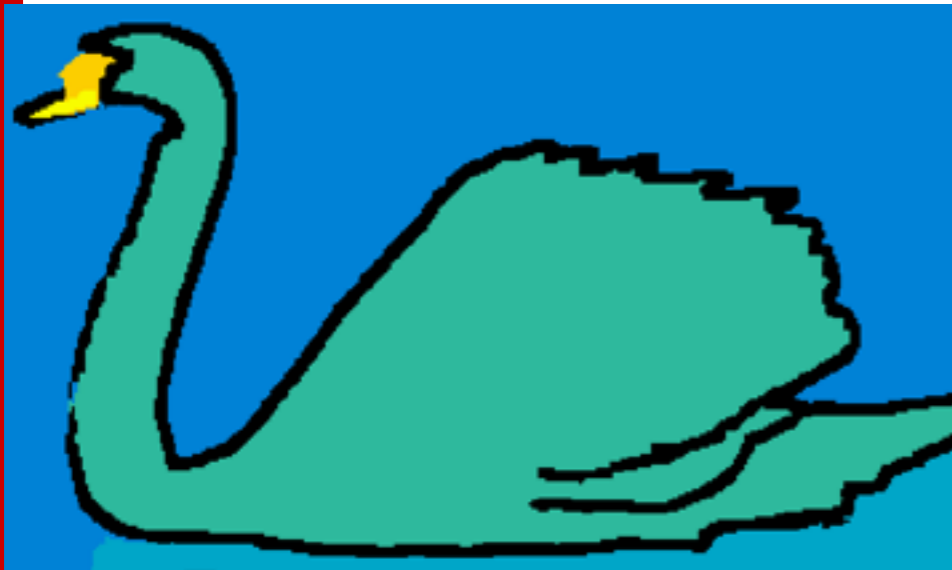
$n=7$



$n=9$

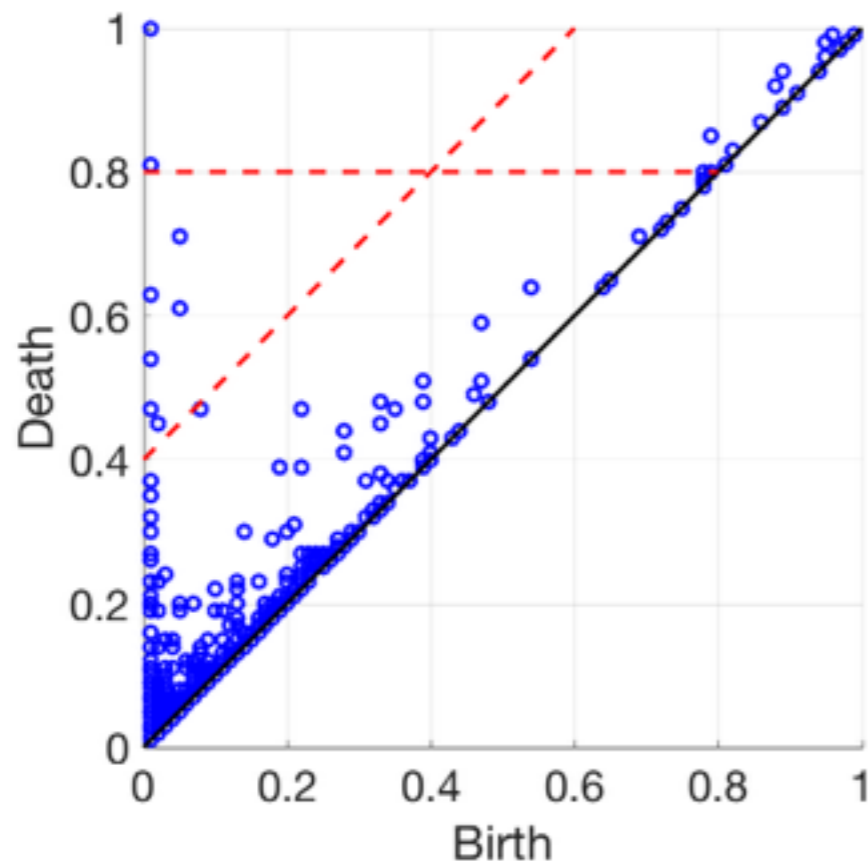
Consensus-based Image Segmentation

- Persistence diagram



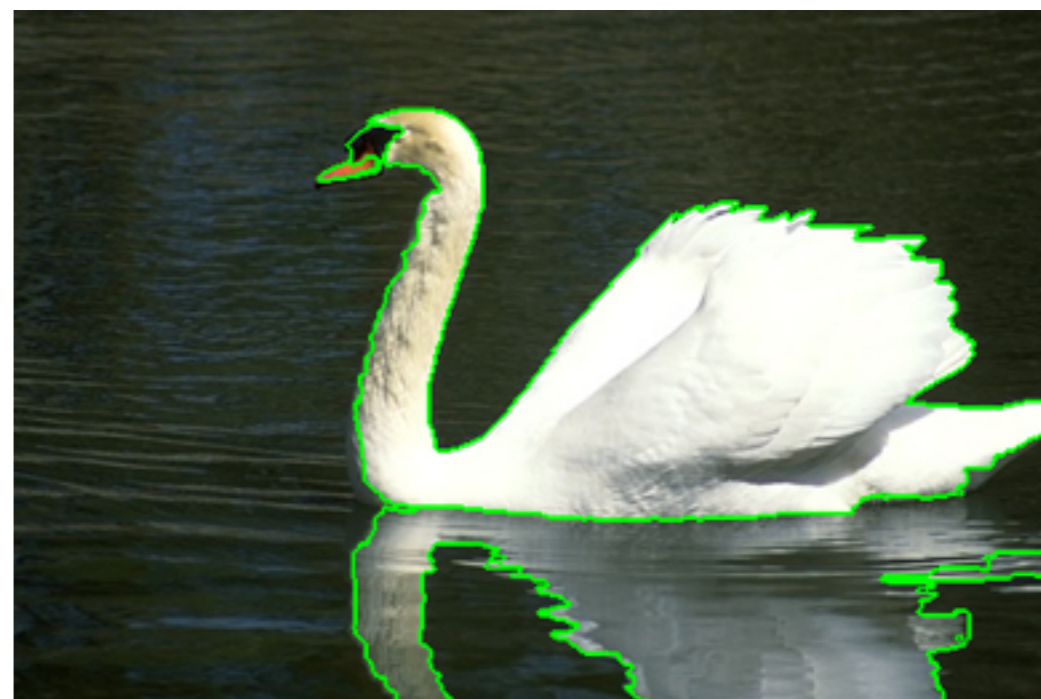
Consensus-based Image Segmentation

- **Thresholding persistence diagram**
 - **Persistence threshold** - extract persistent region and remove noise.
 - **Probability threshold** - make sure capture edges being present in high probability.



Consensus-based Image Segmentation

- Segmentation obtained by color-based region growing



Consensus-based Image Segmentation

- **Experiment - Input set generation**
 - **Dataset - Berkeley Segmentation Database**
 - **Four input algorithms: SAS, Normalized Cuts, Graph-based and Mean Shift**
 - **SAS: number of region varying from 5 to 30**
 - **Normalized Cuts: number of region varying from 5 to 30**
 - **Graph-based: σ varying from 0.4 to 0.8, k varying from 500 to 5000**
 - **Mean Shift: k1 varying from 2 to 15, k2 varying from 7 to 15**
 - **238 input segmentations in total**
 - **Probability are weighted by number of input from each algorithm**

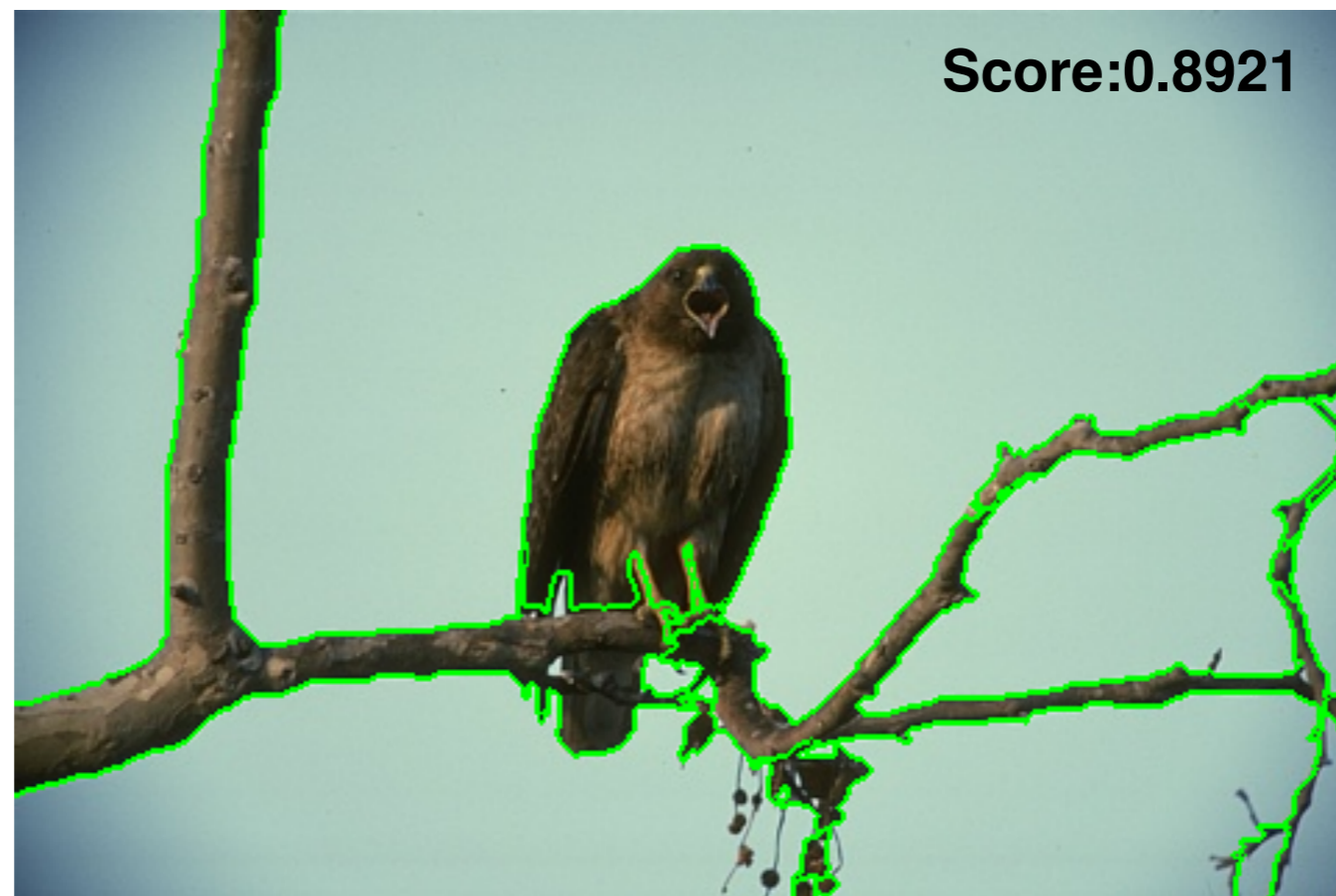
Consensus-based Image Segmentation

- Experiment - Result



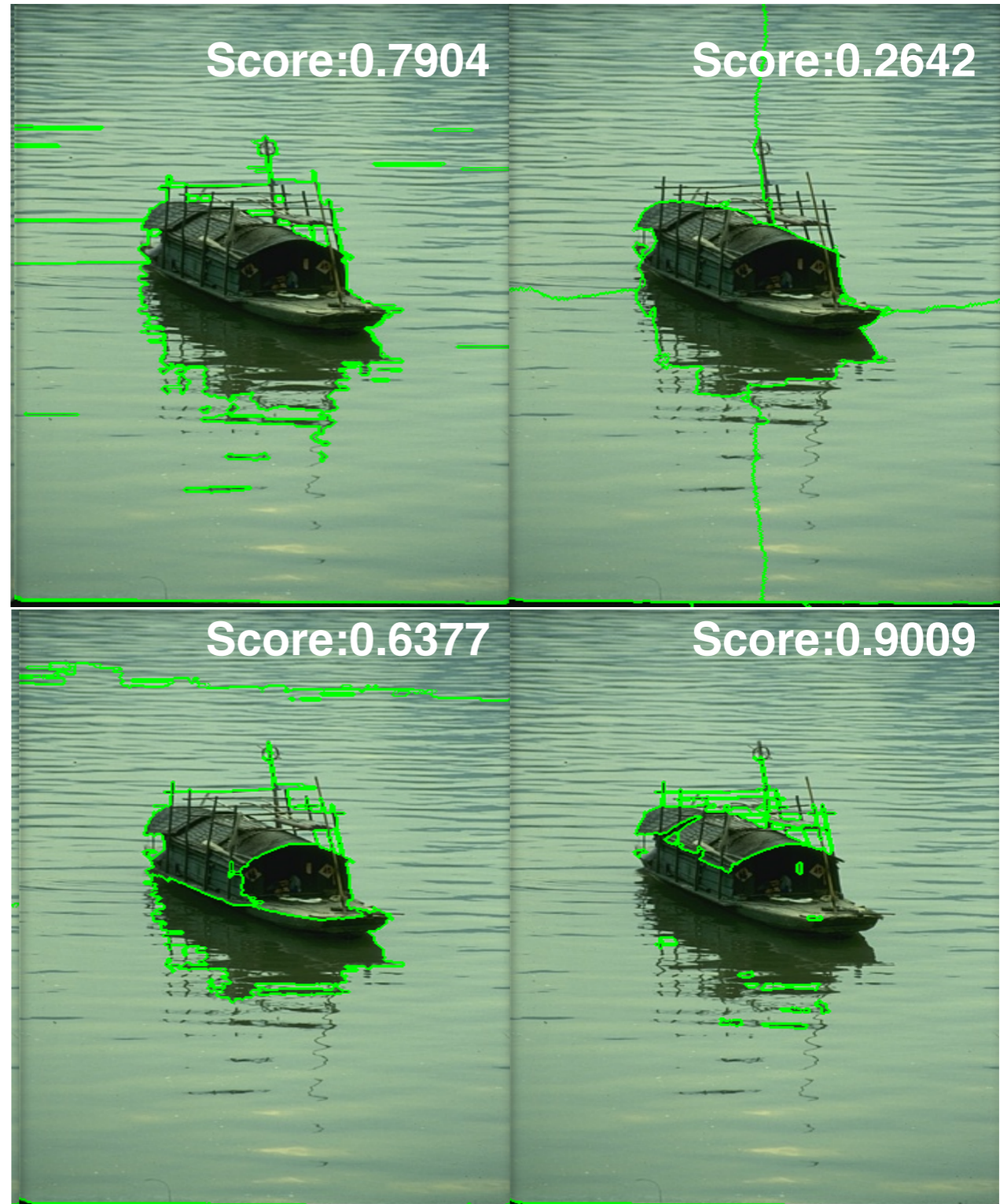
Consensus-based Image Segmentation

- Experiment - Result



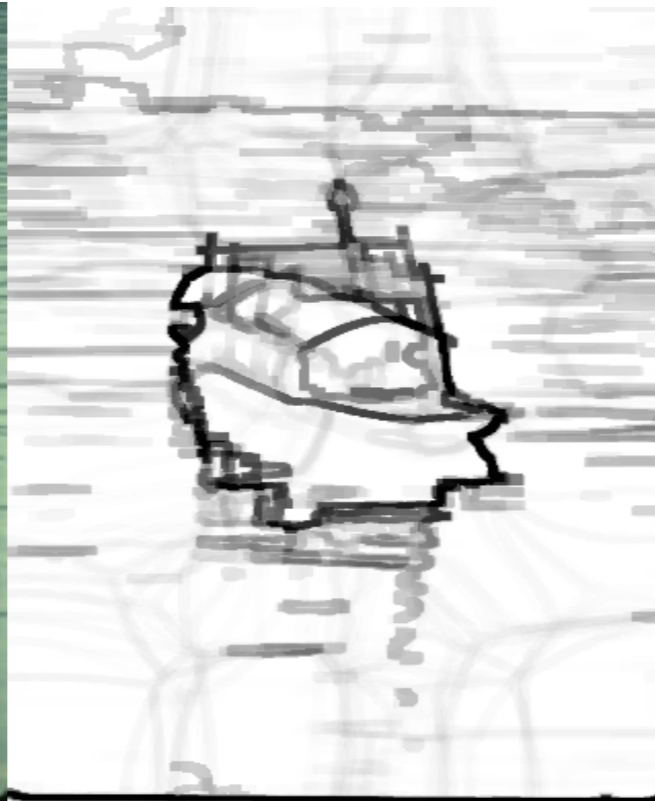
Consensus-based Image Segmentation

- **Experiment - Result**



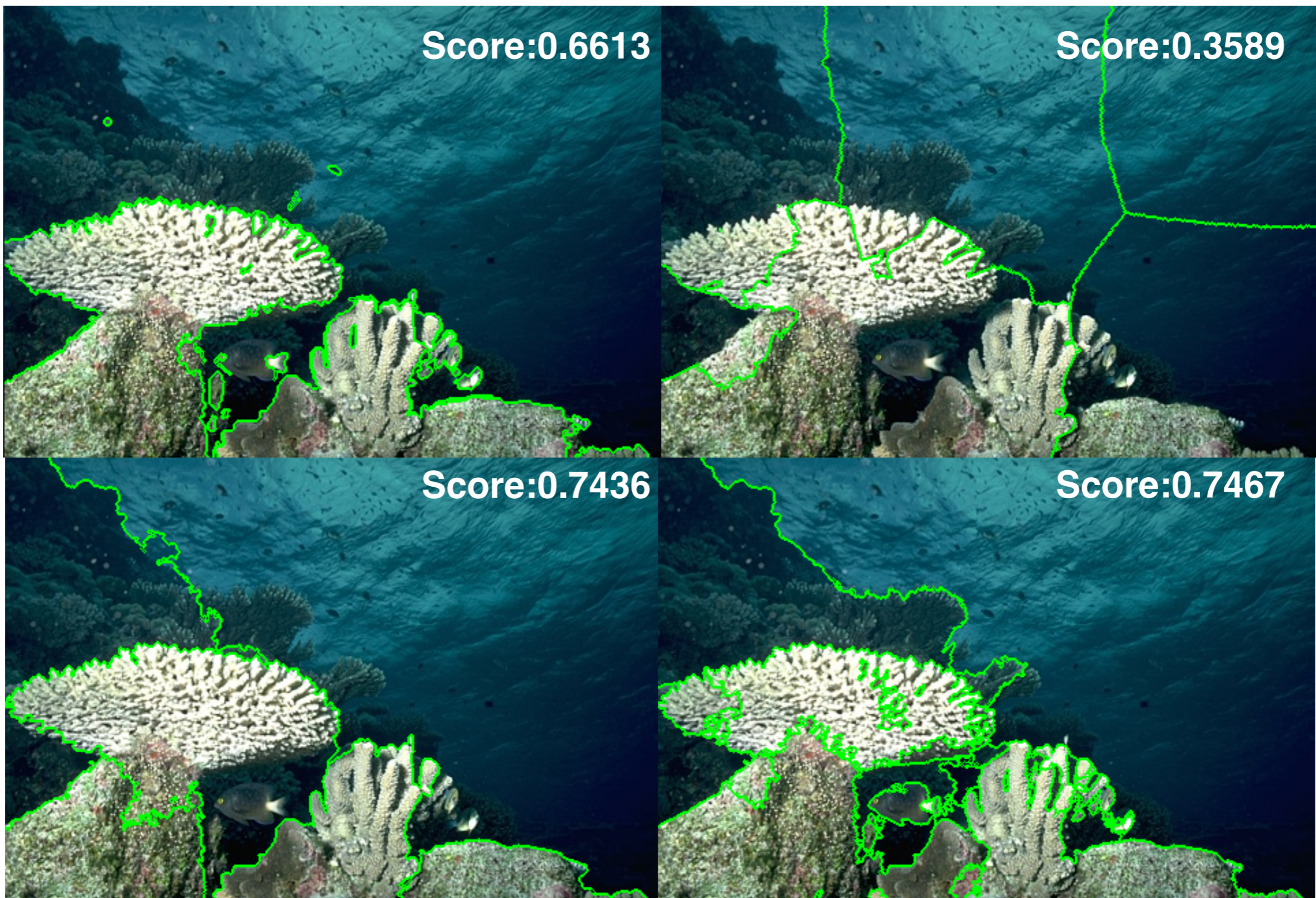
Consensus-based Image Segmentation

- Experiment - Result



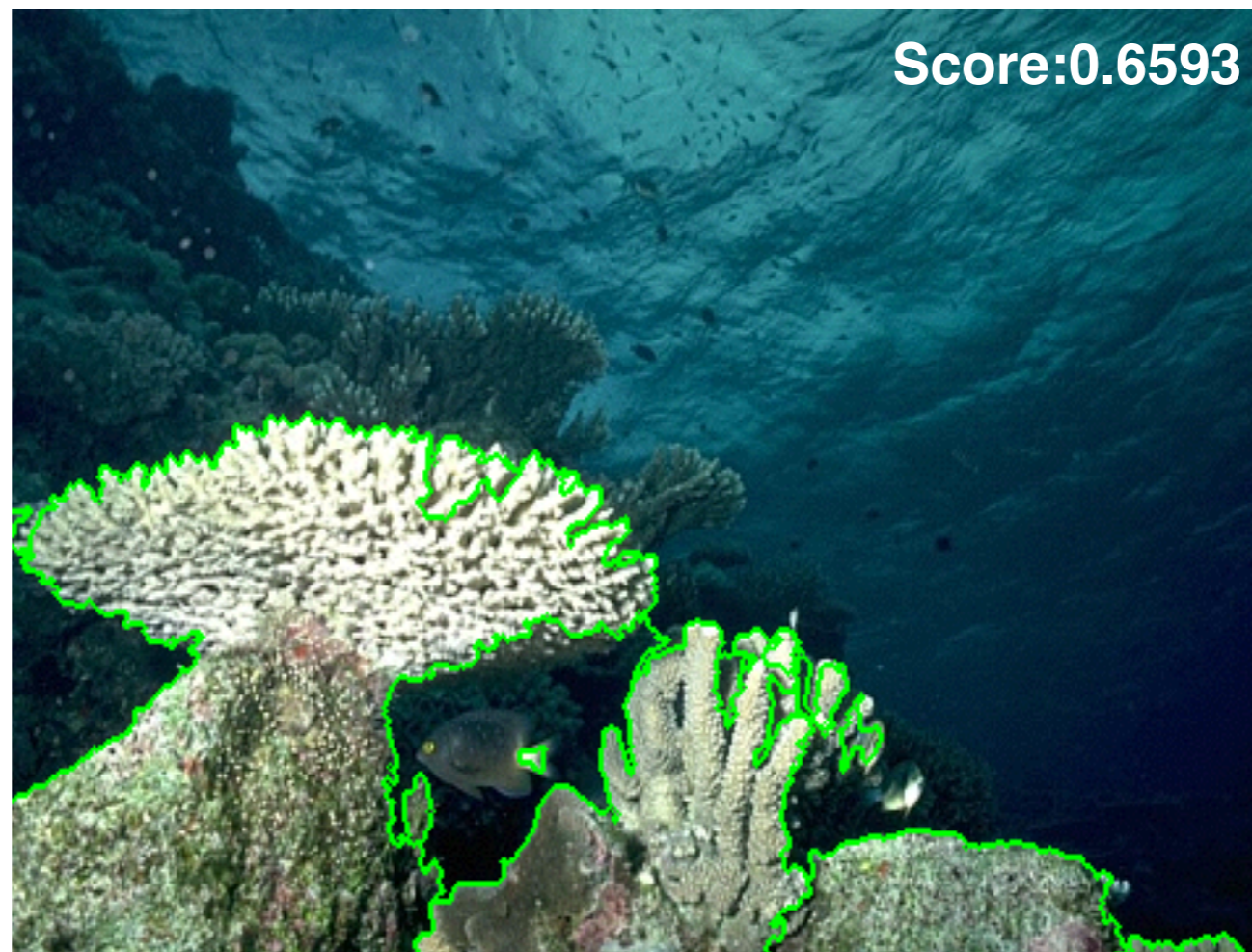
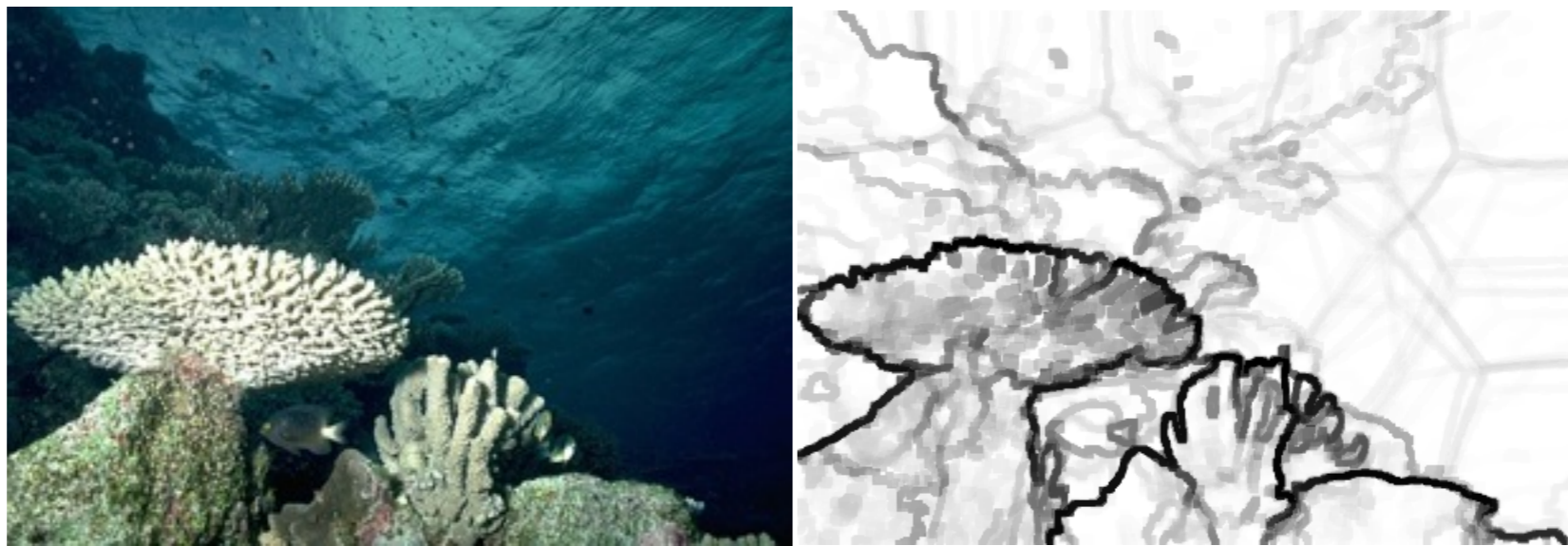
Consensus-based Image Segmentation

- Experiment - Result



Consensus-based Image Segmentation

- Experiment - Result



Consensus-based Image Segmentation

- **Experiment - Result**

- RSC - Coverage score
- VoI - Variation of information

Methods	Graph	NCuts	SAS	Mean Shift
RSC	0.5359	0.3970	0.5325	0.5540
VoI	2.1128	2.3515	1.8251	1.8946

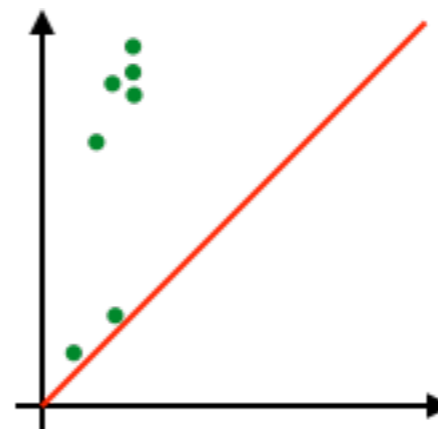
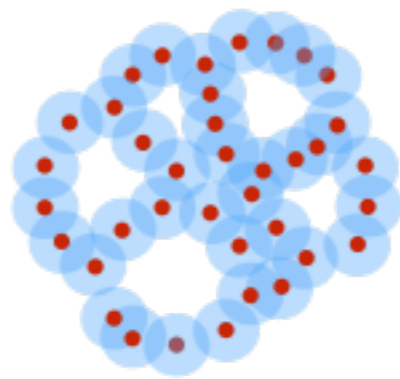
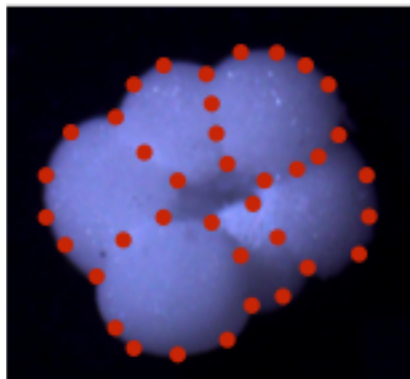
Methods	Consensus-base			
	$\tau = 0.30$	$\tau = 0.35$	$\tau = 0.40$	$\tau = 0.45$
RSC	0.5982	0.6085	0.5725	0.5731
VoI	1.7070	1.6700	1.7600	1.7930

Conclusion

- ▶ Present an innovative framework for image segmentation based on topological persistence which is robust to image conditions and parameter selection.
- ▶ Applied to consensus-based image segmentation which is able to get better segmentation results.
- ▶ Applied to obstacle detection in outdoor scene for autonomous driving which is robust to parameter selection.

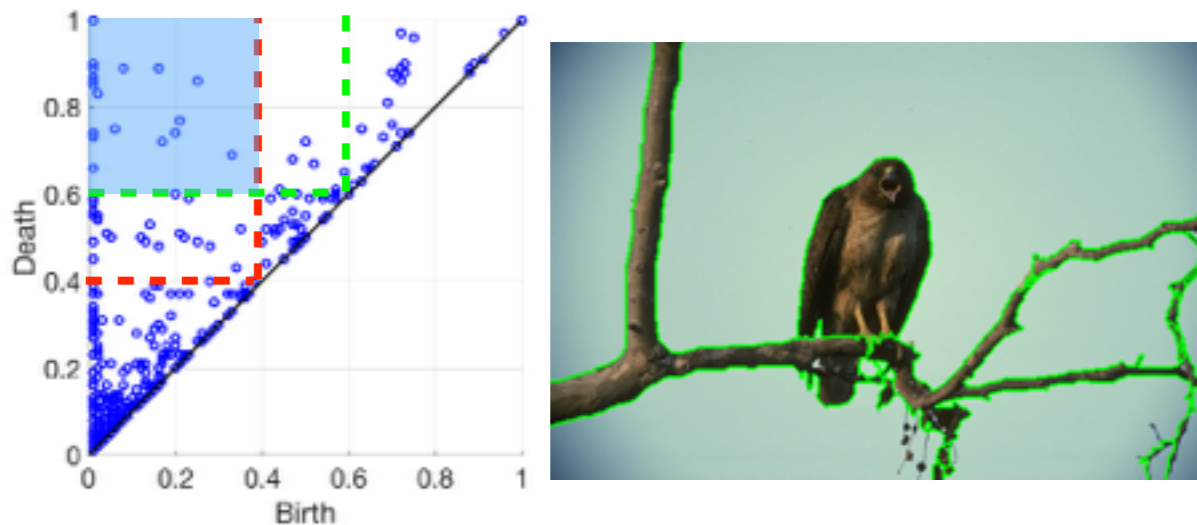
Future work

- **Work has to be done before graduation**
 - ▶ More experiments to demonstrate the robustness of the segmentation using topological persistence.
 - ▶ Extend the mathematical formulation of this work in order to provide guarantees of performance.
 - ▶ Collect image data of different species of foraminifera (forams) and apply topological persistence theory on the dataset to segment the structure of each forams as well as identify forams species.



Future work

- **Extension**
 - ▶ Find a better parameter selection strategy for consensus-based image segmentation.



- ▶ Refine the obstacle segmentation using Markov Random Field.



Publication

1. **Q.Ge** and E. Lobaton, “**Consensus-Based Image Segmentation via Topological Persistence**,” Intl. Workshop on Differential Geometry in Computer Vision and Machine Learning (DIFF-CVML) at CVPR, 2016.
2. S. Chattopadhyay, **Q. Ge**, C. Wei and E. Lobaton, “**Robust Multi-Target Tracking in Outdoor Traffic Scenarios via Persistence Topology based Robust Motion Segmentation**,” IEEE Global Conf. on Signal and Information Processing (GlobalSIP), 2015.
3. C. Wei, **Q. Ge**, S. Chattopadhyay, and E. Lobaton, “**Robust Obstacle Segmentation based on Topological Persistence in Outdoor Traffic Scenes**,” IEEE Symposium Series on Computational Intelligence (SSCI), 2014.
4. **Q. Ge**, N. Lokare, and E. Lobaton, “**Non-Rigid Image Registration under non-Deterministic Deformation Bounds**,” Intl. Symposium on Medical Information Processing and Analysis (SIPAIM), 2014.
5. N. Lokare, **Q. Ge**, W. Snyder, Z. Jewell, S. Allibhai, and E. Lobaton, “**Manifold Learning Approach to Curve Identification with Applications to Footprint Segmentation**,” IEEE Symposium Series on Computational Intelligence (SSCI), 2014.

Thanks!